PILE DRIVING ANALYSIS — SIMULATION OF HAMMERS, CUSHIONS, PILES, AND SOIL

by

Lee Leon Lowery, Jr. Assistant Research Engineer T. J. Hirsch Research Engineer and C. H. Samson, Jr. Research Engineer

Research Report 33-9

Piling Behavior Research Study No. 2-5-62-33

Sponsored by The Texas Highway Department

in cooperation with the

U. S. Department of Transportation, Federal Highway Administration Bureau of Public Roads

August 1967

÷

TEXAS TRANSPORTATION INSTITUTE Texas A&M University College Station, Texas

i

-

PREFACE

The information contained herein was developed on research study 2-5-62-33 entitled "Piling Behavior" which is a cooperative research study sponsored jointly by the Texas Highway Department and the U. S. Department of Transportation, Federal Highway Administration, Bureau of Public Roads. The broad objective of this study is to fully develop the use of a computer solution of the wave equation so that it may be used to predict driving stresses in piling and to estimate static load bearing capacity of piling.

This report concerns itself with the following specific items in the work plan as set forth in the study proposal:

1. To determine the effect of dynamic damping in concrete and steel piling on the impact longitudinal stress waves. This was accomplished by correlating theoretical stress waves with data obtained from full scale piles tested under controlled conditions.

2. To study the dynamic load-deformation properties of cushioning materials and their effect on the stress waves in piling. This was accomplished by correlating theoretical stress waves with data from full scale pile tests under controlled conditions. Theoretical results were compared with experimental data gathered for various cushion materials.

3. To evaluate the true energy output of different pile driving hammers (single acting steam hammers, double acting steam hammers, and open and closed end diesel hammers) using the wave equation to analyze portions of data obtained by the Michigan State Highway Commission and published in a report entitled "A Performance Investigation of Pile Driving Hammers and Piles."

4. To determine a uniform basis of rating pile driver energy output applicable to different type hammers.

5. To correlate the wave equation with suitable experimental test data.

During the course of investigation of the above items, the factors listed below were also found to influence the wave equation results, and therefore were also investigated and are reported herein:

1. A study of the effect of ram elasticity on piling behavior.

2. A study of the influence of parameters used to describe soil behavior.

The information reported herein is necessary in order to understand the dynamic behavior of piling and to properly simulate pile driving hammers, capblocks and cushion blocks, piles, and soils for wave equation analysis of piling behavior.

The opinions, findings and conclusions expressed in this report are those of the authors and not necessarily those of the Bureau of Public Roads.

LIST OF TABLES

Table		Page
3.1	Effect of Breaking the Ram Into Segments When Ram Strikes a Cushion	5
3.2	Effect of Breaking Ram Into Segments When Ram Strikes a Steel Anvil	5
3.3	Summary of Belleville Cases Solved by Wave Equation	7
3.4	Summary of Detroit Cases Solved by Wave Equation	8
3.5	Summary of Muskegon Cases Solved by Wave Equation	8
3.6	Effect of Cushion Stiffness on ENTHRU for BLTP-6; 10.0	9
3.7	Effect of Cushion Stiffness on FMAX for BLTP-6; 10.0	9
3.8	Effect of Cushion Stiffness on LIMSET for BLTP-6; 10.0	9
3.9	Data Reported in the Michigan Study	
3.10	Summary of Results for Michigan Steam Hammers	12
3.11	Summary of Results for Michigan Diesel Hammers	14
3.12	Comparison of Energy Output Measured Experimentally With That Predicted by Equation 3.6, for Diesel Hammers	16
3.13	Comparison of Measured Output With That Given by Equation 3.7, for Single Acting Steam Hammers	16
3.14	Comparison of Measured Energy Output With That Predicted by Equation 3.11, for Double Acting Steam Hammers	16
3.15	Summary of Hammer Properties and Operating Characteristics	18
3.16	Effect of Removing Load Cell on ENTHRU, LIMSET, and Permanent Set of Pile	19
3.17	Effect on ENTHRU Resulting From Removing the Load Cell Assembly	20
3.18	Effect of Cushion Stiffness on Maximum Point Displacement for Case BLTP-6; 10.0 and 57.9	20
3.19	Effect of Coefficient of Restitution on ENTHRU for Case BLTP-6; 10.0 and 57.9	20
3.20	Effect of Coefficient of Restitution on Maximum Point Displacement for Case BLTP-6; 10.0 and 57.9	21
3.21	Study of Various Hammers Driving the Same Pile	21
4.1	Suspended Pile Data	22
4.2	Dynamic Cushion Properties	24
5.1	Dynamic Properties of New Cushion Blocks of Various Materials	27
6.1	Comparison of Results Found by Using Elastic-Plastic vs Non-Linear Soil Resistance Curves	32
6.2	Influence of Soil Quake at Different Soil Resistances for Case BLTP-6; 57.9 With No Soil Damping	
6.3	Influence of Soil Damping on Different Soil Resistances for Case BLTP-6; 57.9 $(Q = 0.1 \text{ for All Cases})$	33

Pile Driving Analysis - Simulation of Hammers, Cushions, Piles, and Soil

Chapter I

INTRODUCTION

General Background

The problem of pile-driving analysis has been of great interest to engineers for many years. Ever since the first engineer proposed a method for predicting the load carrying capacity of a pile, the whole subject of pile driving has become a much debated field in engineering. In other areas new methods of analysis for structural elements and systems are constantly being proposed with little or no resulting discussion. However, the proposal of a new piling analysis is sure to stir much interest and often some rather heated discussions.

Since over four-hundred pile-driving formulas have been proposed,¹ not including the countless formula modifications which are used,² many engineers resort to the use of only one or two formulas regardless of the driving conditions encountered.³ Although many of the erroneous assumptions made in these formulas have been widely discussed,^{4,5} the fact that they omit many significant parameters which affect the problem seems to have received less attention. However, when the driving formulas omit parameters which change from case to case, the engineer has no means of determining how significant the parameter may be, nor can he tell in which direction or to what extent the change will vary the results. Thus, to obtain an accurate solution obviously requires that fewer erroneous assumptions be made regarding the dynamic behavior of the materials and equipment used in pile driving, and that all significant parameters are included in the analysis.

The first of these problems was solved when it was noted that pile driving is actually a case of longitudinal impact, governed by the wave equation rather than by statics or rigid-body dynamics.^{6,7} However, since the exact simulation and solution of the wave equation applied to piling are extremely complex for all but the simplest problems, many significant parameters still had to be neglected.

The second problem was solved by Smith⁸ who proposed a numerical solution to the wave equation, capable of including any of the known parameters involved in pile-driving analysis. This method of analysis was applicable to tapered, stepped, and composite piles, to nonlinear soil resistances and damping, to piles with cushions, followers, helmets, etc. In other words, it was a completely general method of analysis for the problem of pile driving.

It should be noted that much of the experimental work used in this report was reported by other investigators. These cases are referenced, and the problem number or name used herein will be the same as used by the original reporter. This will enable the reader to determine any additional information about the problem being solved by referring to the original paper.

Objectives

The objectives of this research were:

1. To review and summarize Smith's original method of analysis and to derive a more general solution.

2. To determine how the numerical solution is affected by the elasticity of the ram.

3. To determine the energy output of different type pile hammers.

4. To compare results given by the wave equation with those determined by laboratory experiments and field tests.

5. To illustrate the significance of the parameters involved, including cushion stiffness and damping, ram velocity, material damping in the pile, soil damping and quake, and to determine the quantitative effect of these parameters where possible.

6. To show how the wave equation can be used to determine the dynamic or impact characteristics of the materials involved.

7. To determine the dynamic properties of the cushion subjected to impact loading.

8. To study the effect of internal damping in the pile and its significance.

Literature Review

The basic purpose of any pile driving formula is to permit the design of a functional yet economical foundation. According to Chellis,⁹ there are four basic types of driving formulas:

1. Empirical formulas, which are based on statistical investigations of pile load tests,

2. Static formulas, which are based on the side frictional forces and point bearing force on the pile, as determined by soils investigations,

3. Dynamic formulas, which assume that the dynamic soil resistance is equal to the static load capacity of the pile, and

4. The wave equation, which assumes only those material properties whose dynamic behavior is not completely understood and has not yet been determined experimentally. Each of the preceding formulas has advantages and disadvantages which have been widely noted^{10,11} and need not be restated at this time.

Isaacs is thought to have first noted that the wave equation is applicable to the problem of pile driving.¹² However, Fox¹³ was probably the first person to propose that an exact solution be used for pile-driving analysis. Shortly thereafter, Glanville, Grime, Fox, and Davies¹⁴ published the first correlations between experimental studies and results determined by the exact solution to the wave equation developed by Fox. Since this exact solution was extremely complex, they were forced to use simplified boundary conditions including zero side frictional resistance, a perfectly elastic cushion block, and an elastic soil spring acting only at the tip of the pile. However, even using these simplified boundary conditions, they obtained reasonably accurate results.

In 1940 Cummings¹⁵ discussed several errors inherent in dynamic pile-driving formulas and reviewed the previous work done using the wave equation. However, he also noted that even for the simplest problems, "the complete solution includes long and complicated mathematical expressions so that its use for a practical problem would involve laborious numerical calculations."

A practical pile-driving problem usually involves side frictional soil resistance, soil damping constants, nonlinear cushion and capblock springs, and other factors which prevent a direct solution of the resulting differential equation. However, in 1950 Smith¹⁶ proposed a mathematical model and a corresponding numerical method of analysis which accounted for the effects of many of these parameters. He has continued to update this method and published various other works.^{17,18,19,20,21}

Smith's method of analysis did not really become popular until 1960 when he published a summary of the method's application to the problem of pile-driving analysis.²² In this paper he recommended a number of material constants and the material behavior curves required to account for the dynamic action of the soil, cushion, and pile material.

Smith's method of analyzing pile-driving problems received considerable interest,²⁸ and two immediate applications of the wave equation were suggested:

1. The immediate application of the wave equation, using the most probable material properties to predict ultimate driving resistance and driving stresses.

2. Its use to perform extensive parameter studies in order to determine trends and to gain more insight into the behavior of pile driving, and also determine the relative significance of these parameters. Immediately after the appearance of Smith's paper in 1960, the Bridge Division of the Texas Highway Department initiated a research project with the Texas Transportation Institute to perform exhaustive studies of the behavior of piling by the wave equation. The first report dealt with a computer program based on Smith's numerical solution.²⁴ This program was used to determine the driving stresses induced in a number of prestressed concrete piles which had failed during driving,²⁵ and later to check the conditions at similar sites at which pile breakage due to excessive driving stresses might be experienced.²⁶

Forehand and Reese²⁸ investigated the possibility of predicting the ultimate bearing capacity of piling using the wave equation, but since complete data were available for relatively few problems, they were unable to draw many firm conclusions. They also studied the dynamic action of the soil during driving and recommended some values for the soil parameters used in the wave equation.

In August, 1963 several extensions of Smith's method were presented by the writers.²⁹ Two simple cases for which "exact" solutions were known were compared with Smith's numerical solution to indicate the method's accuracy. A third section of the paper presented the results of a short parameter study which indicated how certain trends in pile driving might be determined and how to study the significance of various parameters. The results for several theoretical and field test problems were also compared.

In 1963 the writers³⁰ published a study on the methods employed in measuring dynamic stresses and displacements of piling during driving, and presented further experimental and theoretical comparisons "to demonstrate that the computer solution of the wave equation offers a rational approach to the problems associated with the structural behavior of piling during driving." This report was based on an earlier study dealing with driving prestressed concrete piles.³¹

An investigation by Hirsch³² involved a study of the variables which affected the behavior of concrete piles during driving. Over 2100 separate problems were solved and the results were presented in the form of graphs for use by design engineers.

Later publications dealt with the dynamic loaddeformation properties of various pile cushion materials and other dynamic properties of materials required to simulate as closely as possible the actual behavior of a pile during driving.^{83,84,85,36}

Chapter II

A NUMERICAL METHOD OF ANALYSIS

The Basic Solution

Since 1931, it has been realized that pile driving involved theories of longitudinal impact rather than statics. However, the application of the wave equation to pile driving was restricted to very simple problems because the exact solution was complex, involved much labor, and for most practical cases, required many simplifying assumptions.

In 1950, Smith³⁷ proposed an approximate solution based on concentrating the distributed mass of the pile, as shown in Figure 2.1a, into a series of small weights, W(1) thru W(MP), connected by weightless springs



Figure 2.1. Idealization of a pile for purpose of analysis.

K(1) thru K(MP-1), with the addition of soil resistance acting on the masses, as illustrated in Figure 2.1b. Time also was divided into small increments. This numerical solution was then applied by the repeated use of the following equations, developed by Smith:³⁸

$$D(m,t) = D(m,t-1) + 12\Delta t V(m,t-1)$$
 Eq. 2.1

$$C(m,t) = D(m,t) - D(m+1,t)$$
 Eq. 2.2

$$F(m,t) = C(m,t)K(m)$$
 Eq. 2.3

$$R(m,t) = \begin{bmatrix} D(m,t) - D'(m,t) \\ K'(m) [1+J(m)V(m,t-1)] \end{bmatrix} Eq. 2.4$$

$$V(m,t) = V(m,t-1) + [F(m,t) - R(m,t)]$$

g $\Delta t/W(m)$ Eq. 2.5

where *m* is the mass number, *t* denotes the time interval number, Δt is the size of the time interval (sec), D(m,t) is the total displacement of mass number *m* during time interval number t(in.), V(m,t) is the velocity of mass *m* during time interval t(ft/sec), C(m,t) is the compression of spring *m* during time interval t(in.), F(m,t) is the force exerted by spring number *m* between segment numbers (m) and (m+t) during time interval t(lb), and K(m) is the spring rate of mass *m* (lb/in.). Note that since certain parameters do not change with time, they are assigned single rather than double subscripts.

The quantity R(m,t) is the total soil resistance acting on segment m(lb/in.); K'(m) is the spring rate of the soil spring causing the external soil resistance force on mass m(lb/in.); D(m,t) is the total inelastic soil displacement or yielding during the t at segment m(in.); J(m) is a damping constant for the soil acting on segment number (m) (sec/ft); g is the gravitational acceleration (ft/sec²); and W(m) is the weight of segment number m(lb).

The solution is begun by initializing the timedependent parameters to zero and by giving the ram an initial velocity. Then an incremental amount of time Δt elapses during which the ram moves down an amount given by Equation 2.1. The displacements D(m,I) of the other masses are computed in the same manner.

Equation 2.2 is then used to determine the compressions C(m,I), after which the internal spring forces acting between the masses are found from Equation 2.3 and the external soil forces R(m,I) are computed from Equation 2.4.

Finally, a new velocity V(m,I) is determined for each mass using Equation 2.5, after which another time interval elapses. New displacements, compressions, forces, and velocities are again computed using the same equations and the cycle is repeated until the solution is obtained. Smith³⁹ and others,^{40,41} give a detailed explanation of this method of solution and the computer programming required. The dynamic behavior of various parameters will be discussed later.

Smith would have probably caused little interest had he simply given a numerical solution for the wave equation. Instead he presented a simple, physical model, easily visualized, using parameters which are readily understood. This and the simplicity of the equations required for a solution doubtlessly account for much of the wave equation's increasing popularity as a means of studying the behavior of piling.

Modifications of the Original Solution

Although the original method of analysis proposed by Smith can be used to solve many of the problems given in this report, it has been greatly extended to include other idealizations. The major additions and changes are summarized here for reference only, and are fully discussed in later chapters.

1. The relationship between soil resistance to penetration of the pile was originally limited to a series of straight lines. The revised program allows the use of any shape for this curve, as noted in Chapter VI.

2. The elastic soil deformation "Q" and the soil damping constant "J" were each limited to one value at the point of the pile and a second value for side resistance. These parameters have been generalized to include different values at each pile segment.

3. A new method by which internal damping in the pile can be accounted for is now included. This method is explained in Chapter V.

4. A second method is included to account for the coefficient of restitution of the capblock or cushionblock.

5. For correlation with experimental data, it is now possible to place forces directly on the head of the pile rather than having to calculate them from the hammercushion-anvil properties. This method was used extensively where the force vs time curve at the head of the pile was known; since then the hammer, cushion, and anvil properties did not influence the solution. 6. The linear force vs compression curve for various cushion materials used previously has been generalized as noted in Chapter IV.

7. The effect of gravity on the solution can now be accounted for.

8. A special "parameter study" sub-program was written and included in the general program. This feature was used to vary specific parameters or groups of parameters between specified limits in order to study their influence on the solution, and to see if trends could be found.

9. For possible later use, several pile-driving formulas were included in the computer program.

10. The soil resistance on the point segment now uses two springs, one for the side friction acting on the side of the pile and a second spring for point bearing.

Chapter III PILE DRIVING HAMMERS

Ram Idealization

Smith⁴² suggests that since the ram is usually short in length, in many cases it can accurately be represented by a single weight having infinite stiffness. The example illustrated in Figure 2.1 makes this assumption since K(1) represents the spring constant of only the cap block, the elasticity of the ram having been neglected. He also notes that where greater accuracy is desired, or when the ram is long and slender, it can also be divided into a series of weights and springs. However, no work has been done to determine how long the ram can be before its elasticity affects the accuracy of the solution. The most common hammers in the above class include drop, air, and steam hammers. Figures 3.1 and 3.2 show how the ram may be idealized.

In order to determine the significance of dividing the ram into a number of segments, several ram lengths ranging from 2 to 10 ft were assumed, driving a 100-ft



Figure 3.1. Idealization for a long ram striking directly on a cushion block.



Figure 3.2. Idealization for a long ram striking directly on a steel anvil.

 TABLE 3.1. EFFECT OF BREAKING THE RAM INTO SEGMENTS WHEN RAM STRIKES A CUSHION

Number of Ram Divisions	Length of Pile Segments (ft)	Maximum Compressive Force in Pile (kip)	Maximum Tensile Force in Pile (kip)	Maximum Point Displace- ment (in.)
$\begin{array}{r}1\\2\\10\end{array}$	$1.25 \\ 1.25 \\ 1.25$	$263.1 \\ 262.6 \\ 262.9$	219.0 218.8 218.5	$3.057 \\ 3.058 \\ 3.059$

pile with point resistance only. For this parameter study the total weight of the pile varied from 1,500 lb to 10,000 lb, while the ultimate soil resistance ranged from zero to 10,000 lb. The cushion was assumed to have a stiffness of 2,000 kip/in.

Table 3.1 lists the results found for a typical problem solved in this series, the problem consisting of a 10-ft ram traveling at 20 ft/sec, striking a cushion having a stiffness of 2,000 kip/in. The pile used was a 100-ft 12H53 steel pile, driven by a 5,000-lb ram with an initial velocity of 12.4 ft/sec. No pile cap was included in the solution, the cushion being placed directly between the hammer and the head of the pile. Since the ram was divided into very short lengths, the pile was also divided into short segments.

As shown in Table 3.1, the solution is not changed to any extent, regardless of whether the ram is divided into 1, 2, or 10 segments. The time interval Δt was held constant in each case.

In certain hammers such as a diesel hammer, the ram strikes directly on a steel anvil rather than on a cushion. This makes the choice of a spring rate between the ram and anvil difficult because the impact occurs between two steel elements. One possible solution is to place the spring constant of the entire ram between the weights representing the ram and anvil. Also, the ram can be broken into a series of weights and springs as is the pile.

To determine when the ram in this case should be divided, a parameter study was run in which the ram length varied between 6 and 10 ft and the anvil weight from 1,000 to 2,000 lb. In each case, the ram diameter was held constant and the ram was divided into equal segment lengths as noted in Table 3.2. These variables were picked because of their possible influence on the solution.

The pile used was again a 12H53 point bearing pile with a cushion of 2,000 kip/in. spring constant placed between the anvil and head of the pile. The soil parameters used were $RU_{point} = 500$ kip, Q = 0.1 in., and J = 0.15 sec/ft. These factors were held constant for all problems listed in Table 3.2.

The most obvious result shown by Table 3.2 is that when the steel ram impacts directly on a steel anvil, dividing a long ram (6, 8 and 10 ft) into segments has a significant effect on the solution.

Energy Output of Hammer

One of the most significant parameters involved in pile driving is the velocity of the ram immediately before impact. This velocity is often used to determine the maximum kinetic energy of the hammer and its energy output rating, and must be known or assumed before the wave equation or dynamic formulas can be applied.

Although the manufacturers of pile-driving equipment furnish maximum energy ratings for their hammers, these are usually downgraded by foundation ex-

TABLE 3.2. EFFECT OF BREAKING RAM INTO SEGMENTS WHEN RAM STRIKES A STEEL ANVIL

	Number of Ea Ram of Ram Rar Length Divisions Segm	Number		Length of Each —	Maximum Compressive Force on Pile			Maximum	
Anvil Weight (lb)		Ram Segment (ft)	At Head (kip)	At Center (kip)	At Tip (kip)	Displacement (in.)			
2000	10	$\begin{array}{c}1\\2\\5\\10\end{array}$	$\begin{array}{c}10\\5\\2\\1\end{array}$	$513 \\ 437 \\ 373 \\ 375$	513 438 373 375	884 774 674 678	$\begin{array}{c} 0.207 \\ 0.159 \\ 0.124 \\ 0.125 \end{array}$		
	8	1 4 8	8 2 1	478 359 360	478 359 360	833 648 651	0.183 0.117 0.118		
	6	$1\\3\\6$	6 2 1	430 344 342	430 344 342	763 621 616	0.155 0.110 0.109		
1000	10	$\begin{array}{c}1\\2\\5\\10\end{array}$	10 5 2 1	508 451 381 371	509 451 382 372	878 789 691 681	0.160 0.159 0.151 0.153		
	8	$\begin{array}{c}1\\4\\8\\10\end{array}$	8 2 1 0.8	487 443 369 337	488 444 370 338	846 785 675 665	$\begin{array}{c} 0.151 \\ 0.144 \\ 0.134 \\ 0.133 \end{array}$		
	6	1 3 6 10	6 2 1 0.6	457 361 316 320	457 362 316 320	798 666 562 611	0.137 0.128 0.109 0.113		

perts for various reasons. A number of conditions such as poor hammer condition, lack of lubrication, and wear seriously reduce the energy output of a hammer. In addition the energy of many hammers can be controlled by regulating the steam pressure or diesel fuel. To determine how much the rated energy of any given hammer should be reduced is not a simple task.

Chellis⁴³ discusses several reasons for this energy reduction and recommends a number of possible efficiency factors for the commonly used hammers, based on his observations and experience.

The Michigan Study of Pile Driving Hammers

In 1965 the Michigan State Highway Commission⁴⁴ completed an extensive research program designed to obtain a better understanding of the complex problem of pile driving. Though a number of specific objectives were given, one was of primary importance. As noted by Housel,⁴⁵ "Hammer energy actually delivered to the pile, as compared with the manufacturer's rated energy, was the focal point of a major portion of this investigation of pile-driving hammers." In other words, they hoped to determine the energy delivered to the pile and to compare these values with the manufacturer's ratings.

The energy transmitted to the pile was termed "ENTHRU" by the investigators⁴⁴ and was determined by the summation

ENTHRU = $\Sigma F \Delta S$

Where F, the average force on the top of the pile during a short interval of time, was measured by a specially designed load cell, and ΔS , the incremental movement of the head of the pile during this time interval, was found using displacement transducers and/or reduced from accelerometer data. It should be pointed out that ENTHRU is not the total energy output of the hammer blow, but only a measure of that portion of the energy delivered below the load-cell assembly.

Since so many variables influence the value of ENTHRU, and since some of these variables were changing during the pile driving operation (e.g., condition of the cushion, soil resistance, etc.), the investigators were not able to determine the total energy output of the hammer. As noted in the Michigan report:⁴⁶ "Hammer type and operation conditions; pile type, mass, rigidity, and length; and the type and condition of cap blocks were all factors that affected ENTHRU, but when, how, and how much could not be ascertained with any degree of certainty." However, the wave equation can account for each of these factors so that their effects can be determined.

The Michigan report also noted that ENTHRU was not actually a direct measurement of the hammer's efficiency or energy output since the forces and displacements were measured below the capblock, as shown in Figure 3.3. Thus, ENTHRU was defined as "the amount of work done on the load cell."

The maximum displacement of the head of the pile was also reported and was designated LIMSET. Oscillographic records of force vs time measured in the load cell were also reported. Since force was measured only at the load cell, the single maximum observed values for each case will be called FMAX.



Figure 3.3. Typical pile driving assembly (after reference 44).



Figure 3.4. Idealization of a Vulcan hammer.

PAGE SIX

Problem Information

In selecting which of the Michigan pile problems to solve by the wave equation, it was decided to run at least two problems for each hammer used at each of the three testing sites. As shown in Table 3.3, cases selected from the Belleville site include two pile lengths for each of four different hammers. Otherwise, the problems were selected at random and the hammer energies determined are not necessarily typical of the hammer's usual operating characteristics. Similarly, the Detroit and Muskegon site problems are summarized in Tables 3.4 and 3.5. Figures 3.4 and 3.5 illustrate how these problems were idealized for purposes of analysis.

Even though the Michigan study is one of the most completely documented and fully reported research projects published concerning pile driving, certain information was not reported which must be known in order to apply the wave equation. This omission was not the result of any failure in reporting the data, but was because this information was not required by the methods of analysis used in the Michigan project and would have been difficult to measure. Two examples are the lack of information concerning the stiffness of the cushion and the velocity of the ram at impact.

Preliminary Studies

Since cushion-block information was not given, and because the cushion stiffness varies greatly during driving, a broad parameter study was made using the first case mentioned in Table 3.3. In this study, the cushion stiffness was varied by a factor of 50, from 540 kip/in. up to 27,000 kip/in. Also studied was the effect of varying the total soil resistance, RUT, using resistances of 30, 90, and 150 kip and ram velocities of 8, 12, and 16 ft/sec.



Figure 3.5. Idealization of a diesel hammer.

						PILE INFORMATION		
Pile I.D.	Case*	Hammer**	Cushion	\$ 11	Type	Total Length (ft)	Embedded Length (ft)	
BLTP-6	10.0 57.9	V-1 V-1	Oak Oak		12H53 12H53	32.5 72.5	10.0 57.9	
BLTP-4	25.0	LB-312	Micarta		$\left(\begin{array}{c} 12 & \text{in.} \end{array}\right)$	40.7	15.0	
	66.4 -	LB-312	Micarta		$\left\{\begin{array}{c} \text{Pipe} \\ 0.25 \\ \text{in.} \\ \text{wall} \end{array}\right\}$	81.6	56.4	
BRP-4	20.0 50.0	M-DE30 M-DE30	Oak Oak		12H53 12H53	40.0 60.0	20.0 50.0	
BLTP-5	15.0	D-D12	German Oak		$\left\{\begin{array}{c} 12 \text{ in.} \\ \text{Pipe} \\ 0.179 \end{array}\right\}$	40.0	5.0	
	66.0	D-D12	German Oak		$\left\{\begin{array}{c} 0.179\\ \text{in.}\\ \text{wall} \end{array}\right\}$	80.0	50.0	

TABLE 3.3 SUMMARY OF BELLEVILLE CASES SOLVED BY WAVE EQUATION

*Case number indicates pile length below ground surface and not necessarily embeddment.

**Hammer designations are as follows:

V-1 Vulcan 1

V-50C _ Vulcan 50C

V-80C Vulcan 80C -

LB-312 = Link Belt 312 LB-520 =

Link Belt 520 McKiernen-Terry DE-30 M-DE30 =

McKiernen-Terry DE-40 Delmag D-12 M-DE40 -

D-D12 =

D-D22 = Delmag D-22

TABLE 3.4. SUMMARY OF DETROIT CASES SOLVED BY WAVE EQUATION

				P	ILE INFORMAT	ION
Pile I.D.	Case*	Hammer*	- Cushion	Type	Total Length (ft)	Embedded Length (ft)
DLTP-8	$\begin{array}{c} 41.5\\ 80.2 \end{array}$	V-1 V-1	Oak Oak	12H53 12H53	80.1 97.0	41.5 80.2
DTP-5	20.0	V-50C	Micarta	$ \left\{ \begin{matrix} 12 & \text{in.} \\ \text{Pipe} \\ 0.179 \end{matrix} \right\} $	40.0	20.0
	79.0	V-50C	Micarta	in. wall	84.0	79.0
DRP-3	40.0 60.0	LB-312 LB-312	Micarta Micarta	12H53 12H53	80.0 80.0	40.0 60.0
DTP-13	40.0	M-DE30	Oak	$ \left\{ \begin{array}{c} 12 \text{ in.} \\ \text{Pipe} \\ 0.179 \end{array} \right\} $	45.0	40.0
	80.7	M-DE30	Oak	in. wall	90.7	80.7
DTP-15	20.0 80.5	D-D12 D-D12	German Oak	12H53 12H53	46.1 86.1	20.0 80.5

*See Table 3.3 for notation.

The results of this study indicate the significance of the wave equation in helping to understand the many factors that affect pile-driving behavior. The solutions for ENTHRU, FMAX, and LIMSET resulting from a change in the cushion stiffness, soil resistance, and ram velocities are given in Tables 3.6, 3.7, and 3.8, respectively. Whereas before it could not be determined "when, how, or how much," the results of this study indicate that in general for these particular problems, 1) ENTHRU is nearly independent of the cushion block stiffness used, since the cushion stiffness was increased by a factor of 50 while influencing ENTHRU only slightly,

2) FMAX is almost completely independent of the driving resistance,

3) FMAX is almost linearly related to the hammer velocity, and

				PI	LE INFORMATI	ON
Pile I.D.	Case*	Hammer*	Cushion	Туре	Total Length (ft)	Embedded Length (ft)
MLTP-2	20.0	V-1	Oak	$\left\{ egin{array}{ccc} 12 & \mathrm{in.} \ \mathrm{Pipe} \ 0.250 \end{array} ight\}$	45.0	20.0
	53.0	V-1	Oak	in. wall	60.0	53.0
MLTP-9	72.0	V-80C	Micarta	$ \left\{ \begin{matrix} 12 & \text{in.} \\ \text{Pipe} \\ 0.250 \end{matrix} \right\} $	80.0	72.0
	127.0	V-80C	Micarta	l 0.250 in. wall	134.0	127.0
MTP-12	30.5	LB-520	Micarta	$\left\{ egin{array}{c} 12 & \mathrm{in.} \\ \mathrm{Pipe} \\ 0.250 \end{array} ight\}$	40.0	30.5
	70.8	LB-520	Micarta	$\left\{\begin{array}{c} 0.250\\ \text{in.}\\ \text{wall} \end{array}\right\}$	80.0	70.8
MTP-11	69.5	M-DE40	Oak and Plywood	$\left\{ egin{array}{c} 12 & \mathrm{in.} \ \mathrm{Pipe} \ 0.250 \end{array} ight\}$	80.0	69.5
	150.0	M-DE40	r iy wood	$\left\{\begin{array}{c} 0.230\\ \text{in.}\\ \text{wall} \end{array}\right\}$	165.0	150.0
MLTP-8	31.0	D-D22	German Oak	$ \left\{ \begin{matrix} 12 \text{ in.} \\ \text{Pipe} \\ 0.250 \end{matrix} \right\} $	40.0 185.0	31.0
	178.0	D-D22	German Oak	in. wall	185.0	178.0

PAGE EIGHT

TABLE 3.6.	EFFECT	OF CUSHION	STIFFNESS	ON
	ENTHRU	FOR BLTP-6;	10.0	

	ENTHI	RU (kip f	t)		
Ram Velocity (ft/sec)	RUT (kip)	Cushie 540	on Stif 1080	fness (2700	kip/in.) 27,000
8	30 90 150	$3.0 \\ 3.1 \\ 3.0$	$3.0 \\ 3.2 \\ 3.2 \\ 3.2$	$3.0 \\ 3.3 \\ 3.3$	$2.9 \\ 2.9 \\ 3.0$
12	30 90 150	6.6 7.0 6.9	6.4 7.1 7.2	$7.1 \\ 7.2 \\ 7.4$	$\begin{array}{r} 6.4 \\ 6.4 \\ 6.7 \end{array}$
16	30 90 150	$11.8 \\ 12.3 \\ 12.4$	$11.9 \\ 12.6 \\ 12.9$	$12.2 \\ 12.8 \\ 13.2$	$11.3 \\ 11.5 \\ 11.4$

TABLE 3.7.EFFECT OF CUSHION STIFFNESS ON
FMAX FOR BLTP-6; 10.0

FMAX (kip)								
Ram Velocity	RUT	Cushi	on Stiff	ness (1	kip/in.)			
(ft/sec)	(kip)	540	1080	2700	27,000			
8	30 90 150	$132 \\ 137 \\ 143$	$185 \\ 185 \\ 186$	$261 \\ 261 \\ 261 \\ 261$	779 779 779			
12	$\begin{array}{c} 30\\90\\150\end{array}$	198 205 215	$278 \\ 278 \\ 279 \\ 279$	391 391 391	1,169 1,169 1,169			
16	30 90 150	264 275 288	$371 \\ 371 \\ 371 \\ 371$	522 522 522	$1,558 \\ 1,558 \\ 1,558 \\ 1,558$			

TABLE 3.8.EFFECT OF CUSHION STIFFNESS ON
LIMSET FOR BLTP-6; 10.0

	LIM	SET (in.)			
Ram Velocity	RUT	Cushie	on Stif	fness (kip/in.)
(ft/sec)	(kip)	540	1080	2700	27,000
8 •	30 90 150	$1.09 \\ 0.44 \\ 0.32$	$1.08 \\ 0.44 \\ 0.33$	$1.08 \\ 0.45 \\ 0.33$	$1.13 \\ 0.45 \\ 0.33$
12	30 90 150	$2.21 \\ 0.80 \\ 0.55$	2.14 0.82 0.57	$2.19 \\ 0.84 \\ 0.58$	$2.25 \\ 0.84 \\ 0.58$
16	30 90 150	$3.62 \\ 1.30 \\ 0.85$	$3.59 \\ 1.31 \\ 0.87$	$3.63 \\ 1.32 \\ 0.88$	$3.68 \\ 1.34 \\ 0.90$

4) FMAX consistently increases as the cushion stiffness increases.

Thus for the first time, a number of trends may be established for various pile driving situations by using the wave equation.

In order to analyze other of the Michigan problems, certain data given in the Michigan report were used. This information is listed in Table 3.9.

Investigation of Steam Hammers Used in the Michigan Study

As noted in Figure 3.4, the numerical solution to the wave equation uses a series of concentrated weights and springs which closely represent the actual system involved. Time is also divided into small intervals in order to arrive at a solution.

As shown by Smith,¹ the wave equation can be used to determine (among other quantities) the displacement D(m,t) of any mass "m" at time "t", as well as the force F(m,t) of any mass "m" at time "t." Thus the equation for ENTHRU at any point in the system can be determined by simply letting the computer calculate the equation previously mentioned:

ENTHRU =
$$\sum F \Delta S$$

or using the wave equation terms:

ŧ

ENTHRU(m) =
$$\sum \left[\frac{F(m,t) + F(m,t-1)}{2.0} \right]$$

 $\begin{bmatrix} D(m+1,t) - D(m+1,t-1) \end{bmatrix}$

where ENTHRU(m) = the work done on any weight (m+1),

m =the mass number, and

= the time interval number.

For example, the Michigan report determined ENTHRU(2) for the idealized system shown in Figure 3.4, since they recorded forces F(2,t) in the load cell and displacements D(3,t) below the load cell. For the system in Figure 3.5, ENTHRU(3) was determined.

Although it may not have been possible, ENTHRU should actually have been measured directly under the driving hammer ENTHRU(1), since ENTHRU(3) is greatly influenced by several parameters, especially the type, condition, and coefficient of restitution of the cushion, and the weights of the extra driving cap and load cell.

As will be shown later, the coefficient of restitution alone can change ENTHRU(2) by 20%, simply by changing e from 0.2 to 0.6. Nor is this variation in e unlikely since cushion condition varied from new to "badly burnt" and "chips added."

The wave equation was therefore used to analyze the problems since what was needed was a method by which the available data (ENTHRU, LIMSET, FMAX, etc.) could be used to determine the actual hammer energy involved, and also to compensate for the influence of cushion stiffness, e, additional driving cap weights, driving resistance encountered, etc.

Method Used to Correlate Theoretical and Experimental Results

In order to get the best possible correlation between experimental and theoretical solutions, an iterative method was used. This approach was suggested by the preliminary studies mentioned earlier. To demonstrate the method, an example problem, BLTP-6;10.0, will be solved.

Driving Location	Pile I.D.	Case	Hammer* Type	Manufacturer's Maximum Rated Energy (ft lb)	ENTHRU (ft lb)	LIMSET (in.)	Permanent Set (in.)	Estimated Static Soil Resistance (kip)
Belleville	BLTP-6	10.0	V-1	15,000	6,380	0.75	0.48	48
		57.9	V-1	15,000	4,440	0.42	0.02	400
	BLTP-4	25.0	LB-312	18,000	8,010	0.94	0.36	140
		66.4	LB-312	18,000	11,200	0.92	0.02	690
	BRP-4	20.0	M-DE-30	22,400	4,980	0.57	0.37	100
		50.0	M-DE-30	22,400	4,470	0.41	0.12	320
	BLTP-5	15.0	D-D12	22,500	9,040	1.86	1.43	80
		60.0	D-D12	22,500	9,930	0.79	0.11	340
Detroit	DLTP-8	41.5	V-1	15,000	5,760	1.22	1.00	60
		80.2	V-1	15,000	4,540	0.54	0.50	360
	DTP-5	20.0	V-50C	15,100	8,290	2.55	2.00	22
	·	79.0	V-50C	15,100	11,420	0.82	0.09	235
	DRP-3	40.0	LB-312	18,000	7,060	1.36	1.25	60
		60.0	LB-312	18,000	6,620	1.41	0.77	76
	DTP-13	40.0	M-DE30	22,400	9,100	2.21	2.00	30
		80.7	M-DE30	22,400	9,480	1.12	0.07	265
	 DTP-15	20.0	D-D12	22,500	10,100	2.07	2.00	40
		80.5	D-D12	22,500	5,480	0.58	0.25	120
Muskegon	MLTP-2	20.0	V-1	15,000	7,210	1.42	1.00	80
		53.0	V-1	15,000	4,870	0.57	0.09	200
	MLTP-9	72.0	V-80C	24,450	14,660	1.06	0.56	160
		127.0	V-80C	24,450	13,110	1.03	0.23	470
		30.5	LB-520	30,000	14,860	1.48	1.00	40
		70.8	LB-520	30,000	13,140	1.02	0.77	156
	MTP-11	69.5	M-DE40	32,000	16,760	1.16	0.67	160
		150.0	M-DE40	32,000	17,900	1.41	0.05	500
	MLTP-8	31.0	D-D22	39,700	25,500	2.35	1.25	40
		178.0	D-D22	39,700	22,050	1.71	0.04	988

*See Table 3.3 for notation.

Since in nearly every case the condition of the cushion is unknown, the first assumption must be for the cushion rate K(1). For illustrative purposes, assume that K(1) = 180 kip/in. and that soil resistances of 30 and 90 kip were assumed.

The next step was to run the problem with various hammer energies. As shown in Figure 3.6, for each energy input (EINPUT) the wave equation predicts a corresponding theoretical value of ENTHRU. These solutions are then used to plot the curves of Figure 3.6. Also, since each solution predicts a value for LIMSET and initial ram velocity, it is possible to plot the curves of Figure 3.7.

Returning to Figure 3.6, the question becomes what kinetic energy must the falling ram have had in order to cause a value of ENTHRU = 6,380 kip ft (the measured experimental value reported by Michigan and listed

in Table 3.9)? By entering ENTHRU = 6,380 kip ft, and assuming RUT = 30 kip, project to the upper curve where EINPUT is found to be 11,000 kip ft.

To further check the solution, determine the ram velocity required for 11,000 kip ft of kinetic energy from:

$$V = \sqrt{\frac{(\text{EINPUT})}{\text{Ram Weight}}} = 11.9 \text{ ft/sec}$$

Next, from Table 3.9, find the actual value of LIMSET (determined experimentally) and enter this value of 0.75 in. and V = 11.9 ft/sec in Figure 3.7.

Should the projection of these points intersect on the RUT = 30 kip curve, then that assumption was correct. However, this indicates a soil resistance of around 90 kip so that the RUT = 90 kip curve of Figure 3.6 should probably have been used.



Figure 3.6. EINPUT vs ENTHRU.

Returning to Figure 3.6, the new value of EINPUT is found to be 10,100 ft lb, which gives a new ram velocity of 11.4 ft/sec. Substituting this velocity into Figure 3.7, the resulting value of RUT agrees closely with the assumed value of 90 kip.

Since the ram velocity at impact is now known, the assumed cushion stiffness of 1080 kip/in. can be checked. Holding RUT = 90 kip and the initial ram velocity = 11.4 ft/sec, and solving for the change in FMAX as the cushion stiffness varies, the curve of Figure 3.8 can be drawn. The experimental value of FMAX reported in the Michigan paper was 244 kip, which entered into Figure 3.8 gives a value of K (1) = 900 kip/in. Since this is close to the assumed value of 1080 kip/in., the solution was considered to be satisfactory. However, even in cases where the cushion stiffness was quite inaccurate, ENTHRU was only slightly changed when a more accurate value of K (1) was used.

This solution now enables us to determine the energy output of the hammer, and other quantities. Since this hammer is rated at 15,000 ft lb and its actual output was only 10,100 ft lb the hammer must have lost 3,900 ft lb due to friction in the guides or from other causes. Thus, the hammer efficiency is $(10,100) \times (100)/$ 15,000 = 67 percent. Furthermore, since only 6,380 ft lb (ENTHRU) of the 10,100 ft lb output reached the load cell, the difference must have been lost in the helmetcushion-load cell assembly. Thus the efficiency of this assembly must have been $(6,380) \times (100)/10,100 = 63$ percent.

The ability to determine these efficiencies separately is important since it indicates whether the driving hammer or cushion-helmet assembly should be studied to reduce energy losses during driving.

The preceding method was used to solve each of the Michigan steam hammer cases listed in Tables 3.3, 3.4, and 3.5.

Correlation of Experimental and Theoretical Results

It is interesting to compare the final wave equation solution with the experimental results reported in the Michigan pile study. For the above case, comparisons between the experimental results and those given by the wave equation are shown in Figures 3.9 through 3.11. These figures show the experimental and theoretical forces and accelerations, displacements, and energy, vs. time, measured at the load cell. The correlations are reasonably accurate, especially during the first 0.01 sec, although the reflected compressive wave seems to be overestimated, as shown in Figure 3.9A at 0.014 sec. This did not greatly affect either the ENTHRU or dis-





BELLEVILLE SITE CASE BLTP-6; 10.0 (N 20,000 Ram Velocity = 11.4 ft/sec = 90.0 klp (KIP , ≘ ¥ 15,000 STIFFNESS 10.000 NOIHSUC 5,000 K(I) = 900 kip /m 200 400 600 вòо FMAX (KIP)

Figure 3.8. Cushion stiffness vs FMAX.

placement curves, although it may have caused the rather large errors in the acceleration curve of Figure 3.9B.

A summary of the results for the steam hammer cases solved is given in Table 3.10. Listed are the energy output of the hammer, the hammer efficiencies, the ram velocity, and the total soil resistance, RUT, necessary to obtain correlation for each case.

It should be noted that there was no way to determine the soil damping or elasticity constants. Therefore, the constants recommended by Smith⁴⁷ were used. As shown by Forehand and Reese,⁴⁸ these constants affect the resulting RUT values. Therefore, the theoretical RUT values shown in Table 3.10 were not expected to agree closely with the experimental values reported in Table 3.9. However, it is interesting to note that in several cases the ratio of the soil resistance determined experimentally to that predicted by the wave equation is reasonably constant.

Investigation of Diesel Hammers

Used in the Michigan Study

Because the diesel explosive force is much smaller than the impact force, it was found to have little effect on the driving stresses.⁴¹ However, if explosive pressure is neglected, the ram velocity required to predict EN-THRU is much greater than that calculated from the free fall of the ram, even assuming 100 percent efficiency. Therefore, it was necessary to run the diesel hammer cases accounting for the explosive pressure in the hammer.

During impact between the ram and anyil the force on the anvil will reach some maximum value and then decrease. Following this impact, the diesel explosion occurs, exerting an explosive pressure and force between the ram and anvil. This behavior has been studied and reported by some of the hammer manufacturers.⁷¹ In order to simulate this action for wave-equation analysis, the explosive force acting within the diesel hammer is assumed to behave as shown in Figure 3.12. The maximum explosive force is held on the anvil for 0.01 sec after which the force is tapered to zero at 0.0125 sec. Actually, the explosive hammer force lasts considerably longer than this but its magnitude is too small to be a significant factor in pushing the pile down except during the initial driving stages when little or no soil resistance is encountered. The magnitudes of explosive pressures listed in Table 3.11 were obtained from the hammer manufacturer or were assumed.

In previous solutions, it was an easy matter to solve for the total energy of the ram at impact since only its kinetic energy, EINPUT, was involved. Now, since explosive pressure is included, the total energy developed includes both kinetic and explosive energy.

This total energy, ENTOTL, is the sum of the energy transmitted to the anvil, ENTHRU1, and the kinetic rebound energy of the ram after impact, where ENTHRU1 is calculated by the same method as was used for EN-

TABLE	3.10.	SUMMARY	\mathbf{OF}	RESULTS	FOR	MICHIGAN	STEAM	HAMMERS	

Driving Location	Pile I.D.	Case	Hammer* Type	EINPUT (ft lb)	ENTHRU† (ft lb)	Ham- mer** Effi- ciency (%)	Ram- Cushion- Helmet Assembly Efficiency (%)	Ram Velocity (ft/sec)	RUT (kip)	RUT (Theoretical) RUT (Experimental) (%)
Belleville	BLTP-6	$\begin{array}{c} 10.1\\ 57.9\end{array}$	V-1 V-1	$10,100 \\ 7,000$	6,380 4,440	$\begin{array}{c} 67 \\ 47 \end{array}$	63 63	$\begin{array}{c} 11.9\\9.5\end{array}$	90 200	190 50
Detroit	DLTP-8	$\begin{array}{c} 41.5\\ 80.2 \end{array}$	V-1 V-1	9,700 7,200	$5,760 \\ 4,540$	$\begin{array}{c} 65\\ 48\end{array}$	60 63	$\begin{array}{c} 11.2\\ 9.6\end{array}$	50 120	83 33
	DTP-5	20.0 79.0	V-50C V-50C	$12,800 \\ 15,600$	8,290 11,420	85 103	65 73	$12.9\\14.2$	$25 \\ 300 +$	$110 \\ 128 +$
Muskegan	MLTP-2	$\begin{array}{c} 20.0\\ 53.0\end{array}$	V-1 V-1	12,200 7,700	7,210 4,870	81 51	59 63	12.5 10.0	50 150	62 75
· _	MLTP-9	$\begin{array}{c} 72.0\\ 127.0 \end{array}$	V-80C V-80C	19,700 19,200	14,660 13,110	81 79	74 68	$\begin{array}{c} 12.6\\ 12.5\end{array}$	$\begin{array}{c} 175\\ 300 \end{array}$	109 64

*See Table 3.3 for notation.

**Hammer efficiency computed on basis of the manufacturer's maximum rated output.

†Note: The problems were selected at random and the hammer energies determined are not necessarily typical of the hammer's usual operating characteristics.



Figure 3.9. Comparison of theoretical and experimental load cell forces and accelerations.

THRU at the load cell, and the kinetic rebound energy remaining in the ram after impact is given by $WV^2/64.4$, where W is the weight of the ram and V is the rebound velocity of the ram determined by the wave equation.

The efficiencies and initial ram velocities noted in Table 3.11 were found by plotting ENTHRU and EN-THRU1 vs the initial ram velocity as shown in Figure 3.13. Plotting the values of LIMSET vs ram velocity as in Figure 3.14 then gives the total soil resistance predicted by the wave equation. This procedure was used on all diesel hammer cases, and the results are summarized in Table 3.11.



Figure 3.10. Comparison of theoretical and experimental load cell displacements.



Figure 3.11. Comparison of theoretical and experimental values of ENTHRU.

PAGE THIRTEEN

Driving · Location	Pile I.D.	Case		Explosive Force on Anvil (kip)		ENTHRU** (ft lb)	$\mathbf{E}\mathbf{f}$ -	Ram- Cushion Assembly Ef- ficiency (%)	Ram Velocity at Impact (ft/sec)	RUT (kip)	RUT (Theoretical) RUT (Experimental) (%)
Belleville	BLTP-4	$\begin{array}{c} 25.0\\ 66.4\end{array}$	LB-312	98.0	10,630 16,030	8,010 11,200	59 89	75 70	8.2 6.4	$70 \\ 250$	50 36
	BRP-4	$\begin{array}{c} 20.0\\ 50.0\end{array}$	M-DE30	98.0	9,450 9,100	4,980 4,470	42 41	$53 \\ 49$	9.8 10.6	$\frac{100}{200}$	100 63
	BLTP-5	$\begin{array}{c} 15.0\\ 60.0\end{array}$	D-D12	93.7	$13,000 \\ 14,730$	9,040 9,930	58 66	69 67	$\begin{array}{c} 12.8\\ 15.0\end{array}$	$\begin{array}{c} 40\\ 400 \end{array}$	50 118
Detroit	DRP-3	$\begin{array}{c} 40.0\\ 60.0\end{array}$	LB-312	98.0	9,270 13,900	7,060 6,620	52 77	76 48	9.8 5.2	$\begin{array}{c} 45\\60\end{array}$	75 79
	DTP-13	40.0 80.7	M-DE30	98.0	$14,390 \\ 15,280$	9,100 9,480	64 68	63 62	13.7 15.1	$\begin{array}{r} 35\\120\end{array}$	$117 \\ 45$
_	DTP-15	$\begin{array}{c} 20.0\\ 80.5 \end{array}$	D-D12	93.7	15,270 9,430	10,100 5,480	$\begin{array}{c} 68\\ 42 \end{array}$	66 58	15.2 11.6	$\begin{array}{r} 45\\110\end{array}$	112 92
Muskegon	MTP-12	30.5 70.8	LB-520	98.0	22,140 21,260	$14,860 \\ 13,140$	74 71	67 62	$16.4\\14.4$	75 70	$187 \\ 45$
	MTP-11	69.5 150.0	M-DE40	138.0	32,800 36,850	16,760 17,900	$\begin{array}{c} 102\\115\end{array}$	50 49	$\begin{array}{c} 20.6\\ 21.5\end{array}$	$\begin{array}{c} 150\\ 250 \end{array}$	94 50
_	MLP-8	$\begin{array}{c} 31.0\\178.0\end{array}$	D-D22	158.7	31,600 27,300	25,500 22,050	80 69	81 81	17.8 17.1	70 300	$\begin{array}{c} 175\\ 30 \end{array}$

TABLE 3.11. SUMMARY OF RESULTS FOR MICHIGAN DIESEL HAMMERS

*Hammer efficiency based on manufacturer's maximum rated energy.

**Note: The problems were selected at random and the hammer energies determined are not necessarily typical of the hammer's usual operating characteristics.

Determination of Hammer Energy Output Diesel Hammers

At present the manufactures of diesel hammers arrive at the energy delivered per blow by two different methods. One manufacturer feels that "Since the amount of (diesel) fuel injected per blow is constant, the compression pressure is constant, and the temperature constant, the energy delivered to the piling is also constant."⁶⁹ The energy output per blow is thus computed

as the kinetic energy of the falling ram plus the explosive energy found by thermodynamics. Other manufacturers simply give the energy output per blow as the product of the weight of the ram-piston W_R and the length of the stroke h, or the equivalent stroke in the case of closed-end diesel hammers.

The energy ratings given by these two methods dif-fer considerably since the ram stroke h varies greatly thereby causing much controversy as to which, if either,



3 ENTOTL X 100 13,000 X 100 HAMMER EFFICIENCY 59% 30 22,000 ERATED ENERGY (KIP FT) CUSHION EFFICIENCY = _____ 9040 X 100 = 69% ENTOTL 13,000 25 20 15 EN ENTHRU I = 11.000 FT 10 ENTHRU = 9040 BELLEVILLE SITE CASE BLTP-5;15.0

Figure 3.12. Typical force vs time curve for a diesel

PAGE FOURTEEN

hammer.



RAM VELOCITY AT IMPACT (FT/SEC)

12

RAM VELOCITY AT IMPACT = 12.8 FT/SEC

20

16

5

o



Figure 3.14. LIMSET vs ram velocity determined by wave equation analysis.

method is correct and what energy output should be used in dynamic pile analysis.

In conventional single acting steam hammers the steam pressure or energy is used to raise the ram for each blow. The magnitude of the steam force is too small to force the pile downward and consequently it works only on the ram to restore its potential energy, $W_R x h$, for the next blow. In a diesel hammer on the otherhand, the diesel explosive pressure used to raise the ram is, for a short time at least, relatively large.

While this explosive force works on the ram to restore its potential energy $W_R \times h$, the initially large explosive pressure also does some useful work on the pile given by:

$$E_e = \int F \, ds$$
 Eq. 3.1

where F = the explosive force, and

ds = the infinitesimal distance through which the force acts.

Since the total energy output is the sum of the kinetic energy at impact plus the work done by the explosive force.

$$E_{total} = E_k + E_e \qquad Eq. \ 3.2$$

where E_{total} = the total energy output per blow,

- E_k = the kinetic energy of the ram at the instant of impact,
- and $E_e =$ the diesel explosive energy which does useful work on the pile.

It has been noted that after the ram passes the exhaust ports, the energy required to compress the airfuel mixture is nearly identical to that gained by the remaining fall of the ram.⁷⁰ Therefore the velocity of the ram at the exhaust ports is essentially the same as at impact, and the kinetic energy at impact can be closely approximated by:

$$E_{k} = W_{R} (h - d)$$
 Eq. 3.3

where W_R = the ram weight,

- h = the total observed stroke of the ram,
- and d = the distance the ram moves after closing the exhaust ports and impacts with the anvil.

The total amount of explosive energy $E_{e(total)}$ is dependent upon the amount of diesel fuel injected, compression pressure and temperature and therefore may vary somewhat.

Unfortunately, the wave equation must be used in each case to determine the exact magnitude of E_e since it not only depends on the hammer characteristics but also on the characteristics of the anvil, helmet, cushion, pile, and soil resistance. However, values of E_e determined by the wave equation for several typical pile problems indicates that it is usually small in portion to the total explosive energy output per blow, and furthermore, that it is on the same order of magnitude as $W_R \times d$.

Thus, Eq. 3.1 can be simplified by assuming:

$$E_e = W_R \times d$$
 Eq. 3.4

Substituting Eqs. 3.3 and 3.4 into Eq. 3.1 gives:

 $E_{total} = E_k + E_e = W_R (h - d) + W_R d$ Eq. 3.5

so that:

$$E_{total} = W_R h$$
 Eq. 3.6

The results given by this equation are compared with the actual values found by the wave equation in Table 3.12. Note that the results are relatively constant, the average efficiency being 100%.

Steam Hammers

Again using the wave equation in conjunction with the Michigan report, Tables 3.13 and 3.14 suggest efficiency ratings of 60% for the single-acting steam hammers, and 87% for the double-acting hammer, based on an energy output given by:

$$E_{total} = W_R h$$
 Eq. 3.7

In order to determine an equivalent ram stroke for the double-acting hammers, the internal steam pressure above the ram which is forcing it down must be taken into consideration. The manufacturers of such hammers state that the maximum steam pressure or force should not exceed the weight of the housing or casing, or the housing may be lifted off the pile. Thus the maximum downward force on the ram is limited to the total weight of the ram and housing.

Since these forces both act on the ram as it falls through the actual ram stroke h, they add kinetic energy to the ram, which is given by:

$$E_{total} = W_R h + F_R h \qquad Eq. 3.8$$

where W_R = the ram weight,

 F_R = a steam force not exceeding the weight and h = the observed or actual ram stroke.

Since the actual steam pressure is not always applied at

PAGE FIFTEEN

TABLE 3.12.	COMPARISON	OF	ENERGY	OUTPUT	MEASURED	EXPERIMENTALLY	WITH THAT	PREDICTED
			BY EQUA	TION 3.6,	FOR DIESE	L HAMMERS		

Hammer.	Pile I.D.	Case	ENTOTL (ft lb)	$\begin{array}{c} \text{Ram Wt.} \\ W_{R} \\ (\text{lb}) \end{array}$	Observed Ram Stroke h (ft)	$\begin{array}{c} W_{R} \times h \\ E_{total} \\ (ft \ lb) \end{array}$	ENTOTL Etotal
LB-312	BLTP-4	$\begin{array}{c} 25.0\\ 66.4\end{array}$	10,630 16,030	3,857 3,857	3.3* 3.6*	12,800 13,900	.83 1.15
	DRP-3	40.0 60.0	9,270 13,900	3,857 3,857	2.9* 3.0*	11,000 11,600	.84 1.20
DE-30	BRP-4	20.0 50.0	9,450** 9,100**	2,800 2,800	6.6 6.9	18,500 19,300	
	DTP-13	40.0 80.7	14,390 15,280	2,800 2,800	5.2 7.0	14,600 19,600	.99 .78
D-12	BLTP-5	$\begin{array}{c} 15.0\\ 60.0\end{array}$	13,000 14,730	2,750 2,750	4.9 6.1	13,500 16,800	.96 .88
	DTP-15	20.0 80.5	15,270 9,430**	2,750 2,750	6.0 7.0	16,500 19,300	.93
LB-520	MTP-12	30.5 70.8	22,140 21,260	5,070 5,070	3.7* 4.5*	18,500 22,750	1.20 .93
DE-40	MTP-11	69.5 150.0	32,800 36,850	4,000 4,000	7.6 8.2	30,400 32,800	1.08 . 1.12
D-22	MLTP-8	31.0 178.0	31,600 27,300	4,850 4,850	5.6 5.5	27,200 26,700	$1.16\\1.02$
							Avg. $=$ 1.00

*Equivalent stroke derived from bounce chamber pressures.

**Experimental results for these cases appear to be quite inaccurate.

TABLE 3.13.	COMPARISON	OF MEA					BY	EQUATION	3.7,	FOR	SINGLE
			ACT	ING STEA	M HAI	MMERS		-	-		

Pile I.D.	Case	Hammer Type	EINPUT* (ft lb)	W _R (lb)	h** (ft)	Etotal (ft lb)	EINPUT Etotal
BLTP-6	$\begin{array}{c} 10.0\\ 57.9 \end{array}$	V-1 V-1	10,100 7,000	5,000 .5,000	3	15,000 15,000	0.67 0.47
DLTP-8	$\begin{array}{r} 41.5\\ 80.2 \end{array}$	V-1 V-1	9,700 7,200	5,000 5,000	3 3	15,000 15,000	0.65 0.48
MLTP-2	$\begin{array}{c} 20.0\\ 53.0 \end{array}$	V-1 V-1	12,200 7,700	5,000 5,000	3 3	15,000 15,000	0.81 0.51
							Avg. = 0.60

*EINPUT found by wave equation and listed in Table 3.10. **The observed ram stroke h or equivalent ram stroke h. was given in the Michigan report text.

TABLE 3.14.	COMPARISON OF	' MEASURED ENI	ERGY OUTPUT	WITH THAT	PREDICTED	BY EQUATION 3.11,
		FOR DOUBLE .	ACTING STEAM	I HAMMERS		

Pile	Case	Hammer	EINPUT*	W _R	h _e **	E _{total}	EINPUT
I.D.		Type	(ft lb)	(lb)	(ft)	(ft lb)	Etotal
DTP-5	20.0 79.0	V-50C V-50C	12,800 15,600	5,000 5,000	3.02 3.02	15,100 15,100	$\begin{array}{c} 0.85\\ 1.03\end{array}$
ML/TP-9	72.0	V-80C	19,700	8,000	3.05	24,450	0.81
	127.0	V-80C	19,200	8,000	3.05	24,450	0.79
							Avg. = 0.87

*EINPUT found by wave equation and listed in Table 3.10.

**The observed ram stroke h or equivalent ram stroke h, was given in the Michigan report text.

PAGE SIXTEEN

the rated maximum, the actual steam force can be expressed as:

$$F_R = \left(\frac{p}{p_{rated}} \right) W_H$$
 Eq. 3.9

where $W_{\rm H}$ is the housing weight, p is the operating pressure, and $P_{\rm rated}$ is the maximum rated steam pressure.

The total energy output is then given by

$$E_{total} = W_R h + \left[\frac{p}{p_{rated}} W_H \right] h$$
 Eq. 3.10

This can be reduced in terms of Eq. 3.7 by using an equivalent stroke he which will give the same energy output as Eq. 3.10.

$$E_{total} = W_R h_e$$
 Eq. 3.11

Setting Eqs. 3.10 and 3.11 equal yields

$$W_{R} h_{e} = W_{R} h + \left[\frac{p}{p_{rated}} W_{H} \right] h$$
$$= h \left[W_{R} + \frac{p}{p_{rated}} W_{H} \right]$$

or solving for the equivalent stroke:

$$h_e = h \left[1 + \frac{p}{p_{rated}} \times \frac{W_H}{W_R} \right]$$
 Eq. 3.12

Conclusions

The preceding discussion has shown that it is possible to determine reasonable values of hammer energy output simply by taking the product of the ram weight and its observed or equivalent stroke, and applying an efficiency factor listed in Tables 3.12 thru 3.14. This method of energy rating can be applied to all types of impact pile drivers with reasonable accuracy.

A brief summary of this simple procedure for arriving at hammer energies and initial ram velocities is as follows:

Open End Diesel Hammers

$$E = W_R h (e)$$

$$V_R = \sqrt{2g (h-d) (e) }$$

where $W_R = ram$ weight

- V_R = initial ram velocity
- h = observed total stroke of ram
- d = Distance from anvil to exhaust ports
- e = efficiency of open end diesel hammers, approximately 100% when energy is computed by this method.

Closed End Diesel Hammers

$$E^{*} = W_{R} h_{e} (e)$$

 $V_{R} = \sqrt{2g (h_{e}-d) (e)}$

*Note: For the Link Belt Hammers, this energy can be read directly from the manufacturer's chart using bounce chamber pressure gage.

where $W_R = ram$ weight

- $V_R = initial ram velocity$
 - = equivalent stroke derived from bounce h chamber pressure gage
 - d = distance from anvil to exhaust ports
 - = efficiency of closed end diesel hammers. е approximately 100% when energy is computed by this method.

Double-Acting Steam Hammers

$$\begin{array}{rcl} \mathrm{E} & = \mathrm{W}_{\mathrm{R}} \ \mathrm{h}_{\mathrm{e}} \ (\mathrm{e}) \\ \mathrm{V} & = & \sqrt{2 \mathrm{g}} \ \mathrm{h}_{\mathrm{e}} \ (\mathrm{e}) \\ \mathrm{here} \ \mathrm{W}_{\mathrm{R}} & = & \mathrm{ram} \ \mathrm{weight} \end{array}$$

here
$$W_{R} = ram$$
 weig

= equivalent ram stroke

$$= h \left[1 + \frac{p}{p_{rated}} \times \frac{W_{H}}{W_{R}} \right]$$

- h = actual or physical ram stroke
- = operating steam pressure р
- $p_{rated} = maximum$ steam pressure recommended by manufacturer
 - $W_{\rm H}$ = weight of hammer housing
 - = efficiency of double-acting steam hammers, approximately 85% by this method.

Single-Acting Steam Hammers

$$E = W_R h (e)$$

$$V_R = \sqrt{2g h (e)}$$
where $W_R = ram$ weight

- = ram stroke h
- = efficiency of single-acting steam hammers, e normally recommended around 75% to 85%.⁴³ In this study of the Michigan data, a figure of 60% was found. The writers feel the 60% figure is unusually low and would not recommend it as a typical value.

A summary of the properties and operating characteristics of the various hammers is given in Table 3.15.

Effects of the Experimental **Measuring Devices**

Another example of the application of the wave equation to the Michigan pile study is the solution of each of the previous problems, but excluding any effects of the experimental apparatus. When the question was first raised as to how the elasticity of the load cell and the additional weight of the load cell and extra driving cap might affect the results, it was decided to drive a Belleville H pile to refusal with a Delmag D-12 hammer with the load cell and extra driving cap removed. The data recorded for this pile were then compared with the data for similar piles which were driven by the same hammer but which included the extra driving cap and load cell.

The only data obtainable for the noninstrumented pile were the blow count and rate of penetration at various depths, since there was no way to measure the forces, displacements, ENTHRU, etc. It is also possible that a pipe pile might have been affected differently than the

TABLE 3.15. SUMMARY OF HAMMER PROPERTIES AND OPERATING CHARACTERISTICS

Hammer Manu- facturer	Hammer Type	Maximum Rated (ft lb)	Ram Weight (lb)	Casing Weight (lb)	Anvil Weight (lb)	Maximum or Equiva- lent Stroke (ft)	d (ft)	Rated Steam Pressure (psi)	Explosive Pressure (lb)	Cap Block
Vulcan	#1 014 50C 80C 140C	$15,000 \\ 42,000 \\ 15,100 \\ 24,450 \\ 36,000$	5,000 14,000 5,000 8,000 14,000	4,700 13,500 6,800 9,885 13,984		3.00 3.00 3.02 3.06 2.58		120 120 140		
Link Belt	312	18,000	3,857		1188	4.66	0.50		98,000	5 Micarta disks 1″ x 10%″ dia.
	520	30,000	5,070		1179	5.93	0.83		98,000	
MKT Corp	DE20	16,000	2,000		640	8.00	0.92		46,300	nylon disk 2″x 9″ dia.
	DE30	22,400	2,800		77.5	8.00	1.04		98,000	nylon disk 2″ x 19″ dia.
	DE40	32,000	4,000		1350	8.00	1.17		138,000	dia. nylon disk 2" x 24" dia.
Delmag	D-12	22,500	2,750		754	8.19	1.25		93,700	15" x 15" x 5" German
	D-22	39,700	4,850		1147	8.19	1.48		158,700	Oak 15″ x 15″ x 5″ German Oak

H-pile tested, and that the soil conditions of the Detroit or Muskegon sites could be of influence. Furthermore, only one hammer was studied (the Delmag D-12) and the effect on the other hammers could be different. Obviously, these questions cannot be completely answered experimentally since this would mean that every time the hammer, pile type, driving location, or any other parameter changed, a similar noninstrumented pile would also have to be driven under identical conditions.







Figure 3.15. Idealization of a Vulcan hammer without measuring devices.

PAGE EIGHTEEN

Figure 3.16. Idealization of a diesel hammer without measuring devices.

TABLE 3.16. EFFECT OF REMOVING LOAD CELL ON ENTHRU, LIMSET, AND PERMANENT SET OF PILE

		ENTHRU (kip ft)			ISET n.)	PERMANENT SET (in.)	
Case	Ram Velocity (ft/sec)	With Load Cell	Without Load Cell	With Load Cell	Without Load Cell	With Load Cell	Without Load Cell
DTP-15,	8	1.5	1.6	0.27	0.34	0.23	0.25
	12	3.3	3.6	0.53	0.67	0.57	0.57
80.5	16	5.8	6.5	1.02	1.03	0.94	0.97
	20	9.1	10.1	1.54	1.54	1.43	1.47
<u> </u>	8	3.1	3.8	0.62	0.71	0.51	0.62
DLTP-8,	12	7.1	8.5	1.15	1.32	1.06	1.29
80.2	16	12.5	15.1	1.91	2.10	1.82	2.15
	20	19.5	23.6	2.70	3.08	2.65	3.13

Although no problems were solved which involved H piles driven by a Delmag D-12 hammer at the Belleville site, a similar pile was driven at Detroit for which a wave equation solution was obtained.

The results for this problem with the load cell assembly included and excluded are given in Table 3.16. This agrees with the Michigan study conclusion that for case DLTP-15;80.5 the permanent set per blow including the load cell agrees with that found when the load cell is excluded. The corresponding values for ENTHRU do not agree nearly so well.

The results for a similar problem solved at the Detroit site, DLTP-8;80.2, do not agree with this conclusion. This pile was also an H-pile, was embedded to within 0.3 ft of the first H-pile, and also had 55 kip soil resistance. However, DLTP-8;80.2 differs from the Michigan test pile in that this pile was 11 ft longer, and was driven by a Vulcan-1 hammer rather than the Delmag D-12. As shown in the lower half of Table 3.16, ENTHRU, LIMSET, and the permanent set per blow all show large changes when the measuring devices are omitted. This might be overlooked if only the experimental results for case DLTP-15;80.5 were known.

Table 3.17 shows how ENTHRU increases when the load cell assembly is removed.

Effects of Cushion Properties on Driving

Although the general effects of cushioning materials on pile driving are discussed in Chapter IV, the following discussion is given since it deals with the Michigan pile study.

As previously noted, the Michigan report states that the cushion properties influence the values of ENTHRU significantly, although "how, when, or how much" ENTHRU was affected could not be determined. It was thought that ENTHRU could be increased by using a more resistant cushion block, in the case of the Vulcan 1 and McKiernan-Terry DE-30 hammers. Although this conclusion seems reasonable, results given by the wave equation did not seem to agree. For example, as seen in Table 3.6, ENTHRU does not always increase with increasing cushion stiffness, and furthermore, the maximum increase in ENTHRU noted here is relatively small —only about 10 percent. This effect can also be seen in Table 3.18, in which the cushion stiffness varies greatly, while the displacement of the pile point changes less than 10 percent.

However, if a different cushion is used, the coefficient of restitution will probably change too. Since the coefficient of restitution of the cushion may affect EN-THRU, a number of cases were solved with "e" ranging from 0.2 to 0.6. As shown in Tables 3.19 and 3.20, an increase in "e" from 0.2 to 0.6 normally increases ENTHRU from 18 to 20 percent, while increasing the permanent set from 6 to 11 percent. Thus, for the case shown, the coefficient of restitution of the cushion has a greater influence on rate of penetration and ENTHRU than does its stiffness. This same effect was noted in the other solutions, and the cases shown in Tables 3.19 and 3.20 are typical of the results found in other cases.

As was noted in Table 3.7, any increase in cushion stiffness also increases the driving stress. Thus, according to the wave equation, increasing the cushion stiffness to increase the rate of penetration (for example by not replacing the cushion until it has been beaten to a fraction of its original height or by omitting the cushion entirely) is both inefficient and poor practice because of the high stresses induced in the pile. It would be better to use a cushion having a high coefficient of restitution and a low cushion stiffness in order to increase ENTHRU and to limit the driving stress.

This suggests that a long micarta cushion having a relatively low spring rate, and a high coefficient of restitution might be very effective.

Comparison of Various Hammers Driving the Same Pile

One of the objectives of the Michigan pile study was to determine just how effective the various hammers actually were during driving. Therefore, every attempt was made to equalize any variables which would affect the results, such as choosing the driving location to give comparable driving conditions. However, it would be impossible to test several hammers without having some variations occur, perhaps in the soil resistance or hammer condition. Since the wave equation does not have this limitation, it can be used to advantage here.

			ENT (ft	HRU lb)	Increase
Driving Location	Pile I.D.	Case	With Load Cell	Without Load Cell	ENTHRU in (%)
Belleville	BLTP-6	10.0 57.9	6380 4440	7500 5300	18 19
	BLTP-4	25.0 66.4	8010 11200	8800 12000	10 8
	BRP-4	20.0 50.0	4980 4470	5750 6450	15 44
	BLTP-5	15.0 60.0	9040 9930	$\begin{array}{c} 10750\\ 12300 \end{array}$	19 24
Detroit	DLTP-8	41.5 80.2	$5760\\4540$	6900 5400	21 19
	DTP-5	20.0 79.0	8290 11420	10000 12700	23 12
	DRP-3	40.0 60.0	7060 6620	7600 7200	13 11
	DTP-13	40.0 80.7	9100 9480	10850 11400	$\begin{array}{c}13\\20\end{array}$
	DTP-15	20.0 80.5	10100 5480	$\begin{array}{c} 11500\\ 6600 \end{array}$	$\frac{14}{20}$
Muskegon	MLTP-2	20.0 53.0	7210 4870	8800 5700	$\begin{array}{c} 23\\17\end{array}$
	MLTP-9	72.0 127.0	14660 13110	17000 16000	
	MTP-12	30.5 70.8	14860 13140	17000 15000	14 14
	MTP-11	69.5 150.0	16760 17900	22000 25300	31 41
	ML/TP-8	31.0 178.0	25500 22050	31000 26600	22 21

TABLE 3.17. EFFECT ON ENTHRU RESULTING FROM REMOVING THE LOAD CELL ASSEMBLY

TABLE 3.18. EFFECT OF CUSHION STIFFNESS ON MAXIMUM POINT DISPLACEMENT FOR CASES BLTP-6; 10.0 AND 57.9

			_	Ma	ximum Point	Displacemen	t (in.)	
Pile		RUT	Ram Velocity		Cushion Stif	fness (kip/i	n.)	Maximum Change
Ĩ.D.		(kip)	(ft/sec)	540	1080	2700	27,000	(%)
BLTP-6;	10.0	30	12 16 20	2.20 3.54 4.66	$2.14 \\ 3.47 \\ 4.93$	$2.22 \\ 3.52 \\ 5.00$	$2.26 \\ 3.70 \\ 5.01$	5 6 7
BLTP-6;	57.9	150	$\begin{array}{c} 12\\16\\20\end{array}$	0.45 0.72 1.06	0.48 0.76 1.10	0.38 0.76 1.11	$0.48 \\ 0.79 \\ 1.15$	6 9 8

TABLE 3.19. EFFECT OF COEFFICIENT OF RESTITUTION ON ENTHRU FOR CASE BLTP-6; 10.0 AND 57.9

Pile	RUT	Ram Velocity	ENTHRU (kip ft)			Maximum Change
I.D.	(kip)	(ft/sec)	e = 0.2	e = 0.4	e = 0.6	(%)
BLTP-6; 10.0	30	$\begin{array}{c} 12\\ 16\\ 20 \end{array}$	$6.0 \\ 10.5 \\ 16.5$	6.5 11.8 17.4	$7.3 \\ 12.8 \\ 20.0$	18 18 17
BLTP-6; 57.9	150	12 16 20	6.7 11.6 18.2	7.2 12.7 19.7	8.2 14.5 22.4	18 20 19

PAGE TWENTY

TABLE 3.20. EFFECT OF COEFFICIENT OF RESTITUTION ON MAXIMUM POINT DISPLACEMENT FOR CASEBLTP-6; 10.0 AND 57.9

Pile I.D.		RUT	Ram Velocity (ft/sec)	Maximun	Maximum Change		
		(kip)		$\overline{e} = 0.2$	e = 0.4	e = 0.6	(%)
BLTP-6;	10.0	30	12 16 20	2.13 3.38 4.73	2.14 3.47 4.93	$2.36 \\ 3.58 \\ 5.17$	$\begin{array}{c}10\\6\\8\end{array}$
BLTP-6;	57.9	150	12 16 20	0.46 0.73 1.05	$0.48 \\ 0.76 \\ 1.10$	0.50 0.81 1.18	8 10 11

TABLE 3.21. STUDY OF VARIOUS HAMMERS DRIVING THE SAME PILE

Hammer	Ram Velocity (ft/sec)	Explosive Force (kip)	Maximum Point Displacement (in.)	Permanent Set of Pile Per Blow (in.)	Blows Per Inch
Vulcan-1	10.0	0	0.125	0.025	8
Vulcan-50C	14.5	0	0.284	0.184	3
Vulcan-80C	12.5	0	0.360	0.260	2
Link Belt 312	7.0	98.0	0.119	0.019	8
Link Belt 520	16.0	98.0	0.357	0.257	3
McKiernen-Terry DE-30	13.0	98.0	0.139	0.039	7
McKiernen-Terry DE-40	21.0	138.0	0.592	0.492	1
Delmag D-12	15.0	93.7	0.173	0.073	5
Delmag D-22	17.5	158.7	0.473	0.373	2

As an example of such a comparison, Case BLTP-6;57.9 is used, with the load cell and extra helmet omitted, and with a soil resistance of 300 kips. This pile was then analyzed by the wave equation to determine its penetration per blow when driven by each of the hammers listed in Table 3.10. In each case, the soil and pile parameters were held constant. Thus, for example, even though the values of the soil damping constant or quake may not be exact, they remained constant for each problem while experimental results would vary unless Q and J did not change at each new driving location.

Again, certain quantities had to be known for each hammer before the wave equation could be applied. For example, the ram velocity at impact must be known, as well as the dynamic behavior of the cushion, the diesel explosive pressure in the hammer, and the length of time it exerts a force on the pile. Since the above data were not directly measured in the Michigan research program, they were being calculated from the previous data reported. The ram velocities at impact and explosive forces on the pile for the diesel hammers were based on the results given in Table 3.11, assuming the explosive force to be acting as shown in Figure 3.12. The Vulcan hammer properties were based on Table 3.10.

The results of driving this pile with the eight different hammers are listed in Table 3.21 in the form of permanent set of the pile per blow and blows per inch.

Chapter IV

CHARACTERISTIC CUSHION PROPERTIES

Introduction

Although a pile cushion serves several purposes, its primary function is to limit impact stresses in both the pile and hammer.⁵⁰ In general, it has been found that a wood or rope cushion is more effective in reducing the driving stresses than one of a relatively stiff material such as Micarta. However, a stiffer cushion is usually more durable and transmits a greater percentage of the hammer's energy to the pile.

For example, the results given in Tables 3.10 and 3.11 give an overall average efficiency of 52 percent for

cushion assemblies using wood, while the Micarta assemblies have an average efficiency of 66 percent. As shown in Table 3.7, an increase in cushion stiffness will also cause an increase in impact stresses which might damage the pile or hammer during driving. This increase in stress is particularly important when driving concrete or prestressed concrete piles.

Dynamic Stress-Strain Curves

In order to apply the wave equation to pile driving, Smith⁵¹ assumes that the cushion's stress-strain curve is



Figure 4.1. Stress-strain curve for a cushion block (after reference 51).



Figure 4.2. Test pile showing placement of strain gages.



Figure 4.3. Cushion test stand.

a series of straight lines as shown in Figure 4.1. Even though this curve might be sufficiently accurate to predict maximum compressive stresses in the pile, the shape of the stress wave often disagrees with that of the actual stress wave.⁵² This discrepancy was at first thought to be the result of inaccurate soil data, since very little was known concerning the soil behavior during driving. It was therefore decided to suspend several test piles horizontally above the ground⁵³ as shown in Figure 4.2 to eliminate the effects of soil resistance.

Table 4.1 lists the pertinent information concerning these piles. The cushion was then hit by the ram and the resulting strains were measured at six points along the pile. Displacements and accelerations of both the ram and the head of the pile were also measured. However, even though the soil resistance had now been ex-

TABLE 4.1.	SUSPENDED	PILE	DATA
		~ ~ ~ ~ ~ ~	

Case			Pile			Cushion		Ram	am
	Material	E (psi)	Ap (in. ²)	L (ft)	Material	Ac (in. ¹)	t (in.)	Weight (lb)	Velocity (ft/sec)
LT-48	Class A Concrete	6.12x10 ⁶	254	65	Fir	62.8	9.0	4160	13.91
LT-41	Class A Concrete	6.12x10 ⁶	254	65	Micarta	89.1	9.0	4160	8.03
LT-39	Steel	30x10 ⁶	21.46	85	Oak	225.0	7.5	2128	11.42
LT-15	Class Y Concrete	*3.96x10	225	65	Oak	225.0	9.5	2128	13.98

 $E_{sonic} = 4.64 \times 10^{6} \text{ psi}$

PAGE TWENTY-TWO



Figure 4.4. Dynamic and static stress-strain curves for a fir cushion.

cluded, the shape of the stress wave still did not agree with the theoretical shape, and so the device illustrated in Figure 4.3 was used to see if the cushion's stress-strain diagram was actually a straight line.

Using this method, the dynamic stresses and strains were measured for several cushion materials. It was later discovered that for a given material, the dynamic stress-strain curves were almost identical to the corresponding static curves. This is demonstrated in Figure 4.4 in which the dynamic and static curves for a fir cushion are compared.

Since the stress-strain curves are not linear as assumed, the shape of the theoretical stress wave in the pile is not likely to agree with the experimental shape and so the "dynamic" curves were used.



Figure 4.5. Idealized test pile with known forces applied at head of the pile.

Furthermore, it is not known how much the rigidity of the pedestal shown in Figure 4.3 affects the cushion's behavior. Therefore, the wave equation was used to check the results. The second method required the following information: 1) the stresses determined experimentally at the head of the pile vs time, 2) the velocity of the ram at impact, and 3) the physical properties of the pile system required for solution by the wave equation.

As shown in Figure 4.5, both the cushion and ram are omitted and the previously determined stresses measured experimentally at gage 1 (see Figure 4.2) are placed on the head of the pile. The wave equation is then used to determine the motion of the ram and the pile, from which the compression of the cushion at any instant of time is known. By plotting the measured cushion forces against the corresponding compressions of the cushion, the dynamic stress-strain curve may be determined. The curves obtained by this method are illustrated in Figures 4.6, 4.7, and 4.8. Comparing these with Figure 4.4, it is noted that the curves are generally similar in shape.

Dynamic Coefficient of Restitution

Although the cushion is needed to limit the driving stresses in both hammer and pile, it reduces the available hammer energy because of internal damping. The load diagram shown in Figure 4.1 illustrates this energy loss since the energy input is given by the area ABC



Figure 4.6. Dynamic stress-strain curve for fir cushion (Case LT-48).

PAGE TWENTY-THREE



Figure 4.7. Dynamic stress-strain curve for a micarta cushion (Case LT-41).

while the energy output is given by area BCD. Usually this energy loss is accounted for by a coefficient of restitution of the cushion "e," in which

$$e = \sqrt{\frac{\text{Area under BCD}}{\text{Area under ABD}}}$$

When the dynamic stress-strain curve for the cushion is known, such as for the previous problem, the coefficient of restitution can be computed. As shown in Figure 4.6, the area under the dynamic curve ABC is computed by summing elemental areas ijkl until point B is reached (i.e., until the strain reaches a maximum), then the area under BCD is determined by summing elemental areas mnop until point D is reached.

Table 4.2 summarizes the results found for the curves of Figures 4.6, 4.7, and 4.8. These coefficients of restitution agree closely with values recommended by Hirsch.⁵⁵ It is interesting that although e = 0.8 is commonly recommended for a micarta capblock, these

TABLE 4.2. DYNAMIC CUSHION PROPERTIES

Case	Cushion Material	Dynamic e	Commonly Recommended e
LT-48	Fir	0.35	0.4055
LT-41	Micarta	0.60	0.8043
L/T-39	Oak	0.47	0.4855

PAGE TWENTY-FOUR



Figure 4.8. Dynamic stress-strain curve for an oak cushion (Case LT-39).

experiments indicate that e is actually much lower, probably around 0.6.

Idealized Dynamic Stress-Strain Curves

The major difficulty in using the dynamic curves derived in the previous section is that numerous points on the curve must be specified in the input data, unless the curve can be input in equation form. Although the



Figure 4.9. Idealized dynamic stress-strain curve for cushion (parabolic).



Figure 4.10. Dynamic force vs compression curves for a fir cushion (Case LT-48).

increasing load curve for each of the curves is nearly parabolic, the unloading segment is rather complex. Therefore, for convenience, the unloading segment will be approximated by a straight line having a slope such that the areas under the two curves result in the use of the correct coefficient of restitution for the cushion material being used.

Thus, the curve shown in Figure 4.9 can be defined by two different points on the loading curve (other than 0.0) and "e" of the material. The points on the curve are used to define the equation of the loading curve, and as long as the cushion strain increases, the increased input energy is computed as described earlier. When the strain in the cushion begins to decrease, the total input energy and the coefficient of restitution are used to determine the slope of the unloading curve in order to give the correct value of "e."

As shown in Figure 4.9, the total input energy is given by the area under the parabolic curve, $A_1 + A_2$, while the output energy is given by the area under the unloading curve, A_2 . Since e is defined by

$$e^2 = A_2/(A_1 + A_2),$$

then

 $A_2 = e^2(A_1 + A_2).$ But A_2 is also given by



Figure 4.11. Dynamic force vs compression curve for a micarta cushion (Case LT-41).



Figure 4.12. Dynamic force vs compression curve for an oak cushion (Case LT-39).

$$A_{2} = \left(\frac{S_{\max}-0}{2}\right) (\epsilon_{2}-\epsilon_{1})$$

$$e^{2}(A_{1}+A_{2}) = \left(\frac{S_{\max}}{2}\right) (\epsilon_{2}-\epsilon_{1})$$

$$(\epsilon_{2}-\epsilon_{1}) = \frac{2e^{2}(A_{1}+A_{2})}{S_{\max}}$$

Since the slope of the straight line BD is given by:

$$Ku = \frac{S_{max}}{(\epsilon_2 - \epsilon_1)}$$

where Ku defines the slope of the unloading curve, e is the coefficient of restitution of the material, $(A_1 + A_2)$ is the total area under the curve ABD (calculated by the computer), and S_{max} is the maximum stress in the cushion determined by the wave equation.

Figures 4.10, 4.11, and 4.12 compare experimental force vs compression curves obtained for the first three cases listed in Table 4.1, with those resulting from the parabolic idealization of Figure 4.9, and the straight line shown in Figure 4.1. Note that the parabolic curves closely represent the actual force-displacement curves while the linear curves are not nearly so close. In each case the parabolic curves tend to "over-shoot" the true maximum force, while the linear curve does not. The effect this has on the stress wave in the pile will be discussed in Chapter V.

PAGE TWENTY-FIVE

Comparison of Actual and Experimental Stress Waves

As noted in Chapter IV, the shape and magnitude of the stress wave in a pile is greatly dependent upon the properties of the cushion used. This will become apparent by comparing the actual stress wave determined experimentally with results found by using the idealized cushion properties mentioned earlier.

The solution for stresses in the pile should be more accurate if the effects of the cushion and ram can be omitted. To accomplish this, the force measured at the head of the pile and the stresses at other gage points were then determined by using the wave equation. The cases solved by this method are listed in Table 4.1. Comparisons between the experimental results and wave equation solutions at two points on the pile are shown in Figures 5.1 through 5.6.

One of the major factors which influenced these comparisons was the fact that the prestressed concrete



Figure 5.1. Theoretical vs experimental solution for Case LT-48, Gage #3.



Figure 5.2. Theoretical vs experimental solution for Case LT-48, Gage #5.

PAGE TWENTY-SIX

test piles cracked while setting up the experiment. Therefore, any reflected tensile forces greater than the prestressing force opened a small gap at the crack such that the prestressing strands alone could transmit the tensile stress down the pile. This is seen by the relative agreement shown in Figures 5.1 through 5.6. Note that the stress-waves shown for the concrete piles (Figures 5.1 through 5.4) do not agree nearly so well as those for the steel pile (Figures 5.5 and 5.6).

Still, the results agree closely in each case, not only in magnitude, but also in the over-all shape of the wave, thus indicating that the numerical solution to the wave equation is quite accurate. Further, any inaccuracies are likely due to faulty assumptions concerning the dynamic behavior of other variables such as the cushion, soil, etc.

As mentioned earlier, the stress-strain curve for the cushion is normally assumed to be linear as in Figure 4.1. The true stress-strain curves shown in Figures 4.6 through 4.8 indicate that the curves are not actually



Figure 5.3. Theoretical vs experimental solution for Case LT-41, Gage #3.



Figure 5.4. Theoretical vs experimental solution for Case LT-41, Gage #5.



Figure 5.5. Theoretical vs experimental solution for Case LT-39, Gage #3.



Figure 5.6. Theoretical vs experimental solution for Case LT-39, Gage #5.

linear and this assumption might therefore cause inaccuracies.

To determine how the shape of the curve affects the solution, the previous three problems were run using the cushion stress-strain curves shown in Figures 4.1 (straight line), 4.6 through 4.8 (true stress-strain curves), and 4.9 (parabolic curve). These solutions are compared in Figures 5.7 through 5.12. In each case, it is noted that the straight line solution is more accurate than the solution using the parabolic curve. This is because a simple parabolic curve was used which, even



Figure 5.7. Theoretical vs experimental solution for Case LT-48, Gage #3.

though it agrees with the actual stress-strain curve most of the time, it cannot follow the reversed curvature at the peak of the actual curve and thus "over-shoots" the true peak force. Figures 4.10 through 4.12 show how closely the parabolic curves follow the true cushion forces, and also how far off the straight line assumption is. The parabolic curve always peaks above the true force vs compression curve, while the spring rate of the straight line can be raised or lowered so that the true maximum cushion force is not exceeded.

Thus the use of the straight-line assumption seems reasonable since it gives fairly accurate results. The linear spring constants used for the curves shown in Figures 5.7 through 5.12 were first varied between wide limits to obtain the most accurate maximum stresses. These spring rates were then used to determine what dynamic modulus of elasticity was required to give the desired spring rate, using the equation: Edynamic = (K cushion) (Length)/(Area of cushion). As shown in Table 5.1, these results give a lower value of E for oak than for fir, which in this case is correct since the fir capblock was highly stressed (4,170 psi) while the oak capblock was stressed only slightly (765 psi).

Further consideration of the dynamic stress-strain curves revealed that the dynamic modulus of elasticity of the capblock is almost exactly 10 percent greater than that given by the slope of the stress-strain curve (Figures 4.6 through 4.8) taken at a point halfway between zero and the maximum strain. As noted by Hirsch,⁶² the static and dynamic stress-strain curves are quite similar, so that curves like those shown in Figures 4.6 through 4.8 are easily determined for any other cushion material.

TABLE 5.1 DYNAMIC PROPERTIES OF NEW CUSHION BLOCKS OF VARIOUS MATERIALS

Case	Cushion Material	Linear Spring Rate - K (lb/in.)	Depth of Cushion (in.)	Area of Cushion (in. ²)	Edynamic (psi)	Slope at Midpoint of Curve (psi)	SMAX in Cushion (psi)
LT-48	Fir	295,000	9.0	62.8	42,200	37,300	4170
LT-41	Micarta	2,320,000	9.0	89.1	234,000	212,000	3850
LT-39	Oak	585,000	7.5	225.0	19,500	17,300	765

PAGE TWENTY-SEVEN



Figure 5.8. Theoretical vs experimental solution for Case LT-48, Gage #5.

It was also recommended that the dynamic modulus be increased as the cushion consolidated. 63

Internal Damping in Piling

+

As noted earlier, differences between experimental and theoretical results were assumed to be the result of inaccurate soil information. Other parameters were also varied in an attempt to obtain more accurate results,⁵⁶ one of which was the material damping or internal damping capacity of the pile material.

Smith⁵⁷ first suggested that the internal damping in the pile might prove significant, and proposed the following equation by which hysterisis in the pile could be accounted for:

$$F(m,t) = C(m,t)K(m)$$

$$- \frac{BK(m)}{12\Delta t} [C(m,t) - C(m,t-1)]$$

in which B is the internal damping constant. He also recommended that B be given a value of about 0.002 in order to produce a narrow hysteresis loop. This equation was derived from the model shown in Figure 5.13



Figure 5.9. Theoretical vs experimental solution for Case LT-41, Gage #3.

PAGE TWENTY-EIGHT



Figure 5.10. Theoretical vs experimental solution for Case LT-41, Gage #5.

(b) and if B is set equal to zero, no damping is present, as seen in Figure 5.13 (a).

The model shown in Figure 5.13 (c) has one major advantage over the previous model in that it is able to account for damping by considering the difference between the material's static modulus of elasticity E, and its sonic modulus of elasticity E_s . This is because a slowly applied load gives the dashpot time to relax without causing the spring K_s to exert a force, thereby resulting in a spring rate equal to K_o . However, when the loads are applied rapidly the dashpot has no chance to deform, resulting in a spring rate of $K_o - K_s$. Thus for the model of Figure 5.13 (c), K_o is determined from the static modulus of elasticity E, while $K_o + K_s$ would use the sonic value E_s .

It is interesting to note that when K_s is infinitely large, model (c) becomes equivalent to model (b), and if $K_s = 0$, model (c) becomes equivalent to model (a).

In order to derive the equation, Figure 5.14 is provided. Figure 5.14 (a) illustrates the damping model wherein point "m" (on the upper mass) has moved a distance x_1 , point "n" (between the dashpot and spring)



Figure 5.11. Theoretical vs experimental solution for Case LT-39, Gage #3.

has moved a distance x_2 , and point "o" (on the lower mass) has moved a distance of x_3 . Assume that at time $t = t_0$ there exists a force F_0 ^{to} in the spring K_0 . There is also a force in the spring K_s given by F_s ^{to}, and a force in the dashpot equal to F_D ^{to}.

As shown in Figure 5.14 (b), after a single time interval passes, point m moves an additional distance Δx_1 , point na moves Δx_2 , and point o moves Δx_3 . At this time, $t = t_1 = t_0 + \Delta t$, and the forces in K₀, K_s, and B are designated F₀^t1, F_s^t1, and F_D^t1, respectively.

At time
$$t_0$$
:
 $F_s^{t_0} = K_s(x_1 - x_2)$. Eq. 5.1

At time $t_1 = t_0 + \Delta t_1$: $F_s^t 1 = K_s[(x_1 + \Delta x_1) - (x_2 + \Delta x_2)].$ $F_s^t 1 = K_s[(x_1 - x_2) + (\Delta x_1 - \Delta x_2)].$ Eq. 5.2

$$\mathbf{F}_{\mathbf{s}}^{t}\mathbf{1} = \mathbf{F}_{\mathbf{s}}^{t}\mathbf{o} + \mathbf{K}_{\mathbf{s}}(\Delta \mathbf{x}_{1} - \Delta \mathbf{x}_{2}). \qquad \text{Eq. 5.3}$$

By definition, at all times:

$$F_{D_{1}^{t}} = B \frac{(\Delta x_{2} - \Delta x_{3})}{\Delta t}.$$
 Eq. 5.4

Because point n must be in equilibrium:

$$F_{s}^{t}l = F_{D}^{t}l.$$
 Eq. 5.5

Substituting Equation 5.3 and 5.4 into 5.5:

$$F_{D}^{t}o + K_{s}(\Delta x_{1} - \Delta x_{2}) = B \frac{(\Delta x_{2} - \Delta x_{3})}{\Delta t}$$

$$F_{D}^{t}o + K_{s}\Delta x_{1} = K_{s}\Delta x_{2} + \frac{B\Delta x_{2}}{\Delta t} \frac{B\Delta x_{3}}{\Delta t}$$

$$F_{D}^{t}o + K_{s}\Delta x_{1} = K_{s}\Delta x_{2} + \frac{B\Delta x_{2}}{\Delta t} \frac{B\Delta x_{3}}{\Delta t}$$

 $F_{D}^{t}o\Delta t + K_{s}\Delta x_{1}\Delta t + B\Delta x_{3} = \Delta x_{2}(K_{s}\Delta t + B).$

Solving for Δx_2 :

$$\Delta x_2 = \frac{F_D t_0 \Delta t + K_s \Delta x_1 \Delta t + B \Delta x_3}{K_s \Delta t + B} \qquad \qquad \text{Eq. 5.6}$$

Substituting Equation 5.6 into 5.4 produces:

$$F_{D}^{t}1 = \frac{F_{D}^{t}o + K}{(K_{s}\Delta t/B) + 1} \qquad \text{Eq. 5.7}$$

The solution begins by setting F_D ^{to} equal to zero, and calculating it for the next time interval from Equation 5.7. The quantity K_s is a constant and $(\Delta x_1 - \Delta x_3)$ is simply the change in compression during a single time interval. Therefore, returning to the earlier terminology, Equation 5.7 can be written:

$$DF(I,t+1) = \frac{DF(I,t) + DK(I) [C(I,t+1) - C(I,t)]}{[DK(I)\Delta t/B] + 1.0 \text{ Eq. 5.8}}$$

where DF(I,t) is the damping force in dashpot number "I" during time interval "t," DK(I) is the dynamic spring rate of damping spring "I," C(I,t) is the compression in spring I during time interval number t, Δt is the time increment, and B is a damping constant.

The static force in spring I will be computed as before, by

$$F(I,t+1) = K(I)[C(I,t+1)].$$
 Eq. 5.9

Thus by adding the Equations 5.8 and 5.9, the total force acting on each mass can be determined for the next time interval.

Since as far as is known this derivation does not appear elsewhere, the boundary conditions for the damp-



Figure 5.12. Theoretical vs experimental solution for Case LT-39, Gage #5.





Figure 5.13. Various idealizations for the spring segment of a pile.

ing force given by Equation 5.7 were checked. From Equation 5.7,

(a) Letting
$$K_s = 0$$
: $F_D^{t_1} = \frac{F_D^{t_0} + 0}{1 + 0} = F_D^{t_0}$.

This is correct since F_D begins at zero and cannot increase in magnitude when $K_s = 0$.

(b) Letting
$$K_s = \infty$$
: $F_D^t 1 = \frac{F_D^t o + \infty}{\infty + 1} = \infty / \infty$.

Since this is indeterminate,

$$F_{D}^{t} \mathbf{1} = K_{s}^{1} \lim_{s \to \infty} \frac{\frac{d}{dK_{s}} [F_{s}^{t} \mathbf{0} + K_{s} (\Delta x_{1} - \Delta x_{3})]}{\frac{d}{dK_{s}} [\frac{K_{s} \Delta t}{B} + 1]}$$
$$= K_{s}^{1} \lim_{s \to \infty} \frac{\mathbf{0} + (\Delta x_{1} - \Delta x_{3})}{\Delta t/B + \mathbf{0}} = \frac{B(\Delta x_{1} - \Delta x_{3})}{\Delta t}.$$

This checks since it is the equation found when $K_s = \infty$ and only the dashpot remains. In this case the models of Figures 5.13 (b) and (c) would be identical

PAGE TWENTY-NINE



Figure 5.14. Idealized pile segment with standard linear solid damping.



Figure 5.15. Comparison of experimental and theoretical solutions for stresses at Gage #3 with damping omitted (Case LT-15).

(c) Letting B = 0:
$$F_D t_1 = \frac{F_D t_0 + K_s(\Delta x_1 - \Delta x_3)}{1 + \frac{K_s \Delta t}{0}}$$

= $\frac{1}{\infty} = 0.$

This checks since if the dashpot has no damping ability, the damping force must be zero.

(d) Letting
$$B = \infty$$
: $F_D^t 1 = \frac{F_D^t o + K_s(\Delta x_1 - \Delta x_3)}{\frac{K_s \Delta t}{\infty} + 1}$
= $F_D^t o + K_s(\Delta x_1 - \Delta x_3)$
But $F_D^t o = F_S^t o = K_s (x_1 - x_2)$.

PAGE THIRTY

Substituting this into the previous equation one finds $F_{D}^{t}1 = [K_{s}][(x_{1}-x_{2}) + (\Delta x_{1}-\Delta x_{2})]$

$$= [K_s][(x_1-x_2) + (\Delta x_1 - \Delta x_2)]$$

= [K_s][(x_1+\Delta x_1) - (x_2+\Delta x_2)]

= $[K_s]$ [Total compression at time t].

This is correct since it is the equation for the spring and when $B = \infty$, the dashpot is "locked" and no damping occurs.

(e) Letting
$$\Delta t = 0$$
: $F_D t_1 = \frac{F_D t_0 + K_s (\Delta x_1 - \Delta x_3)}{0+1}$

This result agrees because it gives the same result as letting $B = \infty$. (See part (d) above.)

(f) Letting
$$\Delta t \rightarrow \infty : F_D t_1$$

= $\frac{F_D t_0 + K_s (\Delta x_1 - \Delta x_3)}{\infty + B} = 0.$

This checks because the force stored in the damping spring would be released by relaxation of the dashpot if $\Delta t = \infty$.

(g) Let $\Delta x_1 = \Delta x_2$ and assume that the damping spring has an initial force stored at $t = t_0$. Although this force should diminish with time, it cannot go to zero during a single time interval, unless $\Delta t = \infty$.

$$\mathbf{F}_{\mathbf{D}}^{\mathsf{t}}\mathbf{1} = \frac{\mathbf{F}_{\mathbf{D}}^{\mathsf{t}}\mathbf{0} + \mathbf{K}_{\mathsf{s}}(\mathbf{0})}{\frac{\mathbf{K}_{\mathsf{s}}\Delta \mathbf{t}}{\mathbf{B}} + 1.0} = \frac{\mathbf{F}_{\mathbf{D}}^{\mathsf{t}}\mathbf{0}}{\frac{\mathbf{K}_{\mathsf{s}}\Delta \mathbf{t}}{\mathbf{B}} + 1.0}$$

This is correct since the force in the spring is reduced, but will never actually reach zero unless $\Delta t = \infty$.

Figures 5.15 through 5.18 compare the effects of damping in a pile using the damping models shown in Figure 5.13. The results given are for test pile number LT-15 which is described in Table 4.1. This particular pile was of lightweight concrete with $E = 3.96 \times 10^6$ and $E_s = 4.63 \times 10^6$ psi. This problem was chosen since E_s was relatively larger than E, indicating the possibility of rather high damping.

However, one is often more interested in the maximum stresses found in the pile, which usually occurs during the first or second pass of the stress wave along the pile. During this time the effects of damping are small and can usually be neglected.



Figure 5.16. Comparison of experimental and theoretical solutions for stresses at Gage #3 for different damping models (Case LT-15).



Figure 5.17. Comparison of experimental and theoretical solutions for stresses at Gage #5 with damping omitted (Case LT-15).

This conclusion may not be accurate for timber piles since wood has a much higher damping capacity than either the steel or concrete piles for which experimental data were available. This higher damping capacity might affect the results earlier in the solution which might in turn lower the accuracy of the results. Nevertheless, if more testing should indicate that the damping models are accurate for timber piling too, then the problem, or rather the uncertainties of damping effects will no longer be a problem.

In any case, if the wave is to be studied for an extended period of time, damping in the pile cannot be



Figure 5.18. Comparison of experimental and theoretical solutions for stresses at Gage #5 for different damping models (Case LT-15).

neglected. This is illustrated in Figures 5.15 and 5.17 where fairly large errors resulted when damping was neglected. On the other hand, Figures 5.16 and 5.18 suggest that in certain cases damping should be accounted for using either of the damping models of Figure 5.13.

The most surprising result of this study is not the accuracy of the damping models, but rather that both models give nearly identical results even though Smith's model is extremely simple while the other is rather complex. Again, this may also prove incorrect for timber piling or other piling which has a large damping capacity. For example, one of the above methods might be more accurate than the other.

Chapter VI SOIL PROPERTIES

Idealized Soil Resistance Curves

The load-deformation characteristics assumed for the soil in Smith's numerical solution are shown in Figure 6.1 (a). This curve excludes the damping effects of the soil caused by rapid loading, and illustrates only the soil resistance caused by static loading. As shown, the two parameters required to define the load-deformation curve are the ground quake "Q(m)" and the ultimate static soil resistance "Ru(m)."

When the soil is located along the side of the pile, it is assumed to resist any rebound of the pile as well as any downward motion. This is typified by the curve OABCDEFG. However, the soil located at the tip of the pile can only exert upward forces, as represented by the curve OABCFCB.

The spring rate for the curve between point O and A may now be determined from

$$K'(m) = \frac{Ru(m)}{Q(m)}$$

In order to include the damping effects of the soil, a third variable J(m) is defined as the damping constant of soil spring "m." Thus the total resistance of

the soil, including the effect of loading rate, is given by

$$R(m,t) = [D(m,t) - D'(m,t)] K'(m)[1 + J(m)V(m,t-1)]$$

where m denotes the segment number of the pile, t is the time interval number, D(m,t) is the displacement of segment m at time interval number t, K'(m,t) is the plastic deformation of the soil, J(m) is the soil damping constant, K'(m) is the soil spring constant, V(m,t) is the velocity of mass number m at time interval number t, and R(m,t) is the soil resistance acting on that element at time t.

In cases in which more accurate soil data are available, the general soil resistance curve of Figure 6.1 (b) may be used to advantage. This curve also uses the variables Q(m) and Ru(m), but the curve no longer must be linear. In this case, the ground quake Q(m) is divided into ten equal segments, and the static soil resistances corresponding to these ten points comprise the input data required to establish the curve. Also, as shown in Figure 6.1 (b), the slope of the unloading curve is given by K'(m). A more complete discussion of the use of this method is given in the appendix.

To check out the programming changes involved in this method, several problems were first solved using

PAGE THIRTY-ONE



(a) ELASTIC-PLASTIC OR "LINEAR" SOIL RESISTANCE CURVE



(b) GENERALIZED SOIL RESISTANCE CURVE

Figure 6.1. Load-deformation characteristics assumed for the soil.

the regular elastic-plastic curve of Figure 6.1 (a). These problems were then solved again using the generalized soil resistance method with soil resistance values lying on the same curve, the two solutions then being checked for identical results.

A number of other problems were also solved to see what changes might result when the shape of the soil resistance curve was altered. For example, the linear soil resistance curve used in a problem originally solved by Smith⁵⁸ is shown in Figure 6.2 (a). This problem was then solved using the nonlinear curve of Figure 6.2 (b).

The solutions for these two problems, shown in Table 6.1, are typical of the results found for the other cases studied, in that a rather large change in the soil curve changed the results only slightly. In this case,

TABLE 6.1. COMPARISON OF RESULTS FOUND BY USING ELASTIC-PLASTIC VS NONLINEAR SOIL RESISTANCE CURVES

	Maxi	Maximum		
Type of Soil Resistance	At Head of Pile	At Center of Pile	At Point of Pile	Point Displace- ment (in.)
Elastic Plastic	290	300	405	0.203
Nonlinear	290	301	370	0.218
Percent Change	0.0	+0.3		+7.4

PAGE THIRTY-TWO

for example, although the soil quake was doubled and the curve made nonlinear, the maximum change in stress was less than 9 percent, and the permanent set increased less than 8 percent. Only a drastic change in the soil resistance curve was found to cause an appreciable difference in the solution.

Therefore, if the soil resistance curve for the problem even slightly resembles the curve of Figure 6.2 (a), the linear resistance equation will probably be satisfactory. Whenever it becomes necessary, the nonlinear soil resistance can be used as explained in the appendix.

Significance of the Soil Quake "Q"

The properties of the soil under the action of dynamic loading are probably the least understood of the many variables affecting the problem.⁶⁴ Although a number of values for the soil quake may be used, the value Q = 0.1, recommended by Chellis⁶⁵ is probably the most widely accepted for general use, except when a more accurate value can be determined. As might be expected, the trouble stems mainly from the large number of variables influencing the value of Q at any given driving location, the most obvious of course being the type of soil encountered. Much work is presently being done to define these factors and to more accurately determine the actual values for both "Q" and "J" to increase the solution's accuracy.^{66,67}






While it is beyond the scope of this paper to attempt to determine values for Q, it is interesting to see how the value of Q affects the solution. After a number of the Michigan research problems with varying values of Q were studied, Case BLTP—6; 57.9 was chosen as being fairly representative. The problems were solved with Q ranging from 0.1 to 0.5, as seen in Table 6.2. To determine whether Q would have similar effects at all magnitudes of soil resistance, Ru_{total} was also varied. The results of this parameter study are given in Table 6.2.

One of the trends noted in Table 6.2 is the small effect Q has on the maximum compressive force found in the pile. The effect on tensile force is more pronounced, although no conclusion could be reached as to whether the tensile stress will increase or decrease as Q changes since the results did not indicate an apparent trend. Maximum ENTHRU values are also relatively independent of the soil quake, with ENTHRU tending to decrease as the soil quake increases.

The most pronounced and consistent trend is the marked increase in maximum point displacement corresponding to increasing values of Q. It is also noted that the percent increase in maximum point displacement is relatively small for a small soil resistance, but greatly increases as the total soil resistance becomes large. This is also shown in Figure 6.3. Similar results

TABLE 6.2. INFLUENCE OF SOIL QUAKE AT DIF-FERENT SOIL RESISTANCES FOR CASE BLTP-6; 57.9 WITH NO SOIL DAMPING

Total Soil Resistance (kip)	Q (in.)	Maxi- mum Point Displace- ment (in.)	Maximum ENTHRU (kip ft)	Maxi- mum Com- pressive Force (kip)	Maxi- mum Tensile Force (kip)
50	$0.1 \\ 0.2 \\ 0.3 \\ 0.4 \\ 0.5$	$1.49 \\ 1.51 \\ 1.51 \\ 1.54 \\ 1.58$	$6.80 \\ 6.80 \\ 6.73 \\ 6.71 \\ 6.69$	$225 \\ 222 \\ 221 $	$109 \\109 \\114 \\119 \\124$
100	0.1 0.2 0.3 0.4 0.5	0.84 0.88 0.90 0.93 0.97	$\begin{array}{c} 6.96 \\ 6.88 \\ 6.86 \\ 6.84 \\ 6.83 \end{array}$	230 224 223 222 222 222	68 85 97 98 97
150	$0.1 \\ 0.2 \\ 0.3 \\ 0.4 \\ 0.5$	$\begin{array}{c} 0.56 \\ 0.57 \\ 0.61 \\ 0.64 \\ 0.69 \end{array}$	$7.10 \\ 7.05 \\ 6.93 \\ 6.88 \\ 6.85$	235 227 225 223 223 223	91 90 128 163 188
200	0.1 0.2 0.3 0.4 0.5	$\begin{array}{c} 0.41 \\ 0.44 \\ 0.48 \\ 0.52 \\ 0.56 \end{array}$	$7.21 \\ 7.13 \\ 7.06 \\ 6.99 \\ 6.90$	240 230 226 224 224	79 67 77 107 118
300	0.1 0.2 0.3 0.4 0.5	0.22 0.30 0.36 0.42 0.47	$7.28 \\ 7.24 \\ 7.16 \\ 7.10 \\ 7.05$	250 234 229 225 224	$ \begin{array}{r} 82 \\ 108 \\ 111 \\ 59 \\ 73 \end{array} $
400	0.1 0.2 0.3 0.4 0.5	$\begin{array}{c} 0.11 \\ 0.21 \\ 0.29 \\ 0.36 \\ 0.41 \end{array}$	$7.30 \\ 7.28 \\ 7.24 \\ 7.18 \\ 7.12$	260 239 233 228 226	$127 \\ 114 \\ 158 \\ 158 \\ 102$

were found for the other Michigan cases studied, except that the tensile force often varied substantially more than indicated for the case of Table 6.2.

Significance of the Soil Damping

Michigan Case BLTP-6;57.9 was also chosen to illustrate the damping effects of the soil. These damping constants were given values ranging from 0.0 to 0.5, and as was done in the previous section, the total soil resistance was varied from 50 to 400 kip to see if trends found at low resistances would also be noted when the soil resistance was large. Since the soil damping constants most commonly used are those recommended by Smith,⁶⁸ i.e., a soil damping constant of 0.05 sec/ft along the side of the pile and 0.15 sec/ft at the point of the pile, the variation of J = 0.0 to 0.5 very likely covers the values typical for many conditions and soils. These results are given in Table 6.3.

As was previously determined for Q, the soil damping constants also have little effect on the maximum ENTHRU values. The maximum compressive forces do

TABLE 6.3. INFLUENCE OF SOIL DAMPING ON DIFFERENT SOIL RESISTANCES FOR CASE BLTP-6; 57.9 (Q = 0.1 FOR ALL CASES)

			-		
		Maxi-		Maxi-	
		mum		mum	Maxi-
m		_ Point		Com-	_mum
Total Sc			-Maximum	pressive	Tensile
Resistan		ment	ENTHRU	Force	Force
(kip)	(sec/ft)	(in.)	(kip ft)	(kip)	(kip)
50	0.0	1.49	6.80	225	109
	0.1	1.11	6.89	221	68
	0.2	0.85	7.03	221	41
	0.3	0.72	7.21	221	18
	0.4	0.63	7.23	222	6
	0.5	0.56	7.25	222	5
100	0.0	0.84	6.96	230	68
	0.1	0.58	7.12	222	31
	0.2	0.49	7.20	223	11
	0.3	0.43	7.25	223	14
	0.4	0.38	7.27	224	12
	0.5	0.34	7.28	225	17
150	0.0	0.56	7.10	235	91
	0.1	0.42	7.23	223	23
	0.2	0.34	7.26	224	21
	0.3	0.28	7.28	225	26
	0.4	0.24	7.27	239	24
	0.5	0.21	7.26	251	22
200	0.0	0.41	7.21	223	79
	0.1	0.28	7.28	225	35
	0.2	0.22	7.28	239	37
	0.3	0.18	7.25	255	31
	0.4	0.15	7.22	267	27
	0.5	0.13	7.20	274	26
300	0.0	0.22	7.28	250	82
	0.1	0.12	7.23	272	53
	0.2	0.09	7.18	286	41
	0.3	0.08	7.14	293	33
	0.4	0.07	7.11	298	31
	0.5	0.07	7.07	302	$\overline{30}$
400	0.0	0.11	7.20	260	127
	0.1	0.07	7.13	308	61
	0.2	0.06	7.07	313	41
	0.3	0.05	7.02	314	35
	0.4	0.05	6.96	314	33
	0.5	0.05	6.90	314	33

PAGE THIRTY-THREE



Figure 6.3. Maximum point displacement vs quake (Case BLTP-6; 57.9).

have a tendency to increase as J increases, especially when the soil resistance is large. While the tensile forces still do not follow any definite pattern, they are somewhat more regular than those determined by varying "Q."



Figure 6.4. Maximum point displacement vs soil damping constant (Case BLTP-6; 57.9).

The maximum point displacements again show the most consistent trend as J is varied, as shown in Figure 6.4. The other cases studied showed this same trend, i.e., as J increases, the maximum displacement decreases rapidly.

Chapter VII CONCLUSIONS

The correlation between the numerical solution and the experimental data presented in Chapter V indicates the potential accuracy of Smith's method, but the problem involves so many important parameters that it is extremely important to know as much as possible about their actual behavior.

As shown in Chapter III, it is possible to determine valuable information from the wave equation even though exact values for some of these parameters are unknown. For example, several problems can be solved in which the unknown parameter varies between upper and lower limits as was done to determine the effect of the ram's elasticity. This study shows that only for steel on steel impact does the elasticity of the ram affect the solution.

In order to study the Michigan data over 5,000 problems had to be solved because certain key informa-

PAGE THIRTY-FOUR

tion such as the ram velocity was not reported. Still, it was possible to study the behavior of the pile-driving hammers discussed. For example, the efficiency of the cushion assembly was remarkably consistent, in that they were nearly independent of the type of pile, pile length, and soil resistance. The correlation between the wave equation and the field data shown in Chapter III further illustrates that Smith's method is accurate, especially when the required data are known and need not be assumed.

Much of the value of this method of analysis is its flexibility. As illustrated in Chapter III, the wave equation can be used for any number of studies which otherwise would not be possible.

It was shown that the stress-strain curve for a cushion is not a straight line. Instead, it follows a curve which is closely parabolic. However, a straight line which has a slope equal to that of the true stress-strain curve taken at a point halfway between zero and the maximum strain gives accurate results. The cushion's dynamic coefficient of restitution was found to agree with commonly recommended values.

The effect of internal damping in the concrete and steel piles was shown to be negligible in these cases, although it can be accurately accounted for by the wave equation if desired.

The data from the Michigan Study of Pile Driving Hammers were extrapolated to evaluate the true energy output of different pile driving hammers. It was found that the energy output for all types of hammers (steam

- and diesel) can be determined by the simple equation: $E = W_R x h x e$
 - where E = energy output in ft-lb
 - $W_{R} = ram$ weight in lb,
 - h = ram stroke or equivalent stroke in ft, and
 - e = hammer efficiency (found to be 60%for the Vul. No. 1, 87% for the Vul. 50C and 80C, and 100% for the diesel hammers investigated by the Michigan Study).

This is believed to be a most significant finding in view of the existing controversy over the manufacturers' rated energies for diesel hammers.

Recommendations

RECOMMENDATIONS FOR FURTHER RESEARCH

The following areas are recommended for further research:

1. A complete evaluation of the data collected by the Michigan State Highway Commission, including correlation of hammer energy, permanent set of pile per blow, etc. This would require a major research effort because of the quantity of data reported. Also, because certain variables were not determined, several theoretical solutions must be solved for each attempt correlation until the unknown parameter can be "pinned down" with reasonable accuracy. For example, the solutions for over 5,000 problems were required to complete the 28case study made in Chapter III.

2. A study to determine how to improve the effi-

ciency of the pile-driving hammers presently in use. This type of research should be most interesting to the hammer manufacturers since present equipment could be optimized to drive piling faster and/or reduce the driving stresses during driving. The possibility that today's pile-driving hammers are as efficient as possible through trial and error is remote.

3. Further research is needed to insure that the damping models proposed in Chapter IV are also accurate for timber piling, and to determine what damping constants should be used.

4. Major research efforts are needed to investigate every aspect of the soil resistance acting on the pile during driving.

- 1. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Proc. ASCE, Aug., 1960, p. 35.
- 2. Federal Construction Council, "Foundation Piling," Building Research Advisory Board, National Academy of Sciences—National Research Council, Publication 987, 1962, p. 28.
- 3. Ibid, p. 8.
- 4. Cummings, A. E., "Dynamic Pile Driving Formulas," Journal of Boston Soc. of Civil Engrs., Jan., 1940.
- 5. Forehand, P. W. and J. L. Reese, "Pile Driving Analysis Using the Wave Equation," Master of Science in Engineering Thesis, Princeton University, 1963, p. 5.
- Isaacs, D. V., "Reinforced Concrete Pile Formula," Inst. Aust. Eng. J., Vol. 12, 1931, p. 415.
- Fox, E. N., "Stress Phenomena Occurring in Pile Driving," *Engineering* (London) Vol. 134, 1932, p. 312.
- 8. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Proc. ASCE, Aug., 1960.
- 9. Chellis, R. D., "Pile Foundations," McGraw-Hill Book Co., New York, 1951, p. 20.
- 10. Fox, E. N., "Stress Phenomena Occurring in Pile Driving," Engineering (London) Vol. 134, 1932.
- 11. Taylor, D. W., "Fundamentals of Soil Mechanics," John Wiley & Sons, New York, 1956, p. 770.
- 12. Isaacs, D. V., "Reinforced Concrete Pile Formula," Inst. Aust. Eng. J., Vol. 12, 1931, p. 312.
- Fox, E. N., "Stress Phenomena Occurring in Pile Driving," *Engineering* (London) Vol. 134, 1932, p. 263.
- Glanville, W. H., G. Grime, E. N. Fox, and W. W. Davies, "An Investigation of the Stresses in Reinforced Concrete Piles during Driving," British Bldg. Research Bd. Tech. Paper No. 20, D. S. I. R., 1938.
- Cummings, A. E., "Dynamic Pile Driving Formula," Journal of Boston Soc. of Civil Engrs., Jan., 1940, p. 6.
- Smith, E. A. L., "Pile Driving Impact," Proceedings, Industrial Computation Seminar, September, 1950, International Business Machines Corp., New York, N. Y., 1951, p. 44.
- 17. Smith, E. A. L., "Impact and Longitudinal Wave Transmission," Transactions, ASME, August, 1955, p. 963.
- Smith, E. A. L., "What Happens When Hammer Hits Pile," *Engineering News Record*, McGraw-Hill Publishing Co., Inc., New York, N. Y., September 5, 1957, p. 46.
- 19. Smith, E. A. L., "Tension in Concrete Piles During Driving," *Journal*, Prestressed Concrete Institute, Vol. 5, 1960, pp. 35-40.
- 20. Smith, E. A. L., "The Wave Equation Applied to Pile Driving," Raymond Concrete Pile Co., 1957.
- 21. Smith, E. A. L., "Pile Calculations by the Wave Equation," *Concrete and Constructional Engr.*, London, June, 1958.

- 22. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Proc. ASCE, Aug., 1960.
- 23. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Transactions, ASCE, Vol. 127, 1962, Part I, p. 1171.
- 24. Samson, Charles H., Jr., "Pile Driving Analysis by the Wave Equation (Computer Procedure)," Report of the Texas Transportation Institute, Texas A&M University, May, 1962.
- Samson, Charles H., Jr., "Investigation of Behavior of Piles During Driving, Lavaca Bay Causeway," Unpublished Report of TTI to Texas Highway Dept., 1962.
- Samson, Charles H., Jr., "Pile Stress Analysis— Harbor Island Bay Bridge," Unpublished Report of the Texas Transportation Institute, July, 1962.
- 27. Hirsch, T. J., "Stresses in Long Prestressed Concrete Piles During Driving," Report of the Texas Transportation Institute, Texas A&M University, September, 1962.
- 28. Forehand, P. W. and J. L. Reese, "Pile Driving Analysis Using the Wave Equation," Master of Science in Engineering Thesis, Princeton University, 1963.
- Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, 1963.
- Hirsch, T. J., C. H. Samson, Jr., and L. L. Lowery, "Driving Stresses in Prestressed Concrete Piles," Structural Eng. Conf. of ASCE, San Francisco, Oct., 1963.
- 31. Hirsch, T. J., "Field Tests of Prestressed Concrete Piles During Driving," Report of the Texas Transportation Institute, Texas A&M University, August, 1963.
- 32. Hirsch, T. J., "Computer Study of Variables which Affect the Behavior of Concrete Piles During Driving," Report of the Texas Transportation Institute, Texas A&M University, August, 1963.
- 33. Samson, C. H., Jr., F. C. Bundy, and T. J. Hirsch, "Practical Applications of Stress-Wave Theory in Piling Design," Presented to the annual Texas Section ASCE meeting, San Antonio, Texas, October, 1963.
- 34. Hirsch, T. J., and C. H. Samson, Jr., "Driving Practices for Prestressed Concrete Piles," Report of the Texas Transportation Institute, Texas A&M University, April, 1965.

ł

- 35. Hirsch, T. J., "Fundamental Design and Driving Considerations for Concrete Piles," 45th Annual Meeting of Highway Research Board, Washington, D. C., January, 1966.
- 36. Hirsch, T. J., and Thomas C. Edwards, "Impact Load-Deformation Properties of Pile Cushioning Materials," Report of the Texas Transportation Institute, Texas A&M University, July 1965.

PAGE THIRTY-SIX

- 37. Smith, E. A. L., "Pile Driving Impact," Proceedings, Industrial Computation Seminar, September, 1950, International Business Machines Corp., New York, N. Y., 1951.
- 38. Smith, E. A. L., "Impact and Longitudinal Wave Transmission," Transactions, ASME, August, 1955.
- 39. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Proc. ASCE, Aug., 1960.
- 40. Forehand, P. W., and J. L. Reese, "Pile Driving Analysis Using the Wave Equation," Master of Science in Engineering Thesis, Princeton University, 1963.
- 41. Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, 1963.
- 42. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Transactions, ASCE, Vol. 127, 1962, Part I, p. 1152.
- 43. Chellis, R. D., "Pile Foundations," McGraw-Hill Book Co., New York, 1951, p. 29.
- 44. Michigan State Highway Commission, "A Performance Investigation of Pile Driving Hammers and Piles," Office of Testing and Research, Lansing, March, 1965.
- 45. Housel, W. S., "Pile Load Capacity: Estimates and Test Results," *Journal of the Soil Mechanics and Foundations Division*, ASCE, Proc. Paper 4483, September, 1965.
- 46. Michigan State Highway Commission, "A Performance Investigation of Pile Driving Hammers and Piles," Office of Testing and Research, Lansing, March, 1965, p. 330.
- 47. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Transactions, ASCE, Vol. 127, 1962, Part I.
- 48. Forehand, P. W. and J. L. Reese, "Pile Driving Analysis Using the Wave Equation," Master of Science in Engineering Thesis, Princeton University, 1963.
- 49. Michigan State Highway Commission, "A Performance Investigation of Pile Driving Hammers and Piles," Office of Testing and Research, Lansing, March, 1965, p. 246.
- Hirsch, T. J., and Thomas C. Edwards, "Impact Load-Deformation Properties of Pile Cushioning Materials," Report of the Texas Transportation Institute, Texas A&M University, July, 1965, p. 1.
- 51. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Transactions, ASCE, Vol. 127, 1962, Part I, p. 1162.
- 52. Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, 1963.
- 53. Hirsch, T. J., and Thomas C. Edwards, "Impact Load-Deformation Properties of Pile Cushioning

Materials," Report of the Texas Transportation Institute, Texas A&M University, July, 1965.

- 54. Hirsch, T. J., and Thomas C. Edwards, "Impact Load-Deformation Properties of Pile Cushioning Materials," Report of the Texas Transportation Institute, Texas A&M University, July, 1965.
- 55. Ibid. p. 29.
- Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, 1963.
- Jacobsen, L. S., "Steady Forced Vibrations as Influenced by Damping," ASME Transactions, Vol. 52, 1930, p. 168.
- 58. Smith, E. A. L., "Pile Driving Analysis by the Wave Equation," Transactions, ASCE, Vol. 127, 1962, Part I, p. 1167.
- Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, 1963, p. 417.
- 60. Ibid, p. 427.
- 61. Ibid, p. 429.
- 62. Hirsch, T. J., and Thomas C. Edwards, "Impact Load-Deformation Properties of Pile Cushioning Materials," Report of the Texas Transportation Institute, Texas A&M University, July, 1965, p. 21.
- 63. Ibid, p. 20.
- 64. Samson, C. H., Jr., T. J. Hirsch, and L. L. Lowery, "Computer Study of Dynamic Behavior of Piling," *Journal of the Structural Division*, ASCE, Vol. 89, No. ST4, Proc. Paper 3608, August, '1963, p. 418.
- 65. °Chellis, R. D., "Pile Foundations," McGraw-Hill Book Co., New York, 1951, p. 23.
- 66. Chan, P. A., "A Laboratory Study of Dynamic Load-Deformation and Damping Properties of Sands Concerned with a Pile-Soil System," a dissertation, Texas A&M University, unpublished, January, 1967.
- 67. Hirsch, T. J., and Thomas C. Edwards, "Use of the Wave Equation to Predict Pile Load Bearing Capacity," Report of the Texas Transportation Institute, Texas A&M University, unpublished, August, 1966.
- 68. Samson, C. H., Jr., F. C. Bundy, and T. J. Hirsch, "Practical Applications of Stress-Wave Theory in Piling Design," Presented at the annual Texas Section ASCE meeting, San Antonio, Texas, October, 1963, p. 1162.
- 69. Rand, Mogens, "Explosion Adds Driving Force to Diesel Hammer," *Engineering Contract Record*, December, 1960.
- 70. Rand, Mogens, "Test Performed with the Delmag Diesel Hammer, Type D-12," December 13, 1955, Publication of the Department of Mechanical Engineering, University of Toronto.
- 71. Rand, Mogens, "How the Diesel Pile Hammer Works," Roads & Streets, May, 1961.

PAGE THIRTY-SEVEN

Appendix A

PROGRAM INPUT DATA

<i><u><u></u></u></i> () (
CARD 101 (I ID1 and		All "ID" values are for identifica- tion only and can be either alpha- betic or numeric.
$1/\Delta t$		Time interval. If left blank, $\Delta tcr/2$ will be used. (1/sec)
MP		Total number of segments in the system to be analyzed.
VELMI	<u> </u>	Initial velocity of the ram. (ft/sec)
MH	_	Element number of the first pile segment.
NR		Number of divisions of the ram.
EEM(NR) —	Coefficient of Restitution of spring number NR, directly under ram.
EEM(NR	+1) -	Coefficient of Restitution of spring number NR+1.
GAMMA (NR) —	The minimum force in the spring beneath the ram once that force has reached a maximum. (kip) For example, if the diesel hammer explosive pressure causes 158.7 kip minimum force in this spring, set GAMMA(NR) = 158.7 kip. If the minimum force the spring can transmit is zero (for example, when no tensile force can exist be- tween the ram and anvil) set the corresponding $GAMMA(I) = 0.0$. If the spring represents a continu- ous body such as the spring be- tween any two pile segments, it can transmit tensile forces between the elements. This is signified by set- ting $GAMMA(I)$ equal to any negative value, usually -1.0 kip.
GAMMA (NR+1)		Same as above, but for spring number $NR+1$.
NSTOP		Total number of time intervals the program is to run.
NOP(I)	VALUE	FUNCTION
NOP(1)		Used to read cards 103-106 and print out the data for problem identification.
	= 1	No identification card is to be used.
	= 2	Read and print a single ID card. (card 103)
	= 3	Read and print two ID cards. (cards 103 and 104)
	= 4	Read and print ID cards 103, 104, and 105.
• •	= 5	Read and print ID cards 103, 104, 105, and 106.
NOP(2)		Used to specify the input method for the segment weights WAM(I).
×	= 1	Read one weight for each segment (card series 200).
	= 2	Read the segment weights for only the first five and last five seg- ments of the pile system from a single card (card 200), and equate all remaining segment weights to the sixth weight in the system. (NOP(2) = 2 is used when a large number of equal weights are pres- ent except for the first or last few weights.)

NOP(I)	VALUE	FUNCTION
NOP(3)		Used to specify the input method for the internal spring stiffness. (XKAM(I).
	=1	Read one stiffness for each inter- nal spring from card series 300.
	= 2	Read the stiffness values for only the first five and last five internal springs on a single card 300, and assign the fifth value to all re- maining internal springs.
		(NOP(3) = 2 is used under the same conditions as $NOP(2) = 2$.
NOP(4)		Used to specify what soil resist- ance distribution act along the pile.
	= 1	Read RUM(I) for each element from card series 400, and set the point bearing soil resistance RUM (MP+1) equal to RUP.
	* = 2	Set all side resistances equal to zero, and set $RUM(MP+1) = RUP$.
	= 3	Distribute RUT-RUP uniformly along the side of the pile from segment MO thru MP, and set RUM(MP+L) = RUP.
	— 4	Distribute RUT-RUP triangularly along the pile between segments MO and MP, and set $RUM(MP+1)= RUP$.
	= 5	Read one 450 series card for each mass upon which a nonlinear re- sistance vs displacement curve acts. If a linear curve also hap- pens to be acting on an element, it must also be input on a 450 series card.
NOP(5)		Used to specify the input method for GAMMA(I). Note: The sig- nificance of GAMMA(I) is dis- cussed in the "500 card series."
	= 1,2	Read GAMMA1 and GAMMA2 from card 101 and assign GAM- MA1 to internal spring number NR, and assign GAMMA2 to spring number NR+1. Then set GAM- MA(I) of the remaining springs to -1.0 .
	· 🖮 3	Same as for $NOP(5)=2$, except that $GAMMA(NR+2)$ is also set equal to 0.0.
	= 4	Same as for NOP(5)=2, except GAMMA(NR+2)=0.0 and GAM- MA(NR+3)=0.0. This option is used when a large number of ele- ments such as an anvil, follower load cell and pile cap are encoun- tered, since these elements cannot transmit a tensile force to the next element. This option can be used to set up to eight consecutive val- ues of GAMMA(I)=0.0 by setting NOP(5)=8.
	= 9	Read GAMMA(I) for each spring from card series 500.

PAGE THIRTY-EIGHT

NOP(I)	VALUE	FUNCTION
NOP(6)		Used to specify the input method for $EEM(I)$.
	= 1 = 2	Read EEM1 and EEM2 from card 101 set EEM(NR)=EEM1, and EEM(NR+1)=EEM(2). Then set EEM(I) for all other springs equal to 1.0 (perfectly elastic). Read EEM(I) for each spring
NOP(7)		from card series 600. Used to specify the input method for BEEM(I).
• • •	= 1 = 2	Set all $BEEM(I) = 0.0$. Read $BEEM(I)$ for each spring from card series 700.
NOP(8)		Used to specify the input method for VEL(I).
	= 1	Read VELMI from card 101 and set VEL $(I,t=0)$ for all segments of the ram (usually one segment) equal to VELMI. Set all other
	= 2	VEL(I) = 0.0. Read $VEL(I)$ for each segment from card series 800.
NOP(9)		Used to specify input method for $Q(I)$.
	= 1	Read QSIDE and QPOINT from card 102 and set all Q(I) along side of the pile equal to QSIDE. Set Q(MP+1) under pile tip equal to QPOINT.
	= 2	Read $Q(I)$ for each element includ- ing $Q(MP+1)$ from card series 900.
NOP(10)		Used to specify input method for $SJ(I)$.
		Read SIDEJ and POINTJ from card 102. Set all $SJ(I)$ along side of pile equal to SIDEJ and $SJ(MP$ +1) under pile tip equal to POINTJ.
		Read $SJ((I)$ for each element in- cluding $SJ(MP+1)$ from card se- ries 1000.
NOP(11)		Used to specify the input method for DYNAMK(I).
	= 2	Set all DYNAMK(I) = 0.0. Read DYNAMK(I) for each spring from card series 1100.
NOP(12)		Used to specify input method for A(I).
		Read AREA from card 102 and set all $A(I)$ equal to AREA.
	= 2	Read A(I) for each internal spring from card series 1200.
NOP(13)		Used to specify which method of internal damping is to be used in the pile.
	- 2	Use Smith's method (refer to Fig- ure 5.13b). Use standard linear solid method (refer to Figure 5.13c).
NOP(14)	1	Used to specify how the force in the cushion after impact is to be determined.
• •	•	Calculate cushion forces from the wave equation applied to the mov- ing ram after impact.

NOP(I)	VALUE	FUNCTION
	= 2 = 3	In this case, the force at the head of the pile at all times is known, probably by experimental methods, and this force curve is to be ap- plied at the head of the pile. The force at each time interval FOR- CIN(t) is read from card series 1300 (kip). Same as when NOP(14)=2, except
		that galvanometer readings rather than forces at each time interval are input and the cushion forces are determined by the computer. In this case, the information on the 1400 header card is needed, fol- lowed by the galvanometer deflec- tion at each time interval from card series 1400.
NOP(15)		Used to specify how gravity is to be accounted for in the solution.
	= 1	The effect of gravity is to be neg- lected.
	= 2	Gravity is to be considered, with the initial displacement of each segment, $D(I,O)$, and the initial soil resistances RAM(I,O) assumed
	= 3	to be zero. Gravity is to be considered, and $D(I,O)$ and $RAM(I,O)$ are to be approximated by Smith's suggested method. ⁶⁰
	= 4	Gravity is to be considered, and the values for $D(I,O)$ and $RAM(I,O)$ are computed by Samson's suggested method. ⁶¹
NOP(16)	= 1	Used to specify the number of problems to be solved using the basic data given on cards 101 through the 1700 card series. Only one problem is to be solved
	= 2	Run more than one problem with changes in these data as specified on card 1600.
NOP(17)		Used to specify whether the ulti- mate pile capacities predicted by various pile driving equations are desired.
	= 1 = 2	No capacities are to be computed. Using the information from card 1700 and the information provided by the wave equation solution, solve for the ultimate resistance to failure as predicted by several popular pile driving equations.
CARD 102 (H	Required)	Y1 1'0' 1'
ID3 ID4		Identification. Ídentification.
RUT		The total static soil resistance act- ing on the pile (kip).
RUP		The total static soil resistance act- ing beneath the point (kip).
MO		Number of first element upor which soil resistance acts.
QSIDE	_	Soil quake along side of pile, if a single value exists. If not, set $QSIDE=0.0$ (in.).
QPOINT		Soil quake beneath pile point (in.)
SIDEJ		Soil damping factor in shear along the side of the pile if a single value exists. If not, set $SIDEJ=0.0$ (sec/ft).
		PAGE THIRTY-NINE

- POINTJ Soil damping factor in compression beneath the pile point (sec/ ft). NUMR – Number of elements for which the
 - 2. Number of elements for which the soil spring does not have a linear stress-strain curve.
- IPRINT Print frequency. For example, if the solution at every 5th time interval is wanted, set IPRINT=5.
- AREA A constant used to convert the forces into stresses or other more convenient values (such as changing lb. to kip by setting AREA = 1000.0).
- NS1-NS6 The element numbers for which solutions vs time interval will be printed. Maximum values and other information are always printed for each element after NSTOP time intervals have elapsed.

CARDS 103-106 (Required only if NOP(1) = 2,3,4,5)

If NOP(1)=1, no identification card will be read. If NOP(1)=2, read card 103 containing 72 columns of alphabetic or numeric identification and print this information above the problem. If NOP(1)=3, read and print two identification cards, up to a maximum of four cards (NOP(1)=5).

- 200 CARD SERIES (Required)
 - IDW1, IDW2 Throughout this Input, variables beginning with the letters "ID" are for identification, in this case to help identify what segment weights are being used.

WAM(I)

weights are being used.
The weight of element number I (kip). a) If NOP(2) = 1, the computer will read MP s egment is eights, ten segment weights to a card from cards 201-230, up to a maximum of 300 segments. For example, if the system is divided into 37 segments, four 200 series cards must be included in the data: 201 through 204. b) If NOP(2) = 2, in this case the pile must have a constant weight per foot along its length. Since the pile is usually divided into equal segment lengths, only a few of the element weights are different. Therefore, only the top five weights (the ram, anvil, ...) and the bottom five weights (..., pile segment, pile point) must be read from the card 200. The computer then sets all other element weights equal to the sixth value punched in the card.

300 CARD SERIES (Required) IDK1. IDK2 — Identification.

IDK1, IDK2 — XKAM(I) —

The internal spring rate of spring I (kip/in.).

a) If NOP(3) = 1, the computer reads MP-1 spring rates from cards 301-330. b) If NOP(2) = 2 the first and last

b) If NOP(3)=2, the first and last five XKAM(I) are read from card 300, and the remaining XKAM(I) are set equal to the sixth XKAM(I) value, i.e., XKAM (MP-4).

400 CARD SERIES (Required if NOP(4) = 1)

IDRL1, IDRL2 — Identification.

RUM(I) -- The ultimate static resistance of the soil acting on pile segment I (kip). a) If NOP(4)=1, read MP ultimate soil resistances, from cards 401-430, and set RUM(MP +1) equal to RUP. b) If NOP(4)=2, set all side friction=0.0 and set RUM(MP+1) = RUP.

c) If NOP(4) =3, distribute (RUT-RUP) uniformly along the pile starting from segment number MO to number MP, and set RUM(MP +1) = RUP.

d) If NOP(4) =4, distribute (RUT-RUP) triangularly between MO and MP set RUM(MP+1)=RUP.
e) If NOP(4)=5, read NUMR cards, each of which can define a linear or nonlinear force-displacement curve for the soil (see card series 450).

450 CARD SERIES (Required if NOP(4) = 5)

When NOP(4) =5, the soil resistance vs displacement curve is nonlinear. This requires ten soil resistances to be read for each soil spring, one for each displacement corresponding to a multiple of Q/10. As shown on data card 451, I is the number of the element upon which the nonlinear resistance is acting, XKIM(I) is the unloading spring rate (kip/in.), and R(I,J) are the soil resistances (kip) at each of the displacements Q/10, 2Q/10, . . . , 9Q/10, Q. Whenever NOP(4)=5, one 450 series card is required for each element upon which soil resistance acts.

- 500 CARD SERIES (Required when NOP(5) = 2)
 - IDG1, IDG2 Identification.
 - GAMMA(I) The minimum force possible in spring I after a peak compressive force has passed, except that any negative GAMMA(I) is construed to mean that that spring can transmit a tensile force of any magnitude (kip).
- 600 CARD SERIES (Required when NOP(6)=2)
 IDE1, IDE2 Identification.
 EEM(I) The coefficient of restitution for MP-1 internal springs. This determines the slope of the unloading curve (dimensionless).
- 700 CARD SERIES (Required when NOP(7)=2)IDB1, IDB2— Identification.BEEM(1)— The damping coefficient of the
MP-1 internal springs (in. sec/ft).
- 800 CARD SERIES (Required when NOP(8)=2) IDV1, IDV2 — Identification. VEL(I) — The initial velocities of each of the MP weights (ft/sec).
- 900 CARD SERIES (Required when NOP(9)=2) IDQ1, IDQ2 — Identification. Q(I) — The soil "quake" for MP+1 soil
- springs (in.). 1000 CARD SERIES (Required when NOP(10)=2)
- IDJ1, IDJ2 Identification. SJ(I) — The soil damping factor for MP+1 soil spring (sec/ft).
- 1100 CARD SERIES (Required when NOP(11)=2) IDDK1, IDDK2 — Identification. DYNAMK(I) — The dynamic spring rate of MP-1 internal springs (kip/in.).
 1200 CARD SERIES (Required when NOP(12)=2) IDA1, IDA2 — Identification. A(I) — The cross-sectional area of each of
 - The cross-sectional area of each of the MP-1 internal springs (in.²).
- 1300 CARD SERIES (Required when NOP(13) = 2)
- FORCIN(INTV) The force acting on the head of the pile (kip) at time interval INTV, for NSTOP intervals with a maximum NSTOP equal to 100 time intervals.

PAGE FORTY

1400 CARD SERI	ES (Required when $NOP(14) = 2$)
CARD 1400	— Header Card.
APILE	- The area of the head of the pile $(in.^2)$.
EMODUL	- The modulus of elasticity of the pile (kip/in. ²).
RGAGE	- The strain gage resistance (ohm).
RCAL	- Calibration resistance (ohm).
ACTIVG	- Number of active gages.
GFACTR	— Gage factor for the gages used.
D1	 Displacement of the galvanometer trace when RCAL is thrown into the bridge at the head of the pile (in.).
D2 Through	
D5	- Galvo displacements corresponding to RCAL at any other four strain gage points (in.).

CARDS 1401 UP TO 1410

The galvanometer deflection for the gage at the head of the pile, at interval number INTV (in.). DGALVI(INTV)

CARD 1500 (Required when NOP(15) = 4)

- Forces known to lie on the true dynamic force vs compression curve of the cushion (kip). F1 and F2
- The cushion compressions corre-sponding to F1 and F2, respective-C1 and C2 ly (in.).

CARD 1600 (Required when NOP(16) = 2) NOPP(I)

When a number of cases are to be solved for which only a few parameters will change, NOPP(I) designates which parameter to vary and how many different values it should be assigned. For example: NOPP(1) =5 indicates that five problems are to be solved, for which only the ram's initial velocity will vary. Each NOPP(I) controls a single variable as shown in Table A.1. Table A.1.

- DV1 Through DK1
- These parameters control the per-cent change in the variables men-tioned above. For example, assume

that the effects of ram velocities of 10, 12, 14, 16, 18, and 20 ft/sec are being studied. The value of DV1 would be (12 ft/sec - 10 ft/sec)

10 ft/secor DV1=0.20. In this case, NOPP (1) would equal 6 since 6 separate The variables controlled by DV1 to DK1 are also listed in Table A.1.

TABLE A.1. LIST OF PARAMETER VARIATIONS AND THEIR CONTROLLING OPTIONS

Controlling Option	Per Cent Increase in Original Value	Parameter Controlled
NOPP(1)	DV1	VELMI (Initial ram velocity)
NOPP(2)	DW1	W(1)
NOPP(3)	DW2	$\hat{\mathbf{W}}(\hat{2})$
NOPP(4)	DW1	$W(\overline{3})$ through $W(MP)$
NOPP(5)	DK1	XKAM(1)
NOPP(6)	DK2	XKAM(2)
NOPP(7)	DKI	XKAM(3) through
,		XKAM(MP-1)
NOPP(8)	DQI	QSIDE
NOPP(9)	DŐP	QPOINT
• NOPP(10)	DJI .	SIDEJ
NOPP(11)	DJP	POINTJ
NOPP(12)	DRI	RUT
NOPP(13)	DRP	RUP
NOPP(14)	DRI	RUT & RUP
NOPP(15)	DE1	EEM(1)
NOPP(16)	DE2	EEM(2)

CARD 1700 (Required when NOP(17) = 2)

0111113 2100	(accounted when not (if) and)
AREAP	Cross-sectional area of pile (in. ²).
XLONG	Length of pile (ft).
ELAST	Modulus of elasticity of pile $(kip/in.^2)$.
CENR	Value for use in ENR pile driving formula.
\mathbf{QAVG}	Average ground "Quake" (in.).
WRAM	Ram weight (kip).
WPILE	Pile weight (kip).
ENERGY	Actual energy output of the ram (ft lb).

Introduction

The following example problem is given to illustrate the steps necessary to arrive at a solution. In the previous chapters, the functional components involved were discussed separately; for example, the driving hammer, pile, soil properties, etc. However, the input data is more easily handled by grouping according to similar physical quantities rather than functional quantities. For example, one series of cards is used to input all segment weights, another for the spring rates. The order in which the input data is set up for the example problems is by no means unique, but it probably should be followed until the programmer becomes familiar with the operations involved.

It should be noted that any variable without a decimal point (such as MP, MH, NR, NSTOP, and NOP(I) on card 101) is always an integer and must be entered as far to the right in its field as possible. Also, the decimal point does not have to be punched for any variable which has a decimal place already shown on the data sheet unless it is desired to change its position. For example, if the initial ram velocity (IVEL on card 101) is 13.48 ft/sec, the numbers 1, 3, 4, and 8 should be punched in columns 19 through 22, respectively. However, to enter a velocity of 127 ft/sec into IVEL, punch 1, 2, and 7 in columns 19, 20, and 21, and punch a decimal point in column 22.

Except for this last case, decimal points need never be punched.

Example Problem

Since case BLTP-6; 57.9 (from the Michigan Pile Study) was one of the problems most often used in this report, the input data required for its solution will be determined first. Figures 3.3 and 3.4 show the real system and the idealized system.

- A. Given Information—Case BLTP-6; 57.9
 1. Hammer Data-Vulcan #1

 a. Manufacturer's Rated Energy = 15,000 ft lb, normal stroke = 3 ft.
 - b. Ram Weight = 5,000 lb, velocity at impact not measured.
 - Driving Cap Weight = 1,000 lb.
 - d. Cushion Data = Oak block, $6-\frac{1}{4}$ in. deep by 11-1/4 in. in diameter, direction of grain unknown, condition of cushion unknown (somewhere between new and "crushed and badly burnt").
 - 2. Pile Data-CBP 124 H-section
 - a. Area = 15.58 in.^2 .
 - Weight = 53 lb/ft. b.
 - Total Length = 72.5 ft. c.
 - d. Driven Length = 57.9 ft.
 - e. Modulus of Elasticity = 30×10^6 .
 - 3. Soil Data
 - a. Ultimate Soil Resistance = 300 kip (static value from load test after soil "set-up").
 - b. From driving log, 75 percent of the soil resistance is assumed point bearing and 25 percent side resistance.

- c. Soil damping factor "J" and soil quake "Q"-not known.
- 4. Miscellaneous Data
 - a. Load Cell Weight = 580 lb.
- b. Additional Helmet Weight = 1,080 lb. B. Input Data Calculations
- Card 101
 - 1. ID1-Identification Tag, use BLTP-6
 - 2. ID2-Identification Tag, use 57.9.
 - 3. Segment Lengths Although segment lengths of 10 ft are usually satisfactory, a 5 ft length will be used to increase the accuracy of the solution.
 - Time Interval—The normal time interval 4. of 1/4000 to 1/5000 iterations/sec must be halved since the normal segment length of 10 ft was reduced by half. Therefore, use $\Delta t = 1/10,000$ sec or $1/\Delta t = 10,000$.
 - 5. MP—The total number of segments as shown in Figure 3.4 is 3 above the pile plus 14 pile segments. Thus, MP = 17.
 - 6. Since the ram velocity at impact was not recorded, the following ram velocities will be studied: IVEL = 8, 12, 16, and 20 ft/sec.
 - 7. MH—The first pile segment weight = 4.
 - 8. NR—Number of divisions of the ram = 1.
 - 9. EEMI-Coefficient of restitution of cushion = 0.4, EEM2—coefficient of restitution of load cell = 1.0.
 - 10. Since springs 1, 2, and 3 cannot transmit tensile forces, GAMMA(1), (2), and (3) are 0.0. The remaining GAMMA (I) are set equal to -1.0. This is done by setting GAMMA1 = GAMMA2 = 0.0 and designating NOP(5) = 3 so that GAMMA(3)will also be set = 0.0.
 - 11. To allow the wave time to make two complete passes up and down the pile, NSTOP is set = 173 iterations. This is found from the velocity of travel of the stress wave and the value of Δt .

$$V_{\text{wave}} = \sqrt{E/p} = \sqrt{\frac{30,000,000}{(0.283/386)}}$$

202,000 ips or 909 000

$$V_{wave} = \frac{202,000}{12} = 16,800 \text{ ft/sec.}$$

Total distance wave must travel = 4(72.5)= 290 ft.

Total time required $=\frac{290 \text{ ft}}{16,800 \text{ ft/sec}} = .0173$

sec.

$$NSTOP = \frac{Total time}{\Delta t}$$

 $\frac{1}{(1/10,000)} = 173$ iterations. Therefore, use NSTOP = 173 iterations. 12. Option Calculations-NOP(I)

- a. NOP(1)—No header cards to be read in and printed out, so NOP(1) = 1.
- b. NOP(2)—Read segment weights from card series 200 (long form), so NOP(2) = 1.
- NOP(3)—Read spring constants from card series 300 (long form), so NOP(3) = 1.
- d. NOP(4)—Assume triangular soil distribution along the side of the pile, so NOP(4) = 4.
- e. NOP(5)—Since GAMMA(3) is to be set equal to 0.0, NOP(5) = 3.
- f. NOP(6)—Since all the internal springs are considered perfectly elastic, except for the first one or two for which values of "c" are given by EEM1 and EEM2, set NOP(6) = 1 (short form, no series 600 cards).
- g. NOP(7)—Assume zero internal damping in the steel pile, thus set NOP(7) = 1 and do not include the 700 card series.
- h. NOP(8)—Only the ram has an initial velocity, so NOP(8) = 1, no 800 card series.
- i. NOP(9) and NOP(10)—Since more exact soils information is not available, Smith's recommended values for Q and J will be used and input on card 102 (short form). Thus, NOP(9) = = NOP(10) = 1.
- j. NOP(11)—No damping, set NOP(11) = 1.
- k. NOP(12)—Use a single factor to change force to stress for all springs— NOP(12) = 1.
- NOP(13)—Use the damping procedure illustrated in Figure 5.13(a), so NOP (13) = 1.
- m. NOP(14)—Calculate the force at the pile head from the action of the ram so NOP(14) = 1.
- n. NOP(15)—Neglect gravity effects— NOP(15) = 1.
- o. NOP(16)—Since several parameters are to be varied, set NOP(16) = 2, thus card 1600 must be included in the data.
- p. NOP(17)—Do not calculate driving resistance predicted by pile driving equations. NOP(17) = 1.
- Card 102
- 1. ID3-Identification Tag, use 12H53.
- 2. ID4—Identification Tag, use L = 72.
- 3. RUT—Since the Michigan Report noted a soil "set-up" of about 2.0, the static resistance actually encountered during driving was probably around half of the measured 400 kip, so RUT = 200 kip.
- 4. RUP—Assuming 75 percent of the total soil resistance at the point, RUP = 150 kip.

5. MO—Since the length of pile in the ground was 57.9 ft, the first segment upon which soil resistance acts is given by:

$$MO = MP + 1 - \left(\frac{\text{Depth Driven}}{\text{Segment Length}}\right)$$
$$= 17 + 1 - \frac{57.9}{5.0}$$
$$= 18 - 11.6$$
$$= 18 - 12$$
so MO = 6

- 6. QSIDE and QPOINT—Smith's recommended value of 0.1 in. will be used due to lack of better soils data.
- 7. SIDEJ and POINTJ—For the same reasons above for values of Q, use SIDEJ = 0.05 sec/ft and POINTJ = 0.15 sec/ft.
- 8. NUMR—Since the soil springs all act as shown in Figure 6.1(a), NUMR = 0.
- 9. Set IPRINT = 5 to print out the solution at every 5th iteration.
- 10. AREA—A single factor will be used to change all forces from lb to kip, thus AREA = 1000.0.
- 11. NS1 through NS6—In this case, the solutions for segments 1, 2, 3, 4, 11, and 17 are desired and, therefore, NS1 through NS6 are given these values.
- Cards 201-202

Segment Weights—As shown in Figure 3.4, several weights normally present during driving have been added between the pile and the driving cap to obtain experimental data.

- a. W(1) = ram weight = 5.0 kip.
- b. $W(2) = driving cap weight + \frac{1}{2} of$ the load cell weight = 1.29 kip.
- c. $W(3) = \frac{1}{2}$ load cell weight + helmet = 1.37 kip.
- d. W(4) through W(17) = pile segment weights = (53 lb/ft) (5 ft) = 0.265 kip.
- Cards 301-302

Segment Stiffness

- a. Because of the lack of data concerning cushion stiffness, several values of K(1) will be run: K(1) 500, 1,000, and 1,500 kip. in.
- b. The helmet was found to be extremely stiff compared to the load cell, so K(2)was taken as the stiffness of the load cell alone. From dimensions of the load cell given in the Michigan Report and using K = AE/L, the spring rate of the load cell was found to be 86,500 kip/in.
- c. The spring rate of each 5 ft pile segment is found by:

$$K = \frac{AE}{L} = \frac{(15.58) (30x10^3)}{5x12}$$

$$=$$
 7,790 kip/in.

So K(3) through K(16) = 7,790 kip/in.

PAGE FORTY-THREE

Card 1600

- 1. Parameter Options—NOPP(I)—Note that all values of NOPP(I) are set = 1 except when an option is used to vary its assigned parameter, in which case NOPP(I) can equal 2 through 9.
 - a. Since IVEL is to be given the four values of 8, 12, 16, and 20 ft/sec, NOPP(1) = 4.
 - b. NOPP(2) through NOPP(4) = 1 since no segment weights are to be varied.
 - c. NOPP(5) = 3 since three different cushion stiffnesses are to be used (K(1) = 500, 1,000, and 1,500 kip/in.)
 - d. NOPP(6) through NOPP(7)-1 since no other parameter changes are required.

2. Parameter Change Constants-DV1, DE1, DE2, etc. These values specify the desired increase in a given parameter based on the parameter's original value. They may be calculated from the equation:

 $Constant = \frac{Second Vaue - Initial Value}{Initial Value}$

Thus, since the initial value of IVEL is 8 ft/sec and the second value is 12 ft/sec

$$DV1 = \frac{12 - 8}{8} = \frac{4}{8} = 1.0$$

The value for DK1 is therefore given by

$$DK1 = \frac{1000 - 500}{500} = \frac{500}{500} = 1.0$$

All other values such as DW1, DW2, etc., may be left blank or given any value for later use since they are not used as long as the corresponding NOPP(I) = 1.

Appendix C PROGRAM LISTING

\$EXECUTE IBJOB		
\$IBJOB		
SIBFTC MAIN	OF APPROXIMATELY 1200 LINES OUTPUT	
	50 +2+MP +NSTOP/IPRINT (UNLESS J5 CH	
	GRAM IS ABOUT 1 MINUTE	TANGES /
	PROBLEM IS ABOUT = (MP*NSTOP)/60,00	O (MINUTES)
•	DENTIFICATION CARDS (SERIES 103)	
	IDENTIFICATION CARD 103 (72 COLS OF	ALPHAMERIC POOP)
	2 IDENTIFICATION CARDS	
• • • •	UP TO 4 CARDS	
C NOP(2) = 0		
	EW WAM(I), I=1, MP	
· · · · · ·	CARD 200 MAXIMUM DIFFERENT WAM(I) =	TEN
C NOP(3) = 0	The selected to the the	
	EW XKAM(I),I=1,N	- TEM
· · · ·	CARD 300 MAXIMUM DIFFERENT XKAM(I) = D SOIL RESISTANCE VALUES, STANDARD OF	
· · · · · ·	EW STANDARD RUM(I), I=1, MPP	GENERAL METHOD
•	IDE RESISTANCE, SET RUM(MPP) = RUT	
	IDE RESISTANCE, SET RUM(MPP) = RUP	
	M SIDE RESISTANCE(RUT-RUP) WITH RUM(MPP) = RUP
	ULAR SIDE RESISTANCE(RUT-RUP) WITH R	
	UMR CARDS AND USE GENERAL SOIL BEHAV	IOR ROUTINE
C NOP(5) = 0,USE OL		
	GAMMA(NR)=GAMMA1 AND GAMMA(NR+1)=GAM	IMA2 (SOP)
	OP ABOVE AND SET GAMMA(NR+2) = 0.0	
	OP ABOVE AND SET GAMMAS(NR+2) AND (N	(R+3) = 0.0
C = 4, ETC.	ONO FORM THRUT	
	ONG FORM INPUT T NOP(5) IS USED TO SET ADDITIONAL O	$\Delta MMA(T)S = 0.0$
		MRRM 113 = 0.0
	ORT FORM INPUT	
	ONG FORM INPUT	
	LD BEEM(I), I=1,N	

c

it.

PAGE FORTY-SEVEN

С = 1, USE SHORT FORM INPUT = 2, USE LONG FORM INPUT NOP(8) = 0, USE OLD VEL(I), I=1, MPС С = 1, USE SHORT FORM INPUT С = 2, USE LONG FORM INPUT NOP(9) = 0, USE OLD Q(1), I=1, MPP С С = 1, USE SHORT FORM INPUT = 2, USE LONG FORM INPUT C NOP(10) = 0,USE OLD SJ(I), I=1,MPP С = 1, USE SHORT FORM INPUT С = 2, USE LONG FORM INPUT C NOP(11) = 0,USE OLD DYNAMK(I), I=1,N С = 1.DYNAMK=0.0С = 2, USE LONG FORM INPUT C NOP(12) = 0, USE OLD A(I), I=1,NС = 1, USE SHORT FORM INPUT С = 2, USE LONG FORM INPUT C NOP(13) = 0,1, USE SMITHS EEM ROUTINE = 2, USE LINEAR SOLID DAMPING С C NOP(14) = 0,1, USE FOM(MI) COMPUTED FROM RAMS BEHAVIOR = 2, READ NSTOP VALUES OF FORCIN(INTV) (CARD SERIES 1300) С = 3.READ HEADER CARD + NSTOP GALVO DEFLECTIONS(IN.) CARDS 1400 С = 4,READ CARD 1500 AND USE PARABOLIC FOM(1) VS. CEEM(1) С C NOP(15) = 1,NO GRAVITY = 2, GRAVITY WITH DEM(I, 0) = 0.0C С = 3, GRAVITY WITH DEM(I, 0) BY SMITH С = 4, GRAVITY WITH DEM(1,0) BY EXACT = 5, GRAVITY WITH DEM(I, 0) AS USED FOR PREVIOUS PROBLEM С NOP(16) = 0.1, NO PARAMETER CHANGES= 2+ READ CARD 1600 WITH PARAMETER CHANGES С NOP(17) =0,1,NO PILE DRIVING FORMULA OUTPUT С С = 2, READ CARD 1700 WITH PILE DRIVING CONSTANTS С C C NUMBER OF CASES = NOPP(1) * NOPP(2) * ... * NOPP(14)

```
С
  NOPP(1) = 1.RAM VELOCITY = VELMI
С
          = 2,RAM VELOCITY=VELMI,(1.0+DV1)*VELMI
С
           = 3,RAM VELOCITY=VELMI,(1.0+DV1)*VELMI,(1.0+2.*DV1)*VELMI
С
          = 4.ETC.
C \text{ NOPP(2)} = WAM(1) CHANGE
C \text{ NOPP(3)} = WAM(2) \text{ CHANGES}
C \text{ NOPP}(4) = WAM(3, MP) CHANGES
C \text{ NOPP}(5) = XKAM(1) CHANGES
C \text{ NOPP(6)} = XKAM(2) CHANGES
C \text{ NOPP}(7) = XKAM(3,N) CHANGES
C \text{ NOPP } 8) = QSIDE CHANGES
C \text{ NOPP}(9) = QPOINT CHANGES
C NOPP(10) = SIDEJ CHANGES
C \text{ NOPP(11)} = POINTJ CHANGES
C \text{ NOPP(12)} = RUM(1, MP) CHANGES
C \text{ NOPP(13)} = RUM(MPP) CHANGES
C NOPP(14) = BOTH RUM(1, MP) AND RUM(MPP) CHANGE
C \text{ NOPP(15)} = EEM(1) \text{ CHANGES}
C \text{ NOPP(16)} = EEM(2) \text{ CHANGES}
С
С
С
                                                        BEEM(100),
      COMMON
                 WAM(100), XKAM(100), RUM(100),
                                                                      EEM(100)
               GAMMA(100), XKIM(100), CEEMAS(100), NFOM(100), XDEM(100)
      COMMON
                                                       FOM(100), XFOM(100)
                 DEM(100), XCEEM(100), CEEM(100),
      COMMON
                                           RAM(100), RMAX(100), RSTAT(100)
                              DIM(100),
      COMMON
                 VEL(100),
                                              Q(100),FORCIN(100),
                                                                     DFOM(100)
      COMMON R(100,10) , ITRIG(100),
      COMMON FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100),
                                                                        A(100)
              DEMAX(100), IDEMAX(100), SJ(100), NOP( 22), DYNAMK(100)
      COMMON
      COMMON CEEMIN(100), HOLDEM(100), ANSVEC( 50), SE(50, 51) , IROW( 51)
                RUMA(100), WAMC(100), XKAMC(100),
                                                        QA(100),
                                                                      SJA(100)
      COMMON
                ICOL( 51), NOPP( 20), ENTHRU(100), ENTMAX(100),
                                                                                      10
                                                                      IDS( 50)
      COMMON
                                                                                      50
      COMMON QSIDE , QPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP
      COMMON INTV , ISECTN, NUMR , F1 , F2
                                                                 • C2
                                                                                      51
                                                        , C1
```

1

2

3

4

5

6

7

8 9

PAGE FORTY-NINE

PAGE FIFTY

COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT 52 COMMON INTT , I , ITST , IX , NR • MO , MP 53 COMMON NPAGE , N , QUAKE , RUP , RUT , VELMI , ID1 54 COMMON ID2 , ID3 • ID4 , IDW1 , IDW2 , IDK1 , IDK2 55 COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 , IDB1 56 COMMON IDB2 , IDV1 , IDV2 , IDQ2 , IDQ1 , IDJ1 , IDJ2 57 COMMON IDDK1 , IDDK2 , IDA1 , IDA2 , KGRADD, J5 , TMIN 58 COMMON TMAX , SMIN , SMAX , NOPNTS, AREA , NS1 , NS2,NS6 59 • NS4 COMMON NS3 , NS5 , IDEEM , MH , VEL1 , ACCELR 60 • C COMMON B , AREAP , XLONG , ELAST , ACELMX 61 COMMON DV1, DE1, DE2, DRI, DRP, DQI, DQP, DJI, DJP, DW1, DW2, DWI, DK1, DK2, DKI NPAGE =0**9 CONTINUE** NS1 = 0CALL INPUT MP = MPMO = MONR = NRMH=MH N = MP - 1MPP = MP+1INITIALIZE PARAMETER CONSTANTS DELTAA = DELTEEWAMA = WAM(1)WAMB = WAM(2)XKAMA = XKAM(1) $XKAMB = XKAM{2}$ DO 1 I=1,MPRUMA(I) = RUM(I)WAMC(I) = WAM(I)XKAMC(I) = XKAM(I)

É

0000

С

	QA(I) = Q(I)
	SJA(I) = SJ(I)
1	
	NOPA = NOPP(1)
	NOPB = NOPP(2)
	NOPC = NOPP(3)
	NOPD = NOPP(4)
	NOPE = NOPP(5)
	NOPF = NOPP(6)
	NOPG = NOPP(7)
	NOPH = NOPP(8)
	NOPI = NOPP(9)
	NOPJ = NOPP(10)
	NOPK = NOPP(11)
	NOPL = NOPP(12)
	NOPM = NOPP(13)
	NOPN = NOPP(14)
	NOPO = NOPP(15)
	NOPQ = NOPP(16)
	DO 98 IQ = $1,NOPQ$
	DO 98 IO = 1, NOPO
11	DO 98 IN = $1, NOPN$
	IM = IN
	IL = IN
	DO 98 IK = 1,NOPK
	DO 98 IJ = $1, NOPJ$
	DO 98 II = 1,NOPI
	DO 98 IH = $1, NOPH$
	DO 98 IG = $1, NOPG$
	DO 98 IF = $1, NOPF$
	DO 98 IE = $1, NOPE$
	DO 98 $ID = 1, NOPD$
	DO 98 IC = $1, NOPC$
	DO 98 IB = $1, NOPB$

BEGIN PARAMETER VARIATIONS

ء ° د

DEGIN PARAMETER VARIATIONS

PAGE FIFTY-ONE

C

```
DO 98 IA = 1,NOPA
      DELTEE = DELTAA
      DO 4 1=1.MP
      VEL(I) = 0.0
      WAM(I) = WAMC(I)
                            *(1.0 + FLOAT(ID-1) * DWI)
      XKAM(I) = XKAMC(I)
                            *(1.0 + FLOAT(IG-1) * DKI)
      Q(I) = QA(I)
                            *(1.0 + FLOAT(IH-1) * DQI)
      SJ(I) = SJA(I)
                            *(1.0 + FLOAT(IJ-1) + DJI)
      RUM(I) = RUMA(I)
                            *(1.0 + FLOAT(IL-1) * DRI)
    4 CONTINUE
      DO 3 I=1.NR
      VEL(I) = VELMI
                            +(1.0 + FLOAT(IA-1) + DV1)
    3 CONTINUE
      VEL1 = VEL(1)
      WAM(1) = WAMA
                            *(1.0 + FLOAT(IB-I) * DW1)
      WAM(2) = WAMB
                            *(1.0 + FLOAT(IC-1) * DW2)
      XKAM(1) = XKAMA
                            *(1.0 + FLOAT(IE-1) * DK1)
                            *(1.0 + FLOAT(IF-1) + DK2)
      XKAM(2) = XKAMB
      Q(MPP) = QPOINT
                            *(1.0 + FLOAT(II-1) * DQP)
      SJ(MPP) = POINTJ
                            *(1.0 + FLOAT(IK-1) * DJP)
                            *(1.0 + FLOAT(IM-1) * DRP)
      RUM(MPP) = RUP
                            +(1.0 + FLOAT(IO-1) + DE1)
      EEM(NR) = EEM1
      EEM(NR+1) = EEM2
                            *(1.0 + FLOAT(IQ-1) + DE2)
      IF(NOP(4)-5)13, 16, 13
   13 DO 15 I=1, MPP
   15 \times KIM(I) = RUM(I)/Q(I)
   16 CONTINUE
C IF DELTEE IS LEFT BLANK, 1/2 THE CRITICAL TIME INTERVAL WILL BE USED
      IF(DELTEE)32,32,31
   32 DO 33 I=1+N
   33 DELTEE = AMAX1(DELTEE, 39.296+SQRT(XKAM(I)/WAM(I)),
                             39.296*SQRT(XKAM(])/WAM(I+1)))
     1
   31 CONTINUE
                                              END PARAMETER VARIATIONS
С
      C1PC2 = 0.0
```

```
ACELMX = 0.0
   CALL PRINT 1
   CALL REP 1
   J5 = IPRINT
   KXT=1
   INTV = 0
   INTT = 1
   MP = MP
   N = MP-1
   MPP = MP+1
   NOP15P = NOP(15)+1
   GD T0(50,50,49,48,47,43,50,50,50),NUP15P
43 DO 42 I = 1, MP
42 DEM(I) = HOLDEM(I)
44 RAM(MP) = DEM(MP) + XKIM(MP)
   RAM(MP+1) = DEM(MP) * XKIM(MP+1)
   HOLDEM(MP) = DEM(MP)
   HOLDEM(1) = DEM(1)
   CEEM(1) = DEM(1) - DEM(2)
   FOM(1) = CEEM(1) * XKAM(1)
   DO 45 I = 2_{1}N
  HOLDEM(I) = DEM(I)
   CEEM(I) = DEM(I) - DEM(I+1)
   FOM(I) = CEEM(I) * XKAM(I)
45 \text{ RAM(I)} = FOM(I-1) - FOM(I) + WAM(I)
   GO TO 49
47 CALL EXACTG
   GO TO 49
48 CALL SMITH
49 CONTINUE
   WRITE(6,8002)(DEM(I),I=1,MP)
   WRITE(6,8001)(DIM(I),I=1,MP)
   WRITE(6,8003)(FOM(I),I=1,MP)
   WRITE(6,8004)(CEEM(I),I=1,N)
   WRITE(6,8005)(RAM(I),I=1,MPP)
```

PAGE FIFTY-THREE

```
WRITE(6,8006)(XKIM(I),I=1,MPP)
50 CONTINUE
   NSM = MP-1
   NSM=MINO(NS6,NSM)
   WRITE(6,1104)NS1,NS2,NS3,NS4,NS5,NSM,NS1,NS2,NS3,NS4,NS5,NS6,MPP
                                                   BEGIN ITERATION LOOP
12 CALL REP N
   INTT=INTT
   GO TO(22,9 ), INTT
22 CONTINUE
   CMAX = 0.0
   DO 24 I=NR.N
24 \text{ CMAX} = \text{CMAX+CEEM(I)}
   C1PC2 = AMAX1(C1PC2,CMAX)
   IF(INTV-999)25,23,25
23 J5 = 25
25 CONTINUE
   IF(((INTV/J5)*J5)-INTV)94,26,94
26 CONTINUE
27 \text{ FOMA} = \text{FOM}(\text{NS1})/\text{A}(\text{NS1})
   FOMB = FOM(NS2)/A(NS2)
   FOMC = FOM(NS3)/A(NS3)
   FOMD = FDM(NS4)/A(NS4)
   FOME = FOM(NS5)/A(NS5)
   FOMF = FOM(NSM)/A(NSM)
   RAMP = RAM(MP)/1000.0
   WRITE(6,99)INTV ,FOMA,FOMB,FOMC,FOMD,FOME, CEEM(1),DEM(NS3),
  1 DEM(NS4), DEM(NS5), DEM(NS5P), (ENTHRU(I), I=2,4), ENTHRU(N), ACCELR
   WRITE(6,99) INTV, FOMA, FOMB, FOMC, FOMD, FOME, FOMF, DEM(NS1), DEM(NS2),
  1DEM(NS3), DEM(NS4), DEM(NS5), DEM(NS6), RAMP
94 CONTINUE
   IF(INTV-NSTOP )12,14,14
14 WRITE(6,105)
   MP = MP
   N = MP - 1
```

С C

С

```
MH = MH
      D020I=1,N
      FOMAX(I) = FOMAX(I)/A(I)
      FOMIN(I) = FOMIN(I)/A(I)
      WRITE(6,106)I, IFOMAX(I), FOMAX(I), IFOMIN(I), FOMIN(I),
                  ENTHRU(I), ENTMAX(I)
     1
   20 CONTINUE
С
      BLOWS = 1.0/DIM(MP)
                                         OLD STATEMENT
С
      WRITE(6,2107)DIM(MP),BLOWS
                                        OLD STATEMENT
      WRITE(6,2108)DEMAX(MH-1),DEMAX(MP)
      SMIN = SMIN/12.0
      SMAX = SMAX/12.0
      ERES1 = SQRT(SMIN/SMAX)
      WRITE(6,109) SMIN, SMAX, ERES1
      EINPUT = (WAM(1) + VEL1 + 2)/64.4
      WRITE(6,110)EINPUT
      WRITE(6,111)ACELMX
С
                                       BEGIN ULTIMATE LOAD FORMULAS
      IF(NOP(17)-1)98,98,5
    5 CONTINUE
      C4 = 0.1
      AEL = AREAP*ELAST/XLONG
      NRP = NR+1
      C3 = QAVG
      S = DIM(MPP)
      W = WRAM
      U = ENERGY
      P = WPILE
      RWAVE = 0.0
      DO: 6. I=1, MPP
      RWAVE = RWAVE+RUM(I1/1000.0
    6 CONTINUE
      SEGL = XLONG/(FLOAT(MP-MH+1))
      SUMR = 0.0
      DO 10 I=MH, MP
```

PAGE FIFTY-FIVE

```
10 SUMR = SUMR+RUM(I )*SEGL*(FLOAT(I -MH)+0.5)
      SUMR = SUMR+RUM(MPP) *XLONG
      HILEYL = SUMR/RWAVE
      RENEWS = U/(S+CENR)
      REYTEL = U/(S+(C4*P/W))
      RTERZG = AEL*(-S+SQRT(S**2+(2.0*U*(W+P*EEM1**2)/(AEL*(W+P)))))
      REDTEN = AEL + (-S + SQRT(S + 2 + (2.0 + U + W/(AEL + (W + P)))))
      RHILYD =AEL+(-(S+C3)+SQRT((S+C3)++2+(2.0+U+(W+P+EEM1++2)/
     1
              (AEL*(W+P)))))
      RHILYC=U*(W+P*EEM1**2)/((S+0.5*(C1PC2+C3))*(W+P))
     RCDAST = (AEL/2.) * (-S+SQRT(S**2+(4.*U*(W+P*EEM1**2)/(AEL*(W+P)))))
      WRITE(6,107)
      WRITE(6,108)RENEWS, REYTEL, RTERZG, REDTEN, RHILYD, RHILYC, RCDAST, RWAVE
С
                                             END ULTIMATE LOAD FORMULAS
   98 CONTINUE
      GO TO 9
   99 FORMAT(1X,13,6F9.2,6F9.3,F9.1)
C 99 FORMAT(1X, I3, 5F10.2, 5F11.7,F9.1)
  105 FORMAT(1H0,//, 18X, 63HMAXIMUM COMPRESSIVE AND TENSILE STRESSES (
     1PSI) IN THE SEGMENTS
                             ,//,19X, 7HSEGMENT , 1X, 5H TIME ,
     2 3X, 6HSTRESS, 5X, 4HTIME, 3X, 6HSTRESS, 7X, 6HENTHRU, 7X,
     3 10HMAX ENTHRU
                      .
                            11
  106 FORMAT(20X,14,18,F9.1,19,F9.1,2F13.1)
  107 FORMAT( 16X, 30H ULTIMATE PILE LOADS (KIPS)
                                                       . )
                21X,25H BY ENG NEWS FORMULA = , F15.3,/,
  108 FORMAT(
     1
        22X,25H BY EYTELWEIN
                                     = , F15.3,/,
     2
       22X,25H BY TERZAGHI
                                            F15.3,/ ,
                                     =
                                        .
       22X,25H BY REDTENBACHER
     3
                                            F15.3,/ ,
                                     = ,
     4
      22X,25H BY HILEY (DUNHAM)
                                     = , F15.3,/,
     5
      22X,25H BY HILEY (CHELLIS)
                                     = , F15.3,/,
        22X,25H BY PACIFIC COAST
                                     = , F15.3./ ,
     7
        22X, 25H BY THE WAVE EQUATION = , F15.3)
  109 FORMAT(17X,7HSMIN = F10.1, 7HSMAX = F10.1, 10HERES(1) = F10.7)
  110 FORMAT(16X, 18H EINPUT (FT LBS) = F9.1)
  111 FORMAT(16x_{24H} MAX ACCELERATION (GS) = F9.1)
```

```
1104 FORMAT(3H T,6(6X,1HF,12),1X, 6(6X,1HD,12) ,6X,1HR,12,//)
C1104 FORMAT(115H TIME F(1)
                              F(2)
                                      F(3)
                                             F(4)
                                                    F(5)
                                                           D(2)
                                                                 D(3) D(
     14) D(5) D(P) ENT(2) ENT(3) ENT(4) ENT(N) ACC(MH-1)
C
                                                                     )
C1104 FORMAT(5H TIME,5(2X,4HFOM( I3, 1H) ) ,5(3X,4HDEM( I3, 1H) ) ,
C
     1 3X, 12HENTHRU (1)
                             11)
 2107 FORMAT(1H /
                    ,17X,24HPERMANENT SET OF PILE = F13.8,8H INCHES/
         ,17X,27HNUMBER OF BLOWS PER INCH = F13.8)
     1 .
 2108 FORMAT(1H /
                    ,17X,24HLIMSET FOR (MH-1)
                                                   = F13.8.8H
                                                               INCHES/
         ,17X,27HMAX DISPLACEMENT OF POINT= F13.8)
     1
 8001 FORMAT(33HOINITIAL VALUES FOR DIM(I), I=1.MP /(6E19.8))
 8002 FORMAT(33HOINITIAL VALUES FOR DEM(I), I=1, MP /(6E19.8))
 8003 FORMAT(33HOINITIAL VALUES FOR FOM(I), I=1, MP /(6E19.8))
 8004 FORMAT(33HOINITIAL VALUES FOR CEEM(I), I=1, N /(6E19.8))
 8005 FORMAT(35HOINITIAL VALUES FOR RAM(I), I=1, MP+1 /(6E19.8))
 8006 FORMAT(38HOCONSTANT VALUES FOR XKIM(I), I=1, MP+1 /(6E19.8))
      END
SIBFTC INPUTT
      SUBROUTINE INPUT
                WAM(100), XKAM(100),
                                         RUM(100), BEEM(100),
                                                                 EEM(100)
      COMMON
      COMMON
              GAMMA(100).
                           XKIM(100),CEEMAS(100), NFOM(100),
                                                                XDEM(100)
      COMMON
                DEM(100), XCEEM(100), CEEM(100),
                                                     FOM(100).
                                                                XFOM(100)
                VEL(100),
                            DIM(100),
                                         RAM(100), RMAX(100), RSTAT(100)
      COMMON
      COMMON R(100,10) , ITRIG(100),
                                           Q(100), FORCIN(100),
                                                                DFOM(100)
      COMMON
              FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100),
                                                                   A(100)
      COMMON
              DEMAX(100), IDEMAX(100),
                                          SJ(100),
                                                     NOP( 22), DYNAMK(100)
      COMMON CEEMIN(100), HOLDEM(100), ANSVEC( 50), SE(50,51) ,
                                                                IROW( 51)
                                                      QA(100),
      COMMON
               RUMA(100), WAMC(100), XKAMC(100),
                                                                 SJA(100)
               ICOL( 51), NOPP( 20), ENTHRU(100), ENTMAX(100),
                                                                 IDS( 50)
      COMMON
      COMMON OSIDE , OPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP
      COMMON INTV , ISECTN, NUMR , F1
                                            • F2
                                                    • C1
                                                            · C2
                                  • EEM2
      COMMON IPRINT, DELTEE, EEM1
                                            , GAMMA1, GAMMA2, INT
                                            • NR
                                                    , MO
                                                            , MP
                           , ITST
                                   , IX
      COMMON INTT
                  • I
      COMMON NPAGE . N
                           , QUAKE , RUP
                                            , RUT
                                                    , VELMI , ID1
                                            , IDW2
                                                    , IDK1 , IDK2
      COMMON ID2
                   • ID3
                           • ID4
                                   , IDW1
      COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1
                                                    , IDE2 , IDB1
```

PAGE

FIFTY-SEVEN

1 2

3

4

5

6

7

8 9

10

50

51

52

53

54

55

56

С

```
COMMON IDB2 , IDV1 , IDV2 , IDQ1 , IDQ2 , IDJ1
                                                               , IDJ2
                                                                                    57
    COMMON IDDK1 , IDDK2 , IDA1
                                    , IDA2 , KGRADD, J5
                                                               , TMIN
                                                                                    58
    COMMON TMAX , SMIN , SMAX
                                    • NOPNTS, AREA , NS1
                                                               , NS2,NS6
                                                                                    59
    COMMON NS3
                   • NS4
                           • NS5
                                    , IDEEM , MH
                                                      , VEL1 , ACCELR
                                                                                    60
    COMMON B
                  • C
                           , AREAP , XLONG , ELAST , ACELMX
                                                                                    61
    COMMON DV1, DE1, DE2, DRI, DRP, DQI, DQP, DJI, DJP, DW1, DW2, DWI, DK1, DK2, DKI
    READ(5,100)ID1,ID2,DELTEE,MP,VELMI,MH,NR,EEM1,EEM2,GAMMA1,
   1 GAMMA2, NSTOP, (NOP(I), I=1, 20)
    READ(5,101)ID3, ID4, RUT, RUP, MO, QSIDE, OPDINT, SIDEJ, PDINTJ, NUMR,
   1 IPRINT, AREA, NS1, NS2, NS3, NS4, NS5, NS6
    RUT = RUT + 1000.0
    RUP = RUP + 1000.0
    NR = MAXO(NR,1)
    N = MP - 1
    MPP = MP+1
    WAM(MPP) = -0.0
    XKAM(MP) = -0.0
  \times XKAM(MPP) = -0.0
    IF(NOP(1)-2)9,7,7
  7 \text{ NOIDS} = 12 + (\text{NOP}(1) - 1)
    READ(5,103)(IDS(I),I=1,NOIDS)
  9 CONTINUE
    IF(NOP(2)-1) 1,1,14
  1 READ(5,102)IDW1,IDW2,(WAM(I),I=1,MP)
    GO TO 2
 14 \text{ NRP1} = \text{NR+1}
    NRP5 = NR+5
    NRP6 = NR+6
    MPM3 = MP-3
    READ(5,111)IDW1, IDW2, WAM(1), (WAM(L), I=NRP1, NRP5),
   1
                (WAM(I).I=MPM3.MP)
111 FORMAT(A5,A4,-3P10F6.4)
    DO 76 I=1.NR
76 WAM(I) = WAM(1)
```

```
DO 77 I=NRP6, MPM3
   77 \text{ WAM(I)} = \text{WAM(NRP5)}
    2 CONTINUE
       IF(NOP(3)-1) 3,3,15
    3 READ(5,104)IDK1,IDK2,(XKAM(I),I=1,N)
       GO TO 4
   15 \text{ NRM1} = \text{NR}-1
      NRP5 = NR+5
      NRP6 = NR+6
      MPM3 = MP-3
      READ(5,112)IDK1,IDK2,XKAM(1),(XKAM(I),I=NR,NRP5),
                   (XKAM(I), I=MPM3, N)
     1
  112 FORMAT(A5, A4, -3P10F6.0)
       DO 78 I=1,NRM1
   78 \times AM(1) = \times AM(1)
      DO 79 I=NRP6, MPM3
   79 \times XKAM(I) = XKAM(MPM3)
    4 CONTINUE
       IF(NOP(4)-1)22,5,5
    5 \text{ NOP4} = \text{NOP}(4)
       DD 6 I=1, MP
    6 RUM(I) = 0.0
       RUM(MPP) = RUP
       GO TO(10,22,11,13,17,22,22,22,22),NOP4
   10 READ(5,106)IDRL1, IDRL2, (RUM(I), I=1, MPP)
C INPUT RUM(I) IN UNITS OF KIPS - THE COMPUTER WILL CONVERT TO LBS.
       GO TO 22
   11 RCONST = (RUT-RUP)/FLOAT(MPP-MO)
       DO 12 I=MO,MP
   12 \text{ RUM}(I) = \text{RCONST}
       GO TO 22
   13 DO 16 I=MO, MP
   16 RUM(I) = (2.0*(RUT-RUP)*(FLOAT(I-MO)+0.5))/(FLOAT(MPP-MO))**2
       GO TO 22
C GENERAL R(I,J) INPUT
```

```
17 DO 20 I=1.MPP
   20 \text{ XKIM(I)} = 0.0
      DO 21 K=1, NUMR
   21 READ(5,115)I, XKIM(I), (R(I,J), J=1,10)
   22 CONTINUE
C THE R(I,J) INPUT CARDS CAN BE IN RANDOM ORDER
C THE R(I, J) ARRAY NEED NOT BE ZEROED SINCE IF XKIM(I)=0 THE GENERAL
C SOIL RESISTANCE ROUTINE FOR SEGMENT(I) IS NOT CONSIDERED
C NUMR = TOTAL NUMBER OF SEGMENTS W/GEN. R (DONT FORGET TO ADD MPP)
CC I = THE SEGMENT NUMBER FOR WHICH R(I, J) VALUES ARE BEING INPUT
C R(L,J) = STATIC RESISTANCE ON SEGMENT I AT EACH OF TEN POINTS J
      IF(NOP(5)-1)29,27,26
   26 IF(NOP(5)-9)24,25,24
   25 READ(5,106)IDG1,IDG2,(GAMMA(I),I=1,N)
      GO TO 29
   24 \text{ IGAMMA} = \text{NOP}(5) + \text{NR} - 1
      DO 23 I=1.N
   23 \text{ GAMMA(I)} = -1000.0
      DO 19 I=NR, IGAMMA
   19 \text{ GAMMA(I)} = 0.0
      GAMMA(NR) = GAMMA1
      GAMMA(NR+1) = GAMMA2
      GO TO 29
   27 DO 28 1=1.N
   28 \text{ GAMMA(I)} = -1000.0
      GAMMA(NR) = GAMMA1
      GAMMA(NR+1) = GAMMA2
   29 \text{ GAMMA(MP)} = -0.0
      GAMMA(MPP) = -0.0
      IF(NOP(6)-1)33,31,30
   30 READ(5,107)IDE1,IDE2,(EEM(I),I=1,N)
      GO TO 33
   31 DO 32 I=1,N
   32 EEM(I) = 1.0
      EEM(NR) = EEM1
```

```
EEM(NR+1) = EEM2
   33 \text{ EEM(MP)} = -0.0
      EEM(MPP) = -0.0
      IF(NOP(7)-1)37,35,34
   34 READ(5,107)IDB1,IDB2,(BEEM(I),I=1,N)
      GO TO 37
   35 DO 36 I=1,N
   36 \text{ BEEM(I)} = 0.0
   37 \text{ BEEM(MP)} = -0.0
      BEEM(MPP) = -0.0
C DO NOT TRY TO USE LAST PROBLEMS VALUES OF VEL(I)
      IF(NOP(8)-1)39,39,38
   38 READ(5,108)IDV1,IDV2,( VEL(I),I=1,MP)
      GO TO 71
   39 DO 40 I=NR, MPP
   40 \text{ VEL(I)} = 0.0
      DO 41 I=1,NR
   41 \text{ VEL}(I) = \text{VELMI}
   71 \text{ VEL(MPP)} = -0.0
      IF(NOP(9)-1)45,43,42
   42 READ(5,107)IDQ1,IDQ2,(Q(I),I=1,MPP)
      GO TO 45
   43 DO 44 I=1, MPP
      Q(I) = QSIDE
   44 CONTINUE
      Q(MPP) = QPOINT
   45 IF(NOP(10)-1)49,47,46
   46 READ(5,107)IDJ1,IDJ2,(SJ(I),I=1,MPP)
       GO TO 49
   47 DO 48 I=1,MP
   48 \text{ SJ(I)} = \text{SIDEJ}
       SJ(MPP) = POINTJ
   49 IF(NOP(11)-1)53,51,50
   50 READ(5,104) IDDK1, IDDK2, (DYNAMK(I), I=1, N)
       DO 72 I=1.N
```

```
PAGE SIXTY-ONE
```

```
72 DYNAMK(I) = DYNAMK(I)-XKAM(I)
      GO TO 53
   51 DO 52 I=1,N
   52 DYNAMK(I) = 0.0
C STATEMENT 52 SETS DYNAMK(I) = 0.0 SO SMITHS ROUTINE WILL BE USED
   53 DYNAMK(MP) = -0.0
      DYNAMK(MPP) = -0.0
      IF(NOP(12)-1)57,55,54
   54 READ(5,109)IDA1,IDA2,(A(I),I=1,N)
      GO TO 57
   55 DO 56 I=1,N
   56 A(I) = AREA
   57 A(MP) = -0.0
      A(MPP) = -0.0
      IF(NOP(4)-1)61,58,58
   58 IF(NOP(4)-5)59,61,61
   59 DO 60 I=1.MPP
   60 \text{ XKIM(I)} = \text{RUM(I)/Q(I)}
   61 CONTINUE
      NOP14 = NOP(14)+1
      GO TO(65,65,62,63,65),NOP14
C READ NSTOP VALUES OF FOM(1,T) - MAXIMUM NSTOP = 300
   62 READ(5,120)(FORCIN(I), I=1, NSTOP)
      GO TO 65
   63 READ(5,122)AREAP, EMODUL, RGAGE, RCAL, ACTIVG, GFACTR, D1, D2, D3, D4, D5
      READ(5,121)(FORCIN(I), I=1, NSTOP)
      CE = (AREAP*EMODUL*RGAGE*1000.0)/(ACTIVG*GFACTR*RCAL)
      A(NS1) = CE/D1
      A(NS2) = CE/D2
      A(NS3) = CE/D3
      A(NS4) = CE/D4
      A(NS5) = CE/D5
      DO 64 I=1, NSTOP
   64 \text{ FORCIN(I)} = \text{FORCIN(I)} * A(1)
```

65 CONTINUE

```
IF(NOP(14)-4)67,66,67
   66 READ(5,123)F1,F2,C1,C2
   67 CONTINUE
      DO 90 I = 1,20
   90 \text{ NOPP(I)} = 1
      IF(NOP(16)-2)69,68,69
   68 READ(5,124)(NOPP(I),I=1,20), DV1, DW1, DW2, DWI, DK1, DK2, DKI, DQI,
     1
         DQP, DJI, DJP, DRI, DRP, DE1, DE2
   69 CONTINUE
      DO 8 I=1,20
      NOPP(I) = MAXO(NOPP(I), 1)
    8 CONTINUE
      IF(NOP(17)-1)74,74,73
   73 READ(5,125)AREAP,XLONG,ELAST,CENR,QAVG,WRAM,WPILE,ENERGY
      XLONG = XLONG + 12.0
   74 CONTINUE
  100 FORMAT(A5,A4,F6.0,I3,F4.2,2[3,2F4.3,2F6.0,I4,2011)
  101 FORMAT(A5,A4,2F7.2,I3,4F4.3,2I3,F6.2,6I3)
  102 FORMAT(A5,A4,-3P10F6.4,/(9X,-3P10F6.4))
  103 FORMAT(12A6)
  104 FORMAT(A5,A4,-3P10F6.0,/(9X,-3P10F6.0))
  106 FORMAT(A5,A4,-3P10F6.1,/(9X,-3P10F6.1))
 107 FORMAT(A5,A4, 10F6.5,/(9X,
                                      10F6.5))
  108 FORMAT(A5,A4,
                      10F6.3,/(9X,
                                      10F6.3)
  109 FORMAT(A5,A4,
                     10F6.2,/(9X,
                                      10F6.2))
  115 FORMAT(13,-3P11F6.1)
  120 FORMAT(-3P10F6.1)
  121 FORMAT( 10F6.4)
  122 FORMAT(F7.2,3F7.0,7F4.2)
  123 FORMAT(-3P2F6.1,0P2F6.5)
  124 FORMAT(2011,17F3.2)
  125 FORMAT(F6.2,F5.2,F7.2)
      RETURN
      END
$IBFTC PRINT
```

```
PAGE SIXTY-THREE
```

.

PAGE SIXTY-FOUR

PRINT 1 IS A SUBROUTINE TO PRINT INPUT DATA.

SUBROUTINE PRINT 1

WAM(100), XKAM(100), RUM(100), BEEM(100), EEM(100)	1
GAMMA(100), XKIM(100), CEEMAS(100), NFOM(100), XDEM(100)	2
DEM(100), XCEEM(100), CEEM(100), FOM(100), XFOM(100)	3
	-
WSIDE, WOUNT, SIDEJ, PUTNIJ, NGDIV, NUKAMS, NSTUP	50
INTV, ISECTN, NUMR, FI, F2, C1, C2	51
IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT	52
INTT, I, ITST, IX, NR, MO, MP	53
NPAGE, N , QUAKE, RUP, RUT, VELMI, ID1	54
ID2 , ID3 , ID4 , IDW1 , IDW2 , IDK1 , IDK2	55
	56
IDB2 • IDV1 • IDV2 • IDQ1 • IDQ2 • IDJ1 • IDJ2	57
IDDK1 . IDDK2 . IDA1 . IDA2 . KGRADD. 15 . TMIN	58
NS3 , NS4 , NS5 , IDEEM , MH , VEL1 , ACCELR	60
B, C, AREAP, XLONG, ELAST, ACELMX	61
DV1,DE1,DE2,DRI,DRP,DQI,DQP,DJI,DJP,DW1,DW2,DWI,DK1,DK2,DKI	
	<pre>WAM(100), XKAM(100), RUM(100), BEEM(100), EEM(100) GAMMA(100), XKIM(100), CEEMAS(100), NFOM(100), XDEM(100) DEM(100), XCEEM(100), CEEM(100), FOM(100), XFOM(100) VEL(100), DIM(100), RAM(100), RMAX(100), RSTAT(100) R(100,10), ITRIG(100), Q(100),FORCIN(100), DFOM(100) FOMAX(100),IFOMAX(100), FOMIN(100), IFOMIN(100), A(100) DEMAX(100),IDEMAX(100), FOMIN(100), NOP(22),DYNAMK(100) CEEMIN(100),HOLDEM(100), ANSVEC(50),SE(50,51), IROW(51) RUMA(100), HOLDEM(100), ANSVEC(50),SE(50,51), IROW(51) RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(100) ICOL(51), NOPP(20),ENTHRU(100),ENTMAX(100), IDS(50) QSIDE, QPOINT, SIDEJ, POINTJ, NQDIV, NORAMS, NSTOP INTV, ISECTN, NUMR, F1, F2, C1, C2 IPRINT, DELTEE, EEM1, EEM2, GAMMA1, GAMMA2, INT INTT, I, ITST, IX, NR, MO, MP NPAGE, N, QUAKE, RUP, RUT, VELMI, ID1 ID2, ID3, ID4, IDW1, IDW2, IDK1, IDK2 IDRL1, IDRL2, IDG1, IDG2, IDE1, IDE2, IDB1 IDB2, IDV1, IDV2, IDQ1, IDQ2, IDJ1, IDJ2 IDDK1, IDDK2, IDA1, IDA2, KGRADD, J5, TMIN TMAX, SMIN, SMAX, NOPNTS, AREA, NS1, NS2,NS6 NS3, NS4, NS5, IDEEM, MH, VEL1, ACCELR B, C, AREAP, XLONG, ELAST, ACELMX DV1, DE1,DE2,DR1,DRP,DQ1,DQP,DJ1,DJP,DW1,DW2,DW1,DK1,DK2,DKI</pre>

С

```
NPAGE = NPAGE+1
WRITE(6+L02)NPAGE
IF(N0P(1)-2)3,2,2
2 NOIDS = 12+(N0P(1)-1)
WRITE(6,101)
WRITE(6,103 )(IDS(I),I=1,N0IDS)
WRITE(6,101)
3 CONTINUE
```

C C

```
MPP=MP+1
  RCT = 0.0
  DO 6 I = 1, MPP
  RCT = RCT+RUM(I)/1000.0
6 CONTINUE
  RCP = RUM(MPP)/1000.0
  WRITE(6,105)DELTEE,NOP(1),NOP(16)
  DELTEE = 1.0/DELTEE
  WRITE(6,106) MP, NOP(2), NOP(17)
  WRITE(6,107)ID1, ID2, VELMI, NOP(3), NOP(18)
  WRITE(6,108) ID3, ID4, NSTOP, NOP(4), NOP(19)
  WRITE(6,110) IDW1, IDW2, RCT, NOP(5), NOP(20)
  WRITE(6,111)IDK1,IDK2,RCP,NOP(6)
  WRITE(6,112)IDRL1, IDRL2, MO, NOP(7)
  WRITE(6,113) IDG1, IDG2, QSIDE, NOP(8)
  WRITE(6,114) IDE1, IDE2, QPOINT, NOP(9)
  WRITE(6,115)IDB1,IDB2,SIDEJ,NOP(10)
  WRITE(6,116)IDV1,IDV2,POINTJ,NOP(11)
  WRITE(6,117) IDQ1, IDQ2, NUMR, NOP(12)
  WRITE(6,118)IDJ1,IDJ2,IPRINT,NOP(13)
  WRITE(6,119)IDDK1,IDDK2,AREA,NOP(14)
  WRITE(6,120) IDA1, IDA2, NR, NOP(15)
  WRITE(6,101)
  WRITE(6,121)
  MPP = MP+1
  LINES = 19
  DO 5 I=1, MPP
  WRITE(6,122)I,WAM(I),XKAM(I),RUM(I),GAMMA(I),EEM(I),BEEM(I),
 1 VEL(I),0(I),
                   SJ(I), DYNAMK(I), A(I)
  LINES = LINES+1
  IF(LINES-58)5,4,4
4 \text{ NPAGE} = \text{NPAGE}
 LINES = 5
  WRITE(6,102)NPAGE
  WRITE(6,101)
```

0

PAGE SIXTY-FIVE

WRITE(6,121) **5 CONTINUE** IF(NOP(4)-5)30,7,30 7 IF(LINES-50)9,9,8 8 NPAGE = NPAGELINES = -1WRITE(6,102)NPAGE GO TO 10 9 WRITE(6,101) 10 WRITE(6,123)(J, J=1,10) LINES = LINES+6LINADD = NQDIV/10IF(NQDIV-LINADD+10)13,14,13 13 LINADD = LINADD+114 LINADD = LINADD+1DO 29 I=1, MPP IF(XKIM(I)-0.0)29,29,20 20 LINES = LINES+LINADD IF(LINES-59)24,24,23 23 NPAGE = NPAGEWRITE(6,102)NPAGE WRITE(6,123)(J,J=1,10) LINES = 624 WRITE(6,124)I, (R(I,J), J=1,10) **29 CONTINUE** WRITE(6,101) LINES = LINES+230 WRITE(6,101) LINES = LINES+2LINADD = MP/8IF(MP-LINADD+8)40,41,40 40 LINADD = LINADD+141 LINADD = LINADD+2101 FORMAT(1H0)

102 FORMAT(1H1, 20H 66X, 7HPROBLEM I4) 103 FORMAT(1X.12A6) R(M,N) = STATIC SOIL RESISTANCE FOR GIVEN SEGMENTS -123 FORMAT(85H 1 OTHERS HAVE R(I,J) = 0.0**// 5X,10(8X,I2)**) 105 FORMAT(4X,29H CARD ID1 ID2 1/DELTEE = F8.0,12HNOP(1) =1 I2, 12H NOP(16) =12) 106 FORMAT(28X, 5H MP = 18,12HNOP(2) = I2, 12HNOP(17) = I2107 FORMAT(11H A6, A4, 12H 101 VELMI = F8.2,12H NOP(3) =NOP(18) =1 I2, 12H I2) 108 FORMAT(11H 102 A6, A4, 12H $NSTOP = I8 \cdot 12H$ NOP(4) =1 I2, 12H NOP(19) =I2) 110 FORMAT(11H WAM A6, A4, 12H RUT = F8.1, 12HNOP(5) = I2, 1 12H NOP(20) =I2) 111 FORMAT(11H XKAM A6, A4, 12H RUP = F8.1, 12HNOP(6) = 12)112 FORMAT(11H RUM A6, A4, 12H MO = 18 ,12H NOP(7) = I2)GAMMA A6,A4,12H 113 FORMAT(11H $QSIDE = F_8.4.12H$ NOP(8) = I2)QPOINT = F8.4, 12H114 FORMAT(11H EEM A6, A4, 12H NOP(9) = I2)115 FORMAT(11H BEEM A6,A4,12H SIDEJ = F8.4.12HNOP(10) = I2)116 FORMAT(11H VEL A6, A4, 12H POINTJ =F8.4, 12HNOP(11) = I2)117 FORMAT(11H Q A6,A4,12H NUMR = I8 ,12H NOP(12) = I2)118 FORMAT(11H SOILJ A6,A4,12H IPRINT = I8 ,12H NOP(13) = 12)119 FORMAT(11H DYNAMK A6,A4,12H AREA = F8.2,12H NOP(14) = I2)120 FORMAT(11H A A6, A4, 12H NR = 18 , 12H NOP(15) = I2)WAM(M) RUM(M) GAMMA(M) 121 FORMAT(116H M XKAM(M) EEM(M) 1 BEEM(M) VEL(M) Q(M) SOILJ(M) DYNAMK(M) A(M) 1. 2 116H (KIPS) (KIPS/IN) (KIPS) (KIPS) (NONE) (SECIN/ (IN) (SEC/FT) (KIPS/IN) (SQ IN) (FT/SEC) 3FT) • 122 FORMAT(14,-3PF10.4,3F10.1,0P2F10.6,F10.3,2F10.6,-3PF10.3,0PF12.3) $124 \text{ FORMAT}(/4H 7 = I_3, 2X, 10F10.1, (/9X, 10F10.1))$ RETURN END SIBFTC REPONE SUBROUTINE REP1 COMMON WAM(100), XKAM(100), RUM(100), BEEM(100), EEM(100) COMMON GAMMA(100), XKIM(100), CEEMAS(100), NFOM(100), XDEM(100)

PAGE SIXTY-SEVEN

1 2

COMMON DEM(100), XCEEM(100), CEEM(100), FOM(100), XFOM(100)	3
COMMON VEL(100), DIM(100), RAM(100), RMAX(100), RSTAT(100)	4
COMMON R(100,10) , ITRIG(100), Q(100), FORCIN(100), DFOM(100)	5
COMMON FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100), A(100)	6
COMMON DEMAX(100), IDEMAX(100), SJ(100), NOP(22), DYNAMK(100)	7
COMMON CEEMIN(100), HOLDEM(100), ANSVEC(50), SE(50, 51) , IROW(51)	8
COMMON RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(100)	9
COMMON ICOL(51), NOPP(20), ENTHRU(100), ENTMAX(100), IDS(50)	10
COMMON QSIDE , QPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP	50
COMMON INTV , ISECTN, NUMR , F1 , F2 , C1 , C2	51
COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT	52
COMMON INTT, I, ITST, IX, NR, MO, MP	53
COMMON NPAGE , N , QUAKE , RUP , RUT , VELMI , ID1	54
COMMON ID2 , ID3 , ID4 , IDW1 , IDW2 , IDK1 , IDK2	55
COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 , IDB1	56
COMMON IDB2 , IDV1 , IDV2 , IDQ1 , IDQ2 , IDJ1 , IDJ2	57
COMMON IDDK1 , IDDK2 , IDA1 , IDA2 , KGRADD, J5 , TMIN	58
COMMON THAX , SMIN , SMAX , NOPNTS, AREA , NSI , NS2,NS6	59
COMMON NS3 , NS4 , NS5 , IDEEM , MH , VEL1 , ACCELR	60
COMMON B , C , AREAP , XLONG , ELAST , ACELMX	61
COMMON DV1, DE1, DE2, DRI, DRP, DQI, DQP, DJI, DJP, DW1, DW2, DWI, DK1, DK2, DKI	
MP = MP	
MPP = MP+1	
SMAX = 0.0	
SMIN = 0.0	
DO 64 I = 1, MPP	
ITRIG(I) = 1	
$DEM(\mathbf{I}) = 0_{\bullet}0$	
XDEM(I) = 0.0	
DEMAX(I) = 0.0	

С

- IDEMAX(I) = 0 CEEM(I) = 0.0 XCEEM(I) = 0.0 CEEMAS(I) = 0.0
```
FOM(I) = 0.0
      XFOM(I) = 0.0
      FOMAX(I) = 0.0
      FOMIN(I) = 0.0
      IFOMAX(I) = 0
      IFOMIN(I) = 0
      NFOM(I) = 1
      RAM(I) = 0.0
      RMAX(I) = 0.0
      RSTAT(I) = 0.0
      DIM(I) = 0.0
      ENTHRU(I) = 0.0
      ENTMAX(I) = 0.0
   64 CONTINUE
      IF(NOP(14)-4)18,65,18
   65 CONTINUE
      C = (F1*C2 - F2*C1)/(C1*C2*(C1-C2))
      B = (F2*C1**2 - F1*C2**2)/(C1*C2*(C1-C2))
      IF(B)22,22,18
   22 IF(F1-F2)24,23,23
   23 C = F1/C1 + 2
      GO TO 25
   24 C = F2/C2 + 2
   25 B = 0.0
      WRITE(6,104)
  104 FORMAT(47HOPARABOLA BASED ON F2 AND C2 ONLY MUST BE USED
                                                                        )
   18 CONTINUE
      RETURN
      END
$IBFTC REPREP
      SUBROUTINE REP N
      COMMON
                WAM(100), XKAN(100),
                                        RUM(100).
                                                   BEEM(100),
                                                                EEM(100)
                                                                                1
      COMMON GAMMA(100), XKIM(100), CEEMAS(100),
                                                   NFOM(100), XDEM(100)
                                                                                2
      COMMON
                DEM(100), XCEEM(100), CEEM(100),
                                                    FOM(100), XFOM(100)
                                                                                3
      COMMON
                VEL(100),
                            DIM(100),
                                        RAM(100).
                                                   RMAX(100), RSTAT(100)
                                                                                4
```

2n

PAGE SIXTY-NINE

С

COMMON R(100,10) , ITRIG(100), Q(100), FORCIN(100), DFOM(100)	5
COMMON FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100), A(100)	6
COMMON DEMAX(100), IDEMAX(100), SJ(100), NOP(22), DYNAMK(100)	7
COMMON CEEMIN(100), HOLDEM(100), ANSVEC(50), SE(50, 51) , IROW(51)	8
COMMON RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(100)	9
COMMON ICOL(51), NOPP(20), ENTHRU(100), ENTMAX(100), IDS(50)	10
COMMON QSIDE , QPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP	
COMMON INTV , ISECTN, NUMR , F1 , F2 , C1 , C2	51
COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT COMMON INTT , I , ITST , IX , NR , MO , MP COMMON NPAGE , N , QUAKE , RUP , RUT , VELMI , ID1	52
COMMON INTT, I, ITST, IX, NR, MO, MP	53
COMMON NPAGE , N , QUAKE , RUP , RUT , VELMI , ID1	54
COMMON ID2 , ID3 , ID4 , IDW1 , IDW2 , IDK1 , IDK2	55
COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 , IDB1	56
COMMON IDB2 , IDV1 , IDV2 , IDQ1 , IDQ2 , IDJ1 , IDJ2	57
COMMON IDDK1 , IDDK2 , IDA1 , IDA2 , KGRADD, J5 , TMIN	58
COMMON TMAX , SMIN , SMAX , NOPNTS, AREA , NS1 , NS2,NS6	59
COMMON NS3 , NS4 , NS5 , IDEEM , MH , VEL1 , ACCELR	60
COMMON B , C , AREAP , XLONG , ELAST , ACELMX	61
COMMON DV1,DE1,DE2,DRI,DRP,DQI,DQP,DJI,DJP,DW1,DW2,DWI,DK1,DK2,DKI	
INTV = INTV+1	

INTV = INTV+1 MP=MP MPP = MP+1 NOP(4) = NOP(4) NOP(13) = NOP(13) NOP(14) = NOP(14) NOP(15) = NOP(15) ITEST1 = 1 ITESTP = 1 DO 68 I = I, MP I=I IF(I-MP)18,I7,18 17 ITESTP = 2 18 CONTINUE XDEM(I) = DEM(I)

```
21 GO TO(34,19), ITESTP
   34 \times CEEM(I) = CEEM(I)
С
      STATEMENT 34 MUST USE A COMPUTED VALUE FOR THE ACTUAL DEM(I+1)
      CEEM(I) = DEM(I) -DEM(I+1) -VEL(I+1)*12.0*DELTEE
       XFOM(I) = FOM(I)
      IF(BEEM(1)-0.000001)36,36,30
   30 IF(DYNAMK(I))31,31,32
С
                                                     SMITHS DAMPING METHOD
   31 DFOM(I) = BEEM(I) *XKAM(I) *(CEEM(I) -XCEEM(I))/(DELTEE*IZ+0)
       GO TO 33
C
                                            STANDARD LINEAR SOLID DAMPING
   32 DFOM(I) = (DFOM(I)+DYNAMK(I)*(CEEM(I)-XCEEM(I)))/
     1
                 (1.0+DYNAMK(I)*DELTEE/(1000.0*BEEM(I)))
   33 FOM(I) = CEEM(I) + XKAM(I) + DFOM(I)
      GO TO 43
   36 IF(0.99999-EEM(I))38,38,39
   38 \text{ FOM(I)} = \text{CEEM(I)} * XKAM(I)
      CEEMAS(I) = AMAX1(CEEMAS(I), XCEEM(I))
      GO TO 43
   39 \text{ CEEMAS(I)} = \text{AMAX1(CEEMAS(I), XCEEM(I))}
      CEEMIN(I) = AMIN1(CEEMIN(I), XCEEM(I))
      IF(CEEM(I))13,43,5
    5 IF(CEEM(I)-CEEMAS(I))11,11,38
   11 FOM(I)=AMAX1(XKAM(I)*(CEEMAS(I)-(CEEMAS(I)-CEEM(I))/EEM(I)**2),0.)
      GO TO 43
   13 IF (CEEM(I)-CEEMIN(I))38,14,14
   14 FOM(I)=AMIN1(XKAM(I)*(CEEMIN(I)-(CEEMIN(I)-CEEM(I))/EEM(I)**2),0.)
   43 CONTINUE
С
                                  IF NOP(14)=2, SET FOM(1) = FORCIN(INTV)
      GO TO(1,16), ITEST1
    1 \text{ NOP14} = \text{NOP(14)+1}
```

20 DEMAX(I) = DEM(I)

PAGE SEVENTY-ONE

DEM(I) = XDEM(I) +VEL(I)*12.0*DELTEE

IF(DEMAX(I)-DEM(I))20,21,21

IDEMAX(I) = INTV

```
GO TO(6,6,2,2,6),NOP14
    2 \text{ FOM}(1) = \text{FORCIN(INTV)}
      IF(FOM(1)-1.0)3.3.4
    3 \text{ DEM(1)} = \text{XDEM(1)}
      CEEM(1) = XCEEM(1)
      GO TO 16
C IF NOP(14) = 4. USE PARABOLIC FOM(1) VS. CEEM(1) CURVE
C THE RAM MUST BE A SINGLE MASS IF FOM VS. DEM IS PARABOLIC
    6 IF(NOP(14)-4)4,7,4
    7 IF(CEEM(1) - CEEMAS(1))9,8,8
    8 \text{ FOM}(1) = C \times CEEM(1) \times 2 + B \times CEEM(1)
      GO TO 12
    4 IF(CEEM(1)-CEEMAS(1))16,12,12
    9 FOMAX(1) = AMAX1(XFOM(1), FOMAX(1))
      FOM(1) = FOMAX(1)-((CEEMAS(1)-CEEM(1))*FOMAX(1)**2)/(2.0*SMAX*
     1
            EEM(1) + + 2
      GO TO 16
   12 SMAX = SMAX+((FOM(1)+XFOM(1))/2.0)*(CEEM(1)-XCEEM(1))
   16 CONTINUE
      IF(GAMMA(I))46,44,45
   44 FOM(I) =AMAX1 (.0, FOM(I))
      GO TO 46
   45 \text{ IF}(FOM(1) - XFOM(1))48,47,47
   48 \text{ NFOM(I)} = 2
   47 IX = NFOM(I)
      GO TO (46,49),IX
   49 HOLDF = FOM(I)
      FOM(IT = AMAXI(FOM(I), GAMMA(I))
COMMENT THE .O1 HOLDS MIN. PRESSURE AT GAMMA(I) FOR .O1 SECONDS WHILE THE
COMMENT .0025 REDUCES THE PRESSURE TO ZERO IN .0025 ADDITIONAL SECONDS.
      TINT = INTV
      IF(TINT - .01/DELTEE)46,46,90
   90 FOM(I) = AMAX1(0.0, GAMMA(I)*(1.0-(DELTEE*TINT-.01)/.0025),HOLDF)
   46 CONTINUE
      ENTHRU(I) = ENTHRU(I)+(FOM(I)+XFOM(I))+(DEM(I+1)-XDEM(I+1))/24.0
```

```
ENTMAX(I) = AMAX1(ENTMAX(I),ENTHRU(I))
       GO TO(22,19), ITEST1
    22 IF(CEEM(1) - CEEMAS(1))15,19,19
   15 SMIN = SMIN-((FOM(1)+XFOM(1))/2.0)*(CEEM(1)-XCEEM(1))
   19 CONTINUE
       IF(NOP(4)-5)29,28,29
С
                                             GENERALIZED SOIL RESISTANCE
   28 CALL GENRAM
      GO TO 55
   29 CONTINUE
С
                                                   SMITHS SOIL RESISTANCE
      IF(XKIM(I))50,155,50
  155 GO TO(55,156), ITESTP
  156 IF(XKIM(MPP ))50,55,50
   50 IF(DIM(I) -DEM(I) +Q(I) )51,52,52
   51 DIM(I) = DEM(I) - Q(I)
   52 CONTINUE
   70 IF(DIM(I) -DEM(I) -Q(I) )53,53,54
   54 DIM(I) = DEM(I) + Q(I)
   53 CONTINUE
      DIM(MPP ) =AMAX1 (DIM(MP),DIM(MPP ))
      ITST = ITRIG(I)
      GO TO(10,57),ITST
   10 IF(DEM(I) -DIM(I) -Q(I) )56,57,57
   56 RAM(I) = (DEM(I)-DIM(I))*XKIM(I)*(1.0+(SJ(I) *VEL(I)))
      GO TO(55,171), ITESTP
  171 RAM(MP) = RAM(MP)+(DEM(MP)-DIM(MPP ))*XKIM(MPP )*
     1 (1.0+(SJ(MPP)*VEL(MP)))
С
                               SEGMENT MP HAS RAM(MP) + RAM(MP+1) APPLIED
€
                                                RAM(MP+1) MAY BE TENSILE
      GO TO 55
   57 RAM(I) = (DEM(I)-DIM(II+ SJ(I) *Q(I) *VEL(I))*XKIM(I).
      ITRIG(I) = 2
      GO TO(55,172), ITESTP
```

172 RAM(MP)=RAM(MP)+(DEM(I)-DIM(MPP)+SJ(MPP)*Q(MPP)*VEL(MP))*XKIM(MPP)

```
55 CONTINUE
    GO TO(58,72), ITEST1
58 VEL(1) = VEL(1)-(FOM(1) +RAM(1))*32.17*DELTEE/WAM(1)
    ITEST1 = 2
    GU TO 59
72 VEL(I) = VEL(I)+(FOM(I-1) -FOM(I) -RAM(I))*32.17*DELTEE/WAM(I)
59 CONTINUE
    IF(NOP(15)-1)85,85,83
83 VEL(I) = VEL(I) + 32.17*DELTEE
85 CONTINUE
65 IF(FOMAX(I)-FOM(I))67,67,66
67 \text{ FOMAX(I)} = \text{FOM(I)}
    IFOMAX(I) = INTV
66 IF(FOMIN(I)-FOM(I))68,69,69
69 \text{ FOMIN(I)} = \text{FOM(I)}
    IFOMIN(I) = INTV
68 CONTINUE
    IF(VEL(2)/VEL1 -2.1)61,60, 60
 60 WRITE(6,105)
    INTT = 2
    RETURN
105 FORMAT(76HO THE RATIO OF THE VELOCITY OF W(2) TO THE VELOCITY OF
   1THE RAM EXCEEDS 2.1. )
 61 IF(VEL(MP)/VEL1 -2.1)63.62.62
 62 WRITE(6,106)
106 FORMAT(76HO THE RATIO OF THE VELOCITY OF W(P) TO THE VELOCITY OF
   1THE RAM EXCEEDS 2.1. )
    INTT = 2
    RETURN
 63 CONTINUE
    LDCELL = MH-1
    ACCELR = (FOM(LDCELL-1)-FOM(LDCELL))/WAM(LDCELL)
 71 ACELMX=AMAX1 (ACELMX, ACCELR)
 73 CONTINUE
```

```
RETURN
```

END

\$IBFTC RAMGEN

SUBROUTINE GENRAM

C C

С

С

C C

NQDIV = NO. OF EQUAL SEGMENTS INTO WHICH Q(I) IS DIVIDED = 10 RSTAT(I) = STATIC SOIL RESISTANCE NEGLECTING THE SOIL DAMPING EFFECTS RMAX(I) = A TEMPORARY MAXIMUM STATIC SOIL RESISTANCE PERCQ = DISTANCE FROM ZERO DISPLACEMENT TO DEM(I) IN UNITS (1.732,..) COMMON WAM(100), XKAM(100), RUM(100). BEEM(100), EEM(100) 1 COMMON GAMMA(100). XKIM(100), CEEMAS(100), NFOM(100), XDEM(100) 2 COMMON DEM(100), XCEEM(100), CEEM(100), FOM(100). XFOM(100) 3 COMMON VEL(100), DIM(100), RAM(100), RMAX(100), RSTAT(100) 4 COMMON R(100,10) , ITRIG(100), Q(100), FORCIN(100), DFOM(100) 5 FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100), COMMON A(100) 6 COMMON DEMAX(100), IDEMAX(100), SJ(100), NOP(22), DYNAMK(100) 7 COMMON CEEMIN(100), HOLDEM(100), ANSVEC(50), SE(50,51) , IROW(51) 8 COMMON RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(100) 9 COMMON ICOL(51), NOPP(20), ENTHRU(100), ENTMAX(100), IDS(50) 10 COMMON QSIDE , QPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP 50 COMMON INTV , ISECTN, NUMR , F1 , F2 • C1 · C2 51 COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT 52 COMMON INTT , I , ITST , IX NR • MO , MP 53 COMMON NPAGE , N , QUAKE , RUP , RUT , VELMI ; ID1 54 COMMON ID2 • ID3 , ID4 , IDW1 , IDW2 J IDK1 IDK2 55 COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 , IDB1 56 COMMON IDB2 . IDV1 , IDV2 , IDQ1 , ID02 , IDJ1 , IDJ2 57 COMMON IDDK1 , IDDK2 , IDA1 , IDA2 , KGRADD, J5 . TMIN 58 COMMON TMAX SMIN , SMAX • NOPNTS • AREA • NS1 , NS2,NS6 59 COMMON NS3 • NS4 , NS5 , IDEEM , MH , VEL1 + ACCELR 60 COMMON B. **,** C . AREAP . XLONG . ELAST . ACELMX 61 COMMON DV1, DE1, DE2, DR1, DRP, DQ1, DQP, DJ1, DJP, DW1, DW2, DW1, DK1, DK2, DK1

 $\phi \leq \pi$

С

MP = MPK = I

PAGE SEVENTY-FIVE

```
QDIV = 10.0
      NQDIV = 10
      IF(XKIM(K)-0.1) 1,2,2
    1 RAM(K) = 0.0
      GO TO 70
    2 IF(DEM(K)-DIM(K))32,3,3
    3 DIM(K) = DEM(K)
      IF(DEM(K) - O(K))7,6,6
    6 \text{ RSTAT(K)} = R(K, NQDIV)
      GO TO 50
    7 PERCQ = DEM(K)/(Q(K)/QDIV)
      IPERCQ = PERCQ
      XPERCQ = IPERCQ
      IF(IPERCQ)8,8,9
    8 \text{ RSTAT(K)} = PERCQ * R(K, 1)
      GO TO 50
    9 RSTAT(K) = R(K, IPERCQ) + (PERCQ-XPERCQ) + (R(K, IPERCQ+1)-R(K, IPERCQ))
      GO TO 50
   32 RMAX(K) = AMAX1(RMAX(K), RSTAT(K))
      RSTAT(K) = RMAX(K) - (DIM(K) - DEM(K)) + XKIM(K)
C THE STATIC FORCE SHOULD REALLY LEAVE THE XKIM(I) SLOPE AND REMAIN
C CONSTANT IF RMAX(I)+RSTAT(I) EVER EXCEEDS 0.0
      IF(RMAX(K)+RSTAT(K))39,50,50
   39 WRITE(6,200)RMAX(K),RSTAT(K),K
  200 FORMAT(11HORMAX(I) = F10.2, 6X, 12H RSTAT(I) = F10.2,6X,4H I = I6)
C STATEMENTS 50 THRU 70 INCLUDE THE SOIL DAMPING EFFECT
   50 \text{ ITST} = \text{ITRIG}(K)
      GO TO(51,57), ITST
   51 IF(DEM(K)-Q(K))56,57,57
   56 RAM(K) = RSTAT(K)+RSTAT(K)*SJ(K)+VEL(K)
      GO TO 70
   57 RAM(K) = RSTAT(K)+R(K,NQDIV)*SJ(K)*VEL(K)
      ITRIG(K) = 2
      GO TO 70
   70 IF(K-MP)80,71,73
```

	71 CONTINUE	
	K = MP + 1	
	IF(XKIM(K)-0.01)80,80,72	
	72 $DEM(K) = DEM(MP)$	
	VEL(K) = VEL(MP)	
	GO TO 2	
	73 CONTINUE	
С		
č	73 IF(RAM(K))74,75,75 (OLD STATEMENT)	
C	74 RAM(K) = 0.0 (OLD STATEMENT) 1	
	74 CONTINUE	
~	75 RAM(MP) = RAM(MP) + RAM(MP+1)	
С	RAM(MP+1) CAN GO INTO TENSI	ON
	OU RETURN	
	END	
\$ I	BFTC EXCTG	
	SUBROUTINE EXACTS	
	COMMON WAM(100), XKAM(100), RUM(100), BEEM(100), EEM(1	00) 1
	COMMON GAMMA(100), XKIM(100), CEEMAS(100), NFUM(100), XDEM(1	
	COMMON DEMIIOU, ALEEMIIOU, CEEMIIO), FOMIIOI, YEOMII	001 2
	CUMMON VEL(IUO), DIM(100), RAM(100), RMAX(100), RETAT(1)	001 4
	(100), (100) , $($	00) 5
	COMMON FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100), A(1)	
	COMMON DEMAX(100), IDEMAX(100), SJ(100), NOP(22), DYNAMK(1	00) 7
	COMMON CEEMIN(100), HOLDEM(100), ANSVEC(50), SE(50,51) , IROW(51) 8
	COMMON RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(1	00) 9
	COMMON ICOL(51), NOPP(20), ENTHRU(100), ENTMAX(100), IDS(50) 9
	COMMON QSIDE , QPOINT, SIDEJ , POINTJ, NQDIV , NORAMS, NSTOP	
	COMMON INTV , ISECTN, NUMR , F1 , F2 , C1 , C2	50
	COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT	51
		52
	COMMON INTE, I , ITSE, IX , NR , MO , MP COMMON NPAGE, N , QUAKE, RUP , RUT , VELMI, IDI	53
	COMMON ID2 , ID3 , ID4 , IDW1 , IDW2 , IDK1 , IDK2	54
	COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 , IDB1	55
	COMMON IDB2 , IDV1 , IDV2 , IDQ1 , IDQ2 , IDJ1 , IDJ2	56
		57
	CUMMUN IDUKI , IDUK2 , IDAI , IDA2 , KGRADD, J5 , TMIN	58

.

;

PAGE SEVENTY-SEVEN

e 😵 🖓 🖧

PAGE SEVENTY-EIGHT

С

COMMON TMAX , SMIN , SMAX , NOPNTS, AREA , NS1 • NS2•NS6 59 , NS5 , IDEEM , MH , VEL1 , ACCELR COMMON NS3 , NS4 60 COMMON B • C , AREAP , XLONG , ELAST , ACELMX 61 COMMON DV1.DE1.DE2.DRI,DRP,DQI,DQP,DJI,DJP,DW1,DW2,DWI,DK1,DK2,DKI and the second sec MP = MPMO = MO MMO = MO-1MMOO = MO - 2MAO = MP - MONSDD = MP - MO + 1DO 6 NSEW = 1, NSDDDO 6 NSE = 1, NSDD6 SE(NSEW, NSE) = 0.0SE(1,1) = XKAM(MO) + XKIM(MO)SE(2,1) = -XKAM(MO)DO 13 K = 2, MAONN = K + MMOONNN = K + MMOSE(K-1,K) = SE(K,K-1)SE(K,K) = XKAM(NN) + XKAM(NNN) + XKIM(NNN)SE(K+1,K) = -XKAM(NNN)**13 CONTINUE** SE(MAD, NSDD) = SE(NSDD, MAO)SE(NSDD,NSDD) = XKAM(MP-1)+XKIM(MP) + XKIM(MP+1) DET = TAMINV(SE, ICOL, NSDD, 50, 0.00001)IF(0.00001 - ABS(DET))14, 12, 1212 WRITE(6,100)DET 100 FORMAT(33HOTHE VALUE OF THE DETERMINANT = F10.7) INTT = 2RETURN 14 CONTINUE WAMTL = 0.0DO 15 NSEW = 2,MO15 WAMTL = WAMTL + WAM(NSEW)

1 C 4 A

```
SE(1, NSDD+1) = WAMTL
   DO 16 NSEW = 2,NSDD
   NUTZ = MMO+NSEW
16 SE(NSEW, NSDD+1) = WAM(NUTZ)
   DO 17 IANS = 1, NSDD
17 \text{ ANSVEC(IANS)} = 0.0
   DO 23 IM1 = 1,NSDD
   DO 23 IM2 = 1,NSDD
23 ANSVEC(IM1) = ANSVEC(IM1)+SE(IM1,IM2)+SE(IM2,NSDD+1) -
   NAT = 0
   DO 26 NST = MO, MP
   NAT = NAT+1
   DEM(NST) = ANSVEC(NAT)
   HOLDEM(NST) = DEM(NST)
26 CONTINUE
   WOS = 0.0
   DO 27 NST = 2,MMO
   WOS = WOS+WAM(NST)
   CEEM (NST) = WOS/XKAM(NST)
   FOM(NST) = WOS
27 CONTINUE
   DO 28 NST = 1, MMO
   NEL = MO - NST
   DEM(NEL) = DEM(NEL+1) + CEEM(NEL)
   HOLDEM(NEL) = DEM(NEL)
28 CONTINUE
   MAM = MP-1
   DO 29 NST = MO, MAM
   CEEM(NST) = DEM(NST) - DEM(NST+1)
   FOM(NST) = CEEM(NST) * XKAM(NST)
   RAM(NST) = DEM(NST) *XKIM(NST)
29 CONTINUE
   RAM(MP) = DEM(MP) * XKIM(MP)
   RAM(MP+1) = DEM(MP) + XKIM(MP+1)
   RETURN
```

END

\$IBFTC SMTH

SUBROUTINE SMITH XKAM(100), BEEM(100), 1 COMMON WAM(100), RUM(100), EEM(100) 2 COMMON GAMMA(100). XKIM(100), CEEMAS(100), NFOM(100), XDEM(100) COMMON DEM(100), XCEEM(100), CEEM(100), FOM(100), 3 XFOM(100) 4 COMMON VEL(100), DIM(100), RAM(100), RMAX(100), RSTAT(100) COMMON R(100,10) , ITRIG(100), Q(100), FORCIN(100), DFOM(100) 5 6 FOMAX(100), IFOMAX(100), FOMIN(100), IFOMIN(100). COMMON A(100) 7 DEMAX(100), IDEMAX(100), SJ(100), NOP(22), DYNAMK(100) COMMON 8 COMMON CEEMIN(100), HOLDEM(100), ANSVEC(50), SE(50,51) , IROW(51) RUMA(100), WAMC(100), XKAMC(100), QA(100), SJA(100) 9 COMMON 10 COMMON ICOL(51), NOPP(20), ENTHRU(100), ENTMAX(100), IDS(50) 50 COMMON QSIDE, QPOINT, SIDEJ, POINTJ, NQDIV, NORAMS, NSTOP , C1 51 COMMON INTY , ISECTN, NUMR , F1 • F2 · C2 52 COMMON IPRINT, DELTEE, EEM1 , EEM2 , GAMMA1, GAMMA2, INT . MP 53 COMMON INTT , NR • MO • I , ITST • IX 54 COMMON NPAGE . N , QUAKE , RUP + RUT , VELMI , ID1 55 , IDW2 , IDK1 COMMON ID2 • ID3 **, ID4** , IDW1 , IDK2 COMMON IDRL1 , IDRL2 , IDG1 , IDG2 , IDE1 , IDE2 • IDB1 56 57 , IDV1 , IDV2 , IDQ1 , ID02 , IDJ1 , IDJ2 COMMON IDB2 , KGRADD, J5 , TMIN 58 COMMON IDDK1 , IDDK2 , IDA1 , IDA2 59 • SMIN - SMAX , NOPNTS, AREA , NS1 , NS2, NS6 COMMON TMAX 60 • NS4 , VEL1 , ACCELR COMMON NS3 , NS5 , IDEEM , MH 61 **,** C , AREAP , XLONG , ELAST , ACELMX COMMON B COMMON DV1, DE1, DE2, DRI, DRP, DQI, DQP, DJI, DJP, DW1, DW2, DWI, DK1, DK2, DKI MP = MP

С

MP = MP N = MP-1 WAMTL = 0.0 RAMTL = 0.0 DO 5 JT = 2,MP WAMTL = WAMTL + WAM(JT) 5 RAMTL = RAMTL + RUM(JT) RAMTL = RAMTL + RUM(MP+1)

```
DO 8 JT = 2, N
   RAM(JT) = (RUM(JT)*WAMTL)/RAMTL
 8 FOM(JT) = FOM(JT-1)+WAM(JT)-RAM(JT)
   RAM(1) = RUM(1) + WAMTL/RAMTL
   RAM(MP) = RUM(MP) + WAMTL/RAMTL
   RAM(MP+1) = RUM(MP+1)*WAMTL/RAMTL
   DEM(MP) = (RAM(MP)+RAM(MP+1))/(XKIM(MP)+XKIM(MP+1))
  HOLDEM(MP) = DEM(MP)
   DO 11 JT = 1.N
   JTM = MP - JT
  CEEM(JTM) = FOM(JTM)/XKAM(JTM)
  DEM(JTM) = DEM(JTM+1) + CEEM(JTM)
  HOLDEM(JTM) = DEM(JTM)
  DIM(JTM)=DEM(JTM)-WAMTL+Q(JTM)/RAMTL
11 CONTINUE
  RETURN
  END
```

1 6 4 K

SDATA

Q.