(with the exception of autos per household) tend to be highly correlated with population density.

# 3.4.1. Worker Density Patterns

Figure 3.2 depicts the results of the cubic spline regression fit to the census-tract level observations of the spatial density of workers, as a function of distance from CBD, for the four urban areas, in 1960, 1970 and 1980. The dependent variable was defined analogously to the population density case, by dividing the number of workers living in each tract by the area of that tract. In all four case areas, the patterns depicted in Fig. 3.2 very closely mirror those exhibited by the population density. Generally, worker densities tend to be around 40 to 50% of the corresponding population density. Discrepancies between the spatial patterns of population and worker densities thus reflect variations in the ratio of workers per person, or in the fraction of workers per household across the urban space. Such variation may be due to larger households with many young children, higher participation rates of women in the work force, the predominance of retirees in particular areas, or higher unemployment rates. Likely illustrations of each of the above can be detected by carefully comparing Fig. 3.1 to Fig. 3.2. Several observations can be made in this regard.

In Atlanta, the worker density near the origin, relative to the corresponding population density, is less than the relative worker densities as one moves away towards the more affluent suburbs, especially for the 1980 data. The lower workers per person ratio in all likelihood reflects higher unemployment rates in the center city, in which poorer racial minorities have tended to cluster over time. In Dallas, in the range of 7 to 13 miles from the CBD, it appears that the difference in worker density between 1970 and 1980 exceeds the difference in this quantity between 1960 and 1970 by a factor that is greater than the corresponding changes in population density. This indicates a marked increase in the workers per person ratio in the early 1980's, reflecting two simultaneous and continuing trends: more two-worker households due to higher labor force participation by women,





# DENSITY PATTERN OF WORKERS Figure 3.2

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accompanied by smaller family sizes, among young couples in the middle to upper middle class that tend to locate in the suburban ring under consideration. Another related factor may be the larger number of working singles who live in the densifying suburbs, particularly in a city like Dallas whose growth was peaking in the early 1980's.

#### 3.4.2. Density of Commuters by Transport Mode

Figure 3.3 depicts the density of workers driving their automobile or carpooling in their daily commute to work, as a function of distance from the CBD, for all four areas and three time periods. As before, the dependent variable is obtained by dividing the number of such commuters in a given tract by the area of that tract. Figure 3.4 presents similar information for the density of workers using bus transit for their work commute (the official Census category consists workers using bus transit or streetcar, the latter being an irrelevant mode for the cities under consideration in this study), thereby giving an indication of relative mode usage as a function of distance from CBD. It must be noted at the onset that transit usage in the four case cities has been over the study period a relatively minor component of the total suburban travel picture, and that the statistical analysis of the corresponding observations might not be very meaningful.However, the resulting patterns shown in Fig. 3.4 appear to be meaningful and plausible.

In general the spatial density functions for both categories are generally similar in shape to the first two curves (worker density and population density). Possible differences in modal split over space and time did not perceptibly distort the underlying worker density patterns. Some differences are nevertheless apparent. For example, the density of bus users in Austin in 1970 does not exhibit the smaller though distinct peak exhibited by the population and worker densities at ~6 miles away from the CBD, thereby clearly reflecting the negligible transit usage in Austin among the suburban residents at that time. In Atlanta, relative transit usage among central city residents (up to ~4 miles) has remained substantial over time, at about 40%. This level rapidly drops as one moves away into the suburbs. In Phoenix, relative transit usage in the core area experienced a drop through the sixties, but

Figure 3.3

DENSITY PATTERN OF WORKERS USING PRIVATE AUTO OR CARPOOL





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apparently reversed some of it in the seventies, as seen by comparing the worker density to the transit users density patterns for the corresponding years.

# 3.4.3. Spatial Patterns of Automobile Ownership

The variation of average automobile ownership per household with distance from the CBD provides a useful characterization of urban structure for the purpose of transport analysis, and one that is not as highly correlated with the various densities seen earlier. Figure 3.5 depicts the cubic spline fit to the average number of autos per household as a function of distance, for the four urban areas under consideration and at the three time periods considered so far. The dependent variables are the corresponding averages taken at the census tract level. Several important and consistent trends are clear in Fig. 3.5, for all four urban areas. Car ownership has increased steadily over time. Spatially, it increases almost linearly with distance from the CBD for about the first 10 miles (in 1980); the increasing trend with distance continues beyond that point, but at a decreasing rate, peaking at about 2 to 2.2 vehicles per household, at a distance that varies across cities, in the  $\sim$ 15 to ~25 miles range (for the 1980 data). A decreasing pattern appears to prevail then, with a local minimum somewhere in the ~25 to ~35 miles range (in 1980). Essentially, this pattern seems to mirror the spatial pattern of household income in the metropolitan area. The temporal evolution of this pattern also appears to be consistent, with all the above mentioned breakpoints progressively shifting outwards. The question then becomes whether the pattern observed over the past twenty or thirty years will continue, or whether some form of saturation has been reached. It is also interesting to note that the shape of Austin's 1980 pattern more closely resembles that of the other three cities than in previous years, reflecting the rapid growth and transformation of Austin in the late seventies, continuing onto the eighties.

While our sample is limited to four areas, the above spatial pattern of auto ownership and its evolution appear to be robust characteristics of urban areas, and are likely to hold in other mature cities as well. Additional data from a selected cross-section of

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areas could yield a useful tool for exploring the implications of evolving urban structure on automobile ownership.

The spatial pattern of automobile ownership density (autos per square mile, calculated by dividing the number of automobiles owned by residents of each given tract by the area of the tract) is shown in Fig. 3.6, as a function of distance from the CBD, for each of the areas and time periods of interest. These functions reflect 1) the underlying distribution of population (and/or workers) and 2) the household auto ownership patterns just discussed. The result is that while the general shape of the auto density functions is similar to that of population or workers, the differences in worker densities over space and time are magnified between the corresponding auto densities. Atlanta provides a good example of this phenomenon, where the differences in automobile ownership densities over time are relatively more substantial than the corresponding differences in population or worker densities.

# **3.5. DIRECTIONAL DENSITY PATTERNS FOR AUSTIN**

In order to further identify certain characteristics of urban structure that might have been masked when considering the overall study area, it is useful to examine some directional spatial density patterns, i.e. within specific travel corridors or sectors of the urban area. Emerging suburban centers unique to certain corridors would then be more likely to be uncovered by the analysis. To illustrate this approach, corridor-level analyses of the same quantities considered in the previous section were conducted for one of the case areas. Austin was selected for convenience, particularly since corridors had recently been defined for transit planning purposes by the appropriate agency. Six different corridors were considered in the Austin metropolitan area, with each corridor being radially oriented with one end being the CBD. These corridors are referred to as the North Central, Northwest, South Central, Southwest, Northeast and Northwest corridors, respectively. The cubic spline regression procedure was used here as well, and applied within each given







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corridor (using only those census tracts that lie mostly within the corridor), for 1960, 1970, and 1980.

Figure 3.7 presents the population density patterns for the six corridors, indicating that the North Central and Northwest corridors are the most dense, both in terms of higher peaks and sustained high levels over long distances, with peaks of about 12,000 residents per square mile near the CBD area. This value is quite higher than the corresponding peak obtained (7,000 per square mile) for the cubic spline fit of the overall density pattern for Austin. The South Central and Southwest corridors, while exhibiting peaks below 6,000 residents per square mile, were interesting because they revealed a two-peaked city at 0.5 miles and 3 miles from the CBD. The first peak was dominant in 1960, but dropped by 1970 while the second peak had risen. The two peaks became less pronounced in 1980, reflecting the greater dispersion of residents within these corridors.

In all corridors, except the North Central and Northwest, the density pattern of workers exhibited a drop near the CBD, coupled with an increase in the suburban areas, as shown in Fig. 3.8. The North Central and Northwest corridors are the only two where densities of workers remained stable or increased slightly near the CBD area, primarily because they include the University (of Texas) area. It can again be noted that the directional worker density patterns maintained a high correlation with the corresponding population density patterns.

The density patterns for workers using private auto or carpool, and those using bus transit, are generally similar to those observed for the area as a whole, with the differences in distance that are better reflected in the directional densities. They are not included herein as their benefit is of a primarily local nature. Figure 3.9 depicts the spatial density of automobile ownership as a function of distance from the CBD, within each of the six corridors. The spatial pattern of household automobile ownership is shown in Fig. 3.10, indicating that the general trends discussed in the previous section in conjunction with the areawide data appear to hold at the corridor level as well. The increase in auto ownership



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#### POPULATION DENSITY PATTERN

Figure 3.7



DENSITY PATTERN OF WORKERS

Figure 3.8



over time is present in all corridors. It can also be noted that the increase in all corridors has been more rapid in the outer areas than near the center.

However, the plots also indicate that those general similarities are accompanied by differences in terms of the peak values and of the distance ranges over which the behavior described earlier applies. For instance, it can be seen that the peak average household auto ownership in the Southeast corridor is ~1.7 autos per household, compared to over 2.2 in several other corridors. These differences undoubtedly reflect socio-economic conditions in the subareas of interest. Spatial differences are also revealed in the distance at which the respective peaks occur, and the corresponding gradients. Thus directional gradients allow the identification of possibly substantial differences in urban structure or development patterns relative to the overall city pattern. As illustrated by the Austin data, development does not occur in a symmetric manner, and emerging suburban nuclei could be masked in the data for the overall area.

#### **3.6. CONCLUDING COMMENTS**

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The spatial density functions of population and other socio-demographic variables provide a useful characterization of urban structure. Taken at different time intervals, these functions provide snapshots of the development pattern of an urban area, which describe the evolution of urban structure in terms of the spatial patterns of residential location, automobile ownership and other variables. The four case studies considered here illustrated the continuing trends, observed over the past three decades, of spatial dispersion away from the traditional central urban cores into the suburbs and exurbs, coupled with the densification of existing suburbs to levels almost comparable to the central cores. Parallelling this pattern has been a continuing growth of average household automobile ownership, in all parts of the urban area, with a distinct spatial and temporal pattern that seems to be robust across the case areas considered as well as within radial corridors in the one case that was so analyzed. While the resulting travel patterns cannot be determined in









Figure 3.10



the absence of the spatial patterns of the location of employment and other activities, one can surmise from looking at the patterns of residence-based variables examined herein that average trip distances are likely to continue to increase, and that congestion levels in the densifying "suburban" subareas will reach levels typically associated with CBD traffic systems. However, suburban networks generally exhibit somewhat different characteristics from CBD systems, in terms of physical features, traffic control and adjoining land use and its generation of traffic-interfering activities. The subsequent chapters in this report shed further light on how congestion and the associated quality of traffic service depend on such features of the traffic networks.

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Several directions for meaningful additional work are suggested by the results presented in this chapter. First, as noted earlier, it would be extremely valuable to consider the corresponding spatial patterns of the location of firms and businesses of different types. This can be accomplished using data sources such as industrial and business directories that give information at the firm level. Second, a larger set of case areas should be considered in order to further assess the robustness of some of the patterns seen here, as well as to possibly classify areas in terms of their respective spatial and temporal patterns. In particular, it would be interesting to examine areas such as San Francisco and Boston that have relatively more elaborate spatial patterns that have developed over longer time frames than many other U.S. cities. Third, it would be interesting to capture the characteristics of the transportation network serving the areas under consideration by examining the densities as a function of network distance or travel time instead of Euclidian distances from the CBD. Finally, it is desirable to integrate the above spatial patterns into an approach to estimate flow patterns and aggregate travel descriptors (such as average trip lengths) resulting from the interaction between the spatial patterns of residence-based variables seen in this chapter, and those of the location of firms and businesses. This would provide an important linkage to the study of the transport implications of evolving urban structures. Such an approach could further incorporate the characteristics of the transport

infrastructure. Preliminary analytic work along these lines, conducted in conjunction with this study, has been promising; it involves the derivation of intraurban flow patterns and average trip lengths under assumed spatial distributions of origins and destinations, for a given generic type of network.

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# CHAPTER 4

# PERFORMANCE OF TRAFFIC NETWORKS: FUNDAMENTAL RELATIONS

#### **4.1. INTRODUCTION**

The previous chapters have examined transport from the demand side, in terms of those activities that generate the flow patterns in a given metropolitan area. This chapter is concerned more directly with the actual flows in the network, and particularly with describing the performance of an urban traffic network, in terms of the quality of traffic service that is or that could be offered by that network under different demand levels. In addition to developing relations among key network-level performance descriptors, the intent is to gain an understanding, and eventually a quantitative description, of how this performance is related to the various features of the network and of the urban area that it serves. This would then provide an operational tool for examining the implications on the quality of traffic service, and thus on the degree of mobility afforded by the traffic system, of the various predicted or proposed scenarios regarding the evolution of urban structure and associated travel patterns. The focus of the present work is limited to urban structure networks, and does not include freeways; extensions in that direction constitute an important future step for this research.

Significant progress has been achieved over the past three decades in terms of characterizing and modelling fundamental traffic phenomena in arterials and intersections. Considerably less effort has been directed towards the development of a network-level traffic theory to characterize the performance of urban street networks. Macroscopic models of traffic flow in urban networks describe the behavior of and interrelation among traffic variables defined at the network level. Such characterization of traffic has important practical implications in terms of measuring the quality of traffic service in a network, and performing related diagnosis, monitoring (over time and space) and evaluation activities

(Ardekani and Herman, 1982; Mahmassani, Williams and Herman, 1984), particularly as these pertain to urban growth and development.

The complex interactions in a traffic network effectively preclude the analytic derivation of macroscopic network-level relationships from the basic principles governing microscopic traffic behavior or from link-level macroscopic models. In addition to questions regarding the very definition of the networkwide traffic descriptors, the existence of meaningful relations among these quantities cannot, a priori, be taken for granted. Some of these questions have been addressed in earlier work by Mahmassani *et al.* (1984) and Williams, Mahmassani and Herman (1985), providing definitions for average speed, concentration and flow, all at the network level, and indicating, on the basis of simulation experiments, that these quantities appear to be related in a manner not unlike their counterparts at the individual road or arterial level.

In the past five years, a network-level modelling approach has developed around Herman and Prigogine's two-fluid theory of town traffic (Herman and Prigogine, 1979; Herman and Ardekani, 1984), which views traffic in a street network (excluding freewaytype facilities) as consisting of two "fluids": moving (or running) vehicles versus stopped vehicles (though still in the traffic stream, such as at traffic signals, as opposed to parked vehicles). The theory postulates that  $V_r = V_m (f_r)^n$ , where  $V_r$  is the average speed of the moving vehicles,  $f_r$  the fraction of running vehicles in the network, and  $V_m$  and n are two parameters which describe the quality of traffic service in the system. The theory leads to a relation between the average running time per unit distance (i.e. the conditional expected trip time per unit distance taken only over moving vehicles) and the average total trip time per unit distance in the network. Field validation has been conducted, using data gathered by the chase-car technique, and, to a very limited extent, aerial photography, under operating conditions found in actual city networks (Ardekani and Herman, 1982; Herman and Ardekani, 1984; Ardekani, Torres-Verdin and Herman, 1985). The sensitivity of the mode been

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The latter approach actually circumvents one of the major obstacles hindering the development of network-level models, namely the cost and difficulty of obtaining reliable data at the network level. The feasibility of using microscopic simulation as a tool to investigate network flow relations has been established in previous work by Mahmassani *a al.* (1984) and Williams *et al.* (1985), on the basis of the NETSIM simulation package. In addition to the obvious cost and resource considerations, this approach allows one a degree of experimental control that is not practical in actual traffic systems, as well as the ability to explore a wider range of situations than can be observed in field work.

Recently, Ardekani and Herman (1987) extended the two-fluid modelling framework to include a set of relations between the principal network traffic variables. These relations are derived from a postulated functional relation between the average fraction of vehicles stopped in a network and the prevailing concentration, slightly modifying an earlier form suggested in Herman and Prigogine's original work (1979). A speed-concentration model can then be derived from the postulated relation, given that the two-fluid assumptions hold. An exploratory calibration of the parameters of the postulated model was also reported, though only very limited aerial photographic data was available for this purpose.

Two principal objectives are adressed in this effort. First, we seek a system of relations that comprehensively describe the joint behavior of the average speed, flow and concentration, as well as the average fraction of vehicles stopped in the network, and the two-fluid stopped and running time variables. Three alternative sets of interrelated models, each (set) having a different starting postulate, are presented and tested against a series of microscopic simulation runs corresponding to different network concentration levels. Second, we analyze the sensitivity of these relations and their parameters to the network's characteristics, particularly its topological features and prevailing control strategies. This

second objective is a modest step towards the more ambitious goal, stated earlier, of relating the quality of traffic service and associated mobility level, to both network features and spatial characteristics of urban activities. Both objectives are supported by microscopic simulation experiments, which provide useful macroscopic insights into network traffic behavior.

In the next section, we present the theoretical fundamentals underlying this work, including the definitions of the principal variables, and the derivation of the flow models from a given postulated relation. In section 4.3, we review the methodological approach followed in the supporting simulation experiments. The three sets of models are then presented, in turn, in section 4.4, and their parameters are calibrated using the results of the simulations, allowing the evaluation of their ability to provide a macroscopic characterization of network traffic flow phenomena. The second objective, namely the sensitivity of these relations and their parameters to network features, is addressed in the next chapter.

#### **4.2. THEORETICAL BACKGROUND**

In this section, we first present the networkwide variable definitions, then conceptually describe the principal relations comprising each set (system) of models, as well as the analytical steps involved in the derivation of the models from a starting functional form relating any two variables.

## 4.2.1. Definition of Network Traffic Variables

The three fundamental traffic variables, speed, concentration, and flow have been generalized in previous work to the network level (Mahmassani *et al.*, 1984). All three are defined as average quantities taken over all vehicles in the network over some observation period  $\tau$ . Average speed V (in mph) is defined as the ratio of total vehicle-miles to total vehicle-hours in the network during the period  $\tau$ , i.e.  $\Sigma x_i / \Sigma t_i$ , where  $x_i$  and  $t_i$  are the distance travelled and the time spent in the network, respectively, by vehicle i, and the

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The average concentration K (in vehicles per lane-mile), for the same period, is the time average of the number of vehicles per unit lane-length in the system. Letting N(t) denote the number of vehicles in the system at time t, and L the total lane-miles of roadway, then

$$K = (1/t) \int [N(t) / L] dt,$$
  
t<sub>0</sub>

. ...

where  $t_0$  is the beginning of the observation period. Effectively, K can be simply calculated by dividing the total vehicle-hours (during t) by tL, where L is the total lanemiles of roadway. One of the key advantages of using simulation experiments is that one can maintain a constant concentration level in the network, by keeping the number of circulating vehicles constant over the period t. This strategy has been adopted in all the experiments discussed herein. The concentration is then simply equal to the known total number of vehicles in the network divided by L.

The average network flow Q is interpreted as the average number of vehicles that pass through a random point of the network, and given by  $(\sum l_i q_i)/(\sum l_i)$ , where  $q_i$  and  $l_i$  respectively denote the average flow (during t) and the length of link i, and the summations are taken over all network links.

Another key variable of interest is  $f_s$ , the average fraction of stopped vehicles over the observation period. It is an important descriptor of the productivity of an urban traffic network, and is suggested by the dichotomization of traffic in the network into moving and stopped vehicles. The variation of  $f_s$  with the prevailing network concentration K is one of the principal relations considered here, as seen later in this section. Other two-fluid variables of interest are the average running time  $T_r$ , stopped time  $T_s$  and total trip time T, all per unit distance; of course,  $T=T_r+T_s$ . The main result of the two-fluid theory is a model relating  $T_r$  to T (or  $T_s$ ), that is invoked in all the following derivations. A detailed presentation of the two-fluid model assumptions and derivations will not be given here as it can be found elsewhere (Herman and Prigogine, 1979; Herman and Ardekani, 1984); the results necessary for the derivations in this chapter are presented as needed. Note one pertinent result used in our simulations to calculate  $f_s$ , namely that  $f_s = T_s/T$ , derived mathematically by Herman and Ardekani (1984) under steady-state conditions, and verified numerically in earlier simulation experiments.

#### 4.2.2. The Traffic Models and Their Interrelation

The characterization of traffic network performance is provided by a set of relations among the variables V,K,Q and  $f_s$ , in addition to the two-fluid relation between T,  $T_r$  and  $T_s$ , which has the following form:

$$T_{r} = T_{m}^{[1/n+1]}T^{[n/n+1]}$$
(1)

The parameter  $T_m$  is simply the inverse of  $V_m$ , interpreted as the average maximum running speed in the network (i.e. without any stopping), whereas the parameter n captures the sensitivity of running speed to the fraction of vehicles stopped in the network, and can serve as an indicator of quality of traffic service in a network (Herman and Ardekani, 1984).

The other relations comprising each model system are:

$\mathbf{V} = \mathbf{v}(\mathbf{K})$		$\mathbf{f}_{\mathrm{S}} = \mathbf{f}(\mathrm{K})$
$\mathbf{Q} = \mathbf{q_1}(\mathbf{K}),$	and	$\mathbf{Q} = \mathbf{q_2}(\mathbf{V}).$

Given a mathematical form for any one of the above relations, the functional forms of the remaining relations can be analytically derived by invoking one, or both, of the following:

1) the identity Q=KV, known to hold for individual roads, has been numerically verified, in earlier simulation work (Mahmassani *et al.*, 1984), to hold at the network level as well. Further evidence to this effect is also offered in this chapter for a more extensive set of simulations.

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2) The two-fluid model, which effectively provides a relation between  $f_s$  and V, since T=1/V (by definition) and  $f_s=T_s/T$ . In this work, we assume the two-fluid model to hold, though comments about the range of applicability of this assumption are also given on the basis of the simulation results.

In each of the three model systems discussed in this paper, a different functional form will be postulated for either the speed-concentration relation v(K), or for the fraction of vehicles stopped-concentration relation f(K). The functional form for the other relation is then derived from the postulated model, by invoking the two-fluid postulate, which states that:

$$V_r = V_m (1 - f_s)^n$$
, (2)

thereby specifying the dependence between  $V_r$ , the average speed of the moving vehicles in the network, and the average fraction of cars that are moving, over the observation period,  $f_r = 1-f_s$ .

The functions  $\mathbf{v}(K)$ ,  $\mathbf{f}(K)$ ,  $\mathbf{q}_1(K)$  and  $\mathbf{q}_2(V)$  are different in each of the three model systems, as they depend on the starting assumption regarding either  $\mathbf{v}(K)$  or  $\mathbf{f}(K)$ . Then, since  $V = V_r f_r = V_r (1-f_s)$  (by definition of the corresponding averages), we obtain, using Eq. 2:

$$V = V_m (1 - f_s)^{n+1}.$$
 (3)

Then, if f(K) is given, substituting it for  $f_s$  in Eq. 3 yields v(K), as follows:

$$V = V_m (1 - f(K))^{n+1}$$
 (4)

Similarly, if v(K) is given, substituting it for V in Eq. 3 allows the derivation of a functional form for f(K):

$$v(K) = V_m (1-f_s)^{n+1},$$
 (5)

which can be rewritten as:

$$f_s = 1 - (v(K)/V_m)^{[1/n+1]}$$
 (6)

The functions  $q_1(K)$  and  $q_2(V)$  can then be easily obtained by substituting v(K) into the identity Q = KV. In the first set of models discussed in this chapter, Ardekani and

Herman's (1987) postulated form for f(K) provides the starting point. The other two model systems are based on two alternative functional forms for v(K), both of which have been used in conjunction with individual streets and highways, as discussed in section 4.4. Before discussing the specific functional forms for each of the three model systems, the simulation experiments conducted to calibrate the models are described.

# **4.3. THE SIMULATION EXPERIMENTS**

In this section, we first present a general description of the simulation experiments, including the common basic network configuration used. Next, we give pertinent information about the individual simulation runs. Additional detail on all these aspects can be found in Williams (1986).

#### 4.3.1. General Description

A series of six simulation runs was performed to evaluate the network flow models of interest; several simulation experiments were also conducted to examine the network's performance in response to the various network features of interest, described in the next chapter. Each of these runs used the same basic network configuration and features, but involved a different vehicular concentration level. As noted earlier, the network is treated as a closed system, with a fixed number of vehicles maintaining a constant concentration throughout the observation (accumulation) period. The circulation of the vehicles is controlled by an elaborate set of detailed microscopic rules (governing car-following, queue discharge, lane switching, gap acceptance, and so on) embedded in the NETSIM package (PMM, 1973; FHWA, 1980). Note that some modification of the code was necessary in order to keep track of stopped versus running time in a manner that is consistent with the two-fluid definitions of these variables (see Williams [1986] for additional detail on these modifications).

The basic network configuration consists of 25 nodes, arranged in a 5-node by 5node square, connected by two-way, four lane streets forming a regular, CBD-like grid, as shc not Eac linh are to a and

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by 5rid, as shown in Fig. 4.1. In designing this network, we sought a degree of regularity that would not interfere nor mask the effect of the principal features investigated in the simulations. Each two-way street is represented by a pair of directed (one-way) links (80 in all). All links used in these simulations are 400-ft long, with no special geometric features. Vehicles are injected into the network via 12 additional entry links placed around the perimeter, three to a side, with each entry link connecting a source node (not part of the 25 network nodes, and numbered 801-812 in Fig. 4.1) to a non-corner boundary node.

Each network node corresponds to a signalized intersection, except for the four corner nodes, which are unsignalized since they present no conflicts to the drivers. Timing of signals at the interior nodes followed a two-phase timing scheme with a 50-50 split and no protected turning movements. Three-phase signals were used at the boundary nodes, providing a protected left turn for vehicles reentering the interior of the system, with the green time nearly equally allocated to vehicles leaving the interior of the network and those reentering it from the boundary. Two-way progression at the mean desired speed (35 mph in this case) was provided along the interior arterials by using 40-sec cycle length with single alternate operation.

Once the desired number of vehicles entered the network, they were not allowed to exit (no sink nodes were specified), thereby maintaining the concentration constant. At the interior intersections, 10% of the traffic turned left, 15% turned right, and the remaining 75% continued straight through. When vehicles reached a boundary node, they split equally between left and right turns, except at the corner nodes, where no choice is available. These traffic movements were used throughout the work reported herein. However, it should be recognized that the circulation pattern can itself be an important determinant of the network's performance. Results to that effect, using different turning percentages, are reported in Mahmassani et al. (1984).

Essentially, each simulation run yields one data point, consisting of values of the desired network-level average quantitites taken over the observation period (generally about



FIGURE 4.1: NETWORK CONFIGURATION. NOTE THAT NODES 801 TO 812 ARE SOURCE NODES AND AS SUCH ARE NOT PART OF THE CIRCULATION NETWORK.

thems metho bound 15 minutes of accumulation, following an initial startup and loading period ranging from 5 to 15 minutes, as described below. The network concentrations in these runs are approximately 10, 20, 40, 60, 80 and 100 vehicles/lane-mile (the actual values, determined by simulation input practicalities, are 9.90, 19.80, 41.58, 61.38, 81.18, and 100.65 vehicles/lane-mile), representing a range from very light to extremely heavy traffic. For comparison purposes, the highest concentration observed in field work by Ardekani (1984) was approximately 30 vehicles/lane-mile in the Austin CBD during heavy traffic conditions. For all practical purposes, network concentrations in excess of 50 vehicles/lane-mile can be considered as very high, and are rather unlikely in actual operations. Therefore, the simulation results allow us to explore network behavior over a wide spectrum of concentrations, including conditions near saturation, which may not be easy to observe in actual street networks. The specifics of the simulation experiments conducted to examine the effect of network features on system performance are discussed in conjunction with the corresponding factor of interest.

#### 4.3.2. Individual Runs

Individual runs consisted of three periods: the loading, network stabilization, and observation (or accumulation) periods. The first, the loading period, is necessary since each run begins with an empty network. As mentioned earlier, vehicles were loaded via the entry nodes (numbered 801-812 in figure 4.1), and the time required for this period depended on the desired network concentration for the particular run and the capacity of the signalized intersection where the vehicles actually entered the network (nodes 12-14, 21, 25, 31, 35, 41, 45, and 52-54). The loading periods in the simulations reported in this and the following chapters ranged from five to thirty-five minutes.

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The second period, network stabilization, allows the vehicles to distribute themselves over the network once no additional vehicles are generated. Two primary methods were used to determine network stability: (1) flow, averaged separately over the boundary and interior links, and (2) the fraction of vehicles (and, thus, the relative

concentration) on the boundary and the interior of the network. Average flows, which were found by averaging the one-minute vehicle discharges from each link separately for the boundary and interior links, are shown in Fig. 4.2 for an illustrative 35-minute run. During the loading period (first five minutes), the average flow for both the interior and boundary links rapidly increases. The flow rates continue to increase for a couple of minutes after the loading period as the vehicles queued on the entry links enter the network. However, after eight minutes, (three minutes after the end of network loading), flow fluctuations, which are still present, occur around apparently stable values. While Fig. 4.2 shows the average flows for the interior and boundary links to be about the same, this was not the case in all runs, although the largest difference was less than 15 percent. The network was considered stable when both the average boundary and interior flows stabilized about particular values for each run (not necessarily the same values for both).

The second criterion for network stability is based on the distribution of vehicles over the boundary and interior links. Since the vehicles were not allowed to turn onto the boundary as they entered the network during loading, none of the vehicles in the network were on the boundary during the first couple of minutes of simulation. However, after circulating for eight minutes (three minutes after loading), according the the rules outlined above, the respective fraction of vehicles on the boundary and interior links appeared to stabilize around certain values. Results from a typical twenty-minute run are shown in Fig. 4.3, where the vehicle fractions appear to stabilize around 0.4 for the boundary links, and 0.6 for the interior links after the first eight minutes of simulation. Interestingly, these particular vehicle fractions closely match the ratios of the lengths of the boundary and the interior links (40 and 60%, respectively), resulting in about the same concentration on both network components. The network was considered "stable" when the vehicle fractions fluctuated about constant values (not necessarily resulting in the same concentration for the boundary and interior). However, the vehicle fractions did not deviate substantially from 0.6 and 0.4 across the various simulation runs considered in this study.

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Figure 4.2. Link Discharge for Interior and Boundary Links



Figure 4.3. Fraction of Vehicles on Boundary and Interior Links

A period of three minutes after the loading stage was found to be adequate for network stabilization under a wide range of concentrations, so long as long queues were not built up on the entry links, thereby requiring long times to clear after the network loading period. For this reason, vehicle entry was spread over long loading times at high concentrations in order to accommodate the large number of vehicles entering the network.

The third and final period of each individual run is the observation period per se, during which most of the useful information is generated. All the network-level variables of interest were accumulated or averaged only over this third period, thereby excluding the transient conditions during the loading and stabilization periods. The duration of this period for the simulations used in this investigation ranged between 12 and 15 minutes.

As noted earlier, the simulation package used in these experiments treats many of the microscopic processes stochastically. In particular, a driver characteristic code is assigned randomly (from a pre-specified, discretized approximately normal distribution) to each vehicle as it enters the network, and determines the degree to which each vehicle (driver) is "aggressive" or "timid", as reflected in the parameter values affecting decision situations such as gap acceptance and reaction times. The asssignment of the driver characteristic code depends on a string of random numbers generated within the program, which, in turn, depends on the random number seed selected by the package user. In the early stages of the research, several otherwise identical runs were made, varying only the random number seed, to determine the variability of the networkwide time (and ensemble) averages of interest in this investigation. The results clearly confirmed that the variability in these averages (when taken over an observation period of 12 to 15 minutes) due to the stochasticity in the microscopic processes is insignificant and negligible for the purpose of this analysis.

Another concern is whether individual vehicles truly experience the traffic conditions in the entire network, or get trapped in a small sector of it. The turning movement rules, which govern the circulation pattern, were specified so as to allow each ve in be in ne

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affic ning each vehicle to circulate throughout the network. It was thus desirable to verify that this was indeed taking place, and that our experimental set-up was not leading to pathological behavior. This was accomplished by examining the detailed itineraries followed by several individual vehicles; the results confirmed that vehicles were allowed to circulate in the network, with no evidence of pathologies (see Williams [1986] for more detail).

In the next section, the results of the simulations are presented and used to address the network-level traffic relations of concern to this study.

# 4.4. ANALYSIS OF TRAFFIC NETWORK MODELS

Figures 4.4 through 4.7 present the basic network-level results of interest from the above runs; Figs. 4.4 and 4.5 respectively depict the variation of speed and flow with concentration, Fig. 4.6 depicts the corresponding variation of speed with flow in these runs, while Fig. 4.7 depicts the variation of the fraction of vehicles stopped with concentration. The general similarity of the K-V-Q patterns to their characteristic counterparts for individual road sections is striking; this observation forms the basis for the functional forms explored in this section. The results of the simulations are first examined to verify that the Q=KV identity holds for the network flow under consideration.

#### 4.4.1. Verification of the Q=KV Identity

In earlier simulation experiments, the basic traffic flow identity relating speed, flow, and concentration was found to hold at the network level as well (Mahmassani *et al.*, 1984). Further evidence to that effect is also offered here for the new simulations (including those used in the analysis of network performance in the next chapter). The average flow Q (in vehicles/lane-hour) for each run is estimated by averaging, over the accumulation period, the minute-by-minute average flows taken over all links, based on the number of vehicles discharged from the downstream end of each link (each minute). Each link's discharge is first divided by two to obtain the flow on a per lane basis. Note with regard to the expression given earlier in this section for Q that the link length  $l_i$  is the same



across all links in these experiments. The other network variables, K and V, are obtained as described earlier in this section. The product KV can then be compared to the independently estimated Q.

The results of this comparison for the six runs are shown in Table 4.1, clearly illustrating the closeness of the two quantities. The small numerical discrepancies are mostly due to the one-minute discretization used in estimating Q, whereas V is determined from quantities accumulated over smaller time steps. The largest differences occur at the high concentration levels, where network operation is least stable. In addition, the independently calculated Q is plotted in Fig. 4.8 against the corresponding product KV for all the simulations conducted in connection with this study, clearly indicating a linear trend with a slope of 1. These results, coupled with earlier similar results (Mahmassani *et al.*, 1984), further confirm the validity of Q=KV at the network level as well.

Next, the three model systems are presented and discussed on the basis of their calibrated performance against the observations generated by the simulations.

## 4.4.2. Network Flow Models

The first set of models discussed is that proposed by Ardekani and Herman (1987), which starts with a postulated functional form for the  $f_s$ -K function f(K). The starting point for the other two sets of models is a postulated functional form for the network-level speed-concentration relation v(K). Given the similarity of the plots in Figs. 4.4 through 4.6 to the patterns encountered in individual road facilities, two well-known functional forms for the speed-concentration relation at the link level are considered here for the network-level variables. The first is Greenshields' widely utilized linear speed-concentration relation, while the second is the nonlinear 'bell-shaped' function, originally proposed by Drake, Schofer and May (1967) for arterials (see Gerlough and Huber (1975) for an overview of these models).

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#### 4.4.2.1. Model System 1

The starting point for this model system is the following postulated functional form for f(K), which specifies the  $f_s$ -K relation:

$$f_s = f_{s,min} + (1 - f_{s,min}) (K/K_i)^{\pi}$$
 (7)

where  $f_{s,min}$  is a parameter intended as the minimum fraction of vehicles stopped in the network,

 $K_j$  is a parameter intended as the "jam" concentration, at which the network is effectively saturated, and

 $\pi$  is a parameter that determines the fraction of vehicles stopped at a given partial concentration (K/K<sub>i</sub>), and could serve as a measure of the quality of service in a network.

The principal assumptions of this relation are reflected in its boundary conditions. In particular, it recognizes that in an urban street network, even under very low concentrations, there is some non-zero  $f_{s,min}$  fraction of stoppage that is inevitable in the network (unless traffic control is fully responsive, unlike any currently in operation, or drivers do not obey traffic laws), as suggested by simulation results (see Fig. 4.7, for example) and field studies (Ardekani and Herman, 1987). On the other hand,  $f_s$  goes to 1, meaning that all vehicles are stopped, as K goes to K<sub>j</sub>. Thus, Eq. 7 states that  $f_s$  is an increasing function of K, that varies in the range from  $f_{s,min}$  to 1 as K goes from zero to K<sub>j</sub>.

Following the steps presented in section 4.2.2, v(K), which specifies the speedconcentration relation, can then be found by substituting Eq. 7 into Eq. 4, yielding:

$$V = V_{m} (1 - f_{s,min})^{n+1} (1 - (K/K_{i})^{\pi})^{n+1}.$$
(8)

The flow-concentration relation  $q_1(K)$  is then easily found using Q=KV, as shown in the previous section:

$$Q = KV_m (1 - f_{s,min})^{n+1} (1 - (K/K_i)^{\pi})^{n+1}.$$
(9)

Model Estimation. The estimation of the parameters of Eq. 7 can be performed by rewriting it as  $f_s = a + bK^{\pi}$ , where  $a = f_{s,min}$  and  $b = (1-f_{s,min})/K_j^{\pi}$ . Nonlinear least squares estimates can then be obtained for a, b and  $\pi$ , from which the original parameters

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by ast ers can be recovered, yielding for the set of observations generated from the simulation experiments estimated values of 0.187, 134.12 vehicles/lane-mile, and 0.208 for  $f_{s,min}$ ,  $K_j$ , and  $\pi$ , respectively. Figure 4.9 depicts the curve corresponding to the estimated parameter values, and also includes the points observed in the simulation experiments for comparison purposes. It appears that the estimated model somewhat overestimates  $f_{s,min}$ . More seriously, between (the practically meaningful) concentrations of 20 and 80 vehicles/lane-mile, it predicts the opposite concavity than that suggested by the observed values.

The ability of this model to describe the speed-concentration pattern can be assessed by comparing the resulting Eq. 8 to the observed simulation results. This requires estimates of the two-fluid parameters n and  $T_m$ , which can be obtained by ordinary least squares estimation of the linear regression equation obtained by taking the natural logarithms of both sides of Eq. 1 (Herman and Ardekani, 1984):

$$\ln T_{\rm r} = (1/n+1) \ln T_{\rm m} + (n/n+1) \ln T.$$
(10)

Using all six data points, the estimates of the two-fluid parameters n and  $T_m$  were found to be 1.051 and 2.692 min/milerespectively. However, it is important to recognize that this analysis assumes that the two-fluid model continues to hold at very high concentrations, well in excess of those encountered in previous field studies. Moreover, the reliability of the simulation at very high concentrations, where conditions are inherently unstable, cannot be taken for granted. The plot of the  $\ln T_r$  vs.  $\ln T$  trend (linear under the two-fluid assumptions) for the six observed points (Fig. 4.10) suggests that the sixth point (representing the highest concentration examined) deviates from the linear trend established by the other five points. However, the simulation results are clearly in agreement with the two-fluid assumptions over the range of practically meaningful concentrations. Hence, n and  $T_m$  were re-estimated, omitting the sixth point, yielding 2.349 and 1.809 min/mile, respectively.



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Figure 4.10. Plot of  $\ln T_r$  vs.  $\ln T$  for Simulation Experiments.



Figure 4.11. Comparison of V-K Model Derived in Model System 1 with Observed Simulation Results.



Figure 4.12. Comparison of Q-K Model Derived in Model System 1 with Observed Simulation Results.

models). Greenshields' function, which forms the basis of this set of models, has the following well-known form:

$$V = V_f (1 - K/K_j),$$
 (11)

where  $V_f$  and  $K_j$  are parameters to be estimated, and respectively interpreted as the free mean speed, which is that experienced when interference from other vehicles in the traffic stream is virtually nonexistent (though vehicles must still obey traffic controls in the system), and the 'jam' concentration, defined earlier.

Note that the  $V_f$  parameter is distinct from the two-fluid parameter  $V_m$  (which is equal to  $1/T_m$ ), the average maximum running speed, which occurs when  $f_s = 0$ , i.e. when no vehicles are stopped in the network. As stated in the previous subsection, this condition does not occur in existing urban traffic systems over any meaningful length of time, even at very low concentrations, due to the presence of the traffic control system. Therefore, because the average travel time corresponding to the free mean speed will exceed the minimum running time  $T_m$  by some usually non-zero stopped time, we will always have  $V_f \leq V_m$ , and in most cases  $V_f < V_m$ . Note that in the first model system discussed above,  $V_f = V_m (l-f_{s,min})^{n+1}$  (by setting K=0 in Eq. 8).

The functional form for f(K), the  $f_s$ -K relation that is compatible with the above linear V-K model and the two-fluid model, is found following the steps presented earlier. Namely, by substituting Eq. 11 into Eq. 6, we obtain:

$$f_s = 1 - [(V_f / V_m) (1 - K / K_j)]^{1/n+1}.$$
(12)

This function has similar boundary conditions as Ardekani and Herman's, since  $f_s=1-(V_f/V_m)^{1/n+1}$  for K=0, and  $f_s=0$  for K=K<sub>j</sub>. However, here the minimum fraction of vehicles stopped,  $f_{s,min}$ , is explicitly stated in terms of the speed parameters  $V_f$  and  $V_m$ . For instance, it becomes clear in this expression that if  $V_f = V_m$ , then  $f_s = 0$  at K = 0.

Finally, the flow-concentration relation is again obtained by applying Q = KV:

$$Q = V_{f} (K - K^{2}/K_{j}).$$
(13)

Model Estimation.Least squares estimates of the model parameters can be easily obtained since Eq. 11 is linear in K. Using the observed simulation data of Fig. 4.4, the estimated values are 18.02 mph and 116.3 vehicles/lane-mile for  $V_f$  and  $K_j$  respectively. The resulting calibrated functions, along with the observed values, are plotted in Figs. 4.13 and 4.14, for Eqs. 11 and 13 respectively, exhibiting in both cases a rather close fit to the data. Moreover, the free mean speed does not appear to be underpredicted; however, because Eq. 11 ignores the slight nonlinear trend exhibited by the K-V data, the speed is slightly overpredicted in the middle concentration range, resulting in an overprediction of the flow in the same range (Fig. 4.14).

Note that there is no need to exclude the sixth data point, for the highest K (as in 'method 2' in the previous section), in estimating the parameters of Eq. 11, because the postulated speed-concentration and resulting flow-concentration relations appear to be consistent with the pattern exhibited by the data, including the range corresponding to that high concentration point. The main justification for excluding that point in the previous section is that the discrepancy appears with regard to the two-fluid model assumption's applicability at higher concentrations. Since v(K) has been specified directly here, this assumption has no direct bearing on the parameter estimates presented so far in this subsection. This is however not the case when Eq. 12 is evaluated for the  $f_s$ -K relation, since this function's parameters are not estimated directly on the  $f_s$ -K data, but from the two-fluid and V-K models separately (just as the parameters of the V-K relation in the first model system were not directly estimated using the corresponding V-K data), as discussed hereafter.

Assessment of the  $f_s$ -K function in this model system requires the estimation of the two-fluid parameters, n and  $T_m$ . Those found by methods 1 and 2 in the previous section are both used here. The results are plotted, along with the observed data, in Fig. 4.15. If method 2 is used in the two-fluid estimation, the resulting  $f_s$ -K curve provides a much better fit to the data, up to a concentration of about 80 vehicles/lane-mile, than that obtained



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Figure 4.13. Comparison of Linear V-K Model with Observed Simulation Results.



Figure 4.14. Comparison of Q-K Model Derived from Linear V-K Relation with Observed Simulation Results.



Figure 4.15. Comparison of f -K Model Derived from Linear V-K Relation with  $^{\rm S}$  Observed Simulation Results.

by method 1. As with the first model, this model's concavity is opposite to that exhibited by the data in the middle range of concentrations. What is interesting however is that this model's fit to the  $f_s$ -K data, with which it was not directly calibrated, is almost as good as that obtained with Eq. 7, which was directly calibrated using that data. Actually, neither model seems capable of reflecting the concavity of the data over the middle range of concentrations, nor with the apparent inflection point prior to the higher concentration values.

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#### 4.4.2.3. Model System 3: Nonlinear V-K Relation.

The second postulated functional form for v(K) is a nonlinear 'bell-shaped' function, originally proposed by Drake *et al.* (1967) for arterials, that could capture the apparent shape of the speed-concentration data in Fig. 4.4:

$$V = V_{f} \exp[-\alpha (K/K_{m})^{d}]$$
(14)

where  $V_f$  (previously defined),  $K_m$ ,  $\alpha$ , and d are parameters to be estimated. The resulting expressions for the  $f_s$ -K and Q-K models are then obtained as shown previously, yielding:

$$f_{s} = 1 - \{ (V_{f}/V_{m}) \exp[-\alpha (K/K_{m})^{d}] \}^{1/n+1}, \text{ and}$$
(15)  
$$Q = KV_{f} \exp[-\alpha (K/K_{m})^{d}].$$
(16)

It can be shown, by solving dQ/dK = 0, that  $K_m$  is the concentration at which maximum flow occurs in the network.

**Model Estimation Results.** Estimation of the parameters of Eq. 14 can be accomplished by nonlinear least squares after some manipulation. Taking the natural logarithms of both sides of the equation, and rearranging the last term on the right-hand side, we obtain:

$$\ln V = \ln V_{f} - (\alpha / K_{m}^{d}) K^{d}, \qquad (17)$$

which is of the form  $\ln V = c_0 + c_1 K^d$ . Nonlinear least squares estimates can then be found for  $c_0$ ,  $c_1$  and d, and it is then possible to recover  $V_f = \exp(c_0)$ . But, since  $c_1 = (\alpha/K_m^d)$ , and only  $c_1$  and d are known, it is not possible to obtain unique values of  $\alpha$  and  $K_m$ . However, this is not particularly problematic from the standpoint of the model's performance, since only the value of  $c_1$  is necessary. Using the observed simulation results, the parameter estimates are 1.49, 17.95 miles/hour, and  $1.83 \times 10^{-3}$  for d,  $V_f$  and  $c_1$  respectively. In order to have an idea of the approximate magnitude of  $\alpha$ , the property that  $K_m$  represents the concentration at maximum flow can be used. Noting from Fig. 4.5 that the maximum flow occurs for a concentration between ~60 and ~65 vehicles/lane-mile, a range of  $\alpha$  can be calculated given the estimated values of  $c_1$  and d, yielding a range from ~0.81 (for  $K_m$ =60) to ~0.91 (for  $K_m$ =65).

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Figure 4.16 shows that this model provides a close fit to the observed speedconcentration data throughout its range. The resulting flow-concentration model, given by Eq. 16, is plotted in Fig. 4.17, along with the observed points. Unlike the relation derived from the linear V-K model, Eq. 16 is not symmetric, and exhibits asymptotic decay of flow as the concentration increases. The model does however provide generally close agreement with the observed data.

The estimated values of the two-fluid parameters are again used in examining the descriptive ability of the corresponding  $f_s$ -K relation (Eq. 15). This function is plotted in Fig. 4.18, for the two sets of two-fluid parameter estimates presented earlier. The curve with the parameters found by method 2 (i.e. excluding the last data point) provides much closer agreement with the corresponding five points than that using the method 1 estimates, as the latter seem to be noticeably influenced by the highest concentration point. Unlike the previous model, maximum  $f_s$  (equal to 1 for plausible signs of the parameters) is approached asymptotically . Whether this behavior is 'correct' or not is difficult to determine, even in a simulated system, given that it would require loading the network to very unrealistic levels. Moreover, the performance of the derived  $f_s$ -K model does not depend only on the postulated V-K function, but also on the two-fluid model invoked in its derivation. As seen earlier, the simulation data appeared to significantly depart from the two-fluid trend at higher concentrations. Nevertheless, Eq. 15 seems to capture the



Figure 4.16. Comparison of Bell-Shaped V-K Model with Observed Simulation Results.

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Figure 4.17. Comparison of Q-K Model Derived from Bell-Shaped V-K Relation with Observed Simulation Results.





network's performance quite well for the range of concentrations that are likely to be encountered in actual urban traffic networks.

#### 4.5. SUMMARY AND CONCLUDING COMMENTS

The principal conclusion from the work presented in this chapter is that it is possible to characterize traffic flow in urban street networks using relatively simple macroscopic models relating the principal networkwide traffic variables. Furthermore, it is remarkable that these relations appear to be not unlike those that have been established at the individual facility level. As illustrated in this paper, the characteristic shape of the fundamental traffic relations encountered for highways and arterials, and upon which traffic engineering procedures have been built, seem to be present at the network level as well, despite the complex interactions that take place in urban street networks.

In terms of the relative performance of the three sets of models presented in this chapter, all three seem to provide a more or less reasonable approximation of the patterns exhibited by the simulated data, at least over certain ranges of concentration. Model systems 2 and 3 provided a much better fit to the speed-concentration data (relative to the derived model in the first system), over the full range of observations; however, this is to be expected since they were calibrated using that data. Generally, the relation between the fraction of vehicles stopped and concentration remains the most problematic in terms of finding a model that is sufficiently convincing over the full concentrations spectrum. However, the performance of the derived models was quite good for concentrations up to about 80 vehicles/lane-mile, already well in excess of realistic values that might be encountered in actual networks. Generally, the nonlinear v(K) function yielded a better set of models in terms of agreement with the simulation results. However, the linear approximation for that same relation, on which the second set of models was based, might offer the advantage of familiarity and ease of comparability.

Still focusing on the less than 80 vehicles/lane-mile concentration range, the results in this chapter provide another demonstration of the two-fluid model's validity. This model served as the principal theoretical bridge between the postulated v(K) function and the corresponding f(K) model. In both the second and third sets of models, the derived model performed quite well against the observed data, even though it was not directly calibrated using that data. However, the behavior of the various network variables at very high concentrations remains to be understood. Based on the simulation results presented here, the applicability of the derived functions at these levels decreased markedly, suggesting that the two-fluid assumptions might not directly extend to these high concentration levels. For instance, it is possible that the relation between  $\ln T_r$  and  $\ln T$  may be nonlinear over the full spectrum of concentrations, though it can be treated as effectively linear over most of the practically meaningful range of concentrations.

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Naturally, since the results presented here are based on a limited set of simulated experiments, they must be interpreted in an exploratory sense aimed at stimulating further inquiry into this problem area. These simulations have been performed for a relatively small network, under controlled conditions, and subject to the microscopic rules embedded in the NETSIM package. However, the results appear to correspond well with the limited field studies conducted to date. Simulations of the kind described here have been very useful in supporting the continued development of network-level traffic flow relations and the investigation of their properties. While simulations in larger, more elaborate networks will undoubtedly provide useful information to advance knowledge on this topic, it is essential to obtain networkwide data on the operation of actual urban traffic systems. The cost and the scale of the problem may appear discouraging; however, technological developments in remote-sensing, telecommunications, opto-electronics, among others, offer challenging opportunities for learning about the workings of traffic in urban areas.

To more completely characterize the performance of urban traffic networks, it is desirable to the understand the sensitivity of the above macroscopic relations and

parameters to various network features. Indications along these lines are presented in the next chapter, with regard to the effect of network link width and length, of traffic timing coordination, and of the intensity of interfering events. In that analysis, and given the results seen in this chapter, parameters will be estimated only for the set of models based on the nonlinear form for v(K).

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#### CHAPTER 5

#### PERFORMANCE OF TRAFFIC NETWORKS: EFFECT OF SYSTEM FEATURES

#### 5.1. INTRODUCTION

The comparison of the three sets of network-level models was conducted in the previous chapter using simulations performed under one set of network conditions. In this chapter, we continue the investigation of a traffic network's overall performance, focussing on the factors that significantly affect the quality of service that it offers. This is accomplished by systematically varying the specified network conditions and examining the response in terms of the network-level relations and their parameters. As concluded in the previous chapter, the model system derived from the nonlinear "bell-shaped" curve for the speed-concentration relation (model system 3) as well as the two-fluid model parameters are used in this chapter to describe the network's response to the various factors.

Three broad categories of factors can be thought to affect a traffic network's performance: 1) topological features, 2) traffic control and 3) traffic activity patterns. These are discussed in turn hereafter, along with the corresponding factor levels considered in this investigation.

The first category includes the configuration of the network (e.g. grid, radial, irregular) and the physical characteristics of its components (e.g. street width, block length, and other geometric design chatracteristics). Only a grid network is used in this study, with street links varying in width from two to six lanes and in length from 400 to 1000 feet.

The factors in the traffic control category primarily include intersection control, signal timing and coordination schemes, as well as movement restrictions, speed control, and the battery of actions available to traffic engineers in controlling flow. The effects of signal timing on network performance are examined in this chapter for three alternative control strategies: 1) coordination for "perfect" progression, 2) simultaneous operation (all traffic signals begin their north-south green phase simultaneously, then begin their east-

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fact traff furth does serv west green phase together), and 3) random offsets, when the traffic signal cycles begin at randomly designated times. Of course, many other network factors can be included in traffic control, but are not investigated in this work, such as one-way street designation, speed limits, turn prohibitions, and protected turns at intersections.

The third category, referred to as traffic activity patterns, broadly encompasses the circulation patterns of vehicles in the network, resulting from trip routing and timing decisions, as well as the frequency and intensity of interfering occurrences (e.g. temporary lane blockages due passenger or package pick-up or delivery, parking manoeuvres) associated with a particular adjoining land use and activity pattern. The behavioral characteristics of motorists would also be included in this category. Indirectly, land use is an important element to the extent that it generates trip patterns and affects interfering activity. In future work, this category should be separated into two types of factors: 1) the more global trip patterns, resulting from the spatial distribution of residences, businesses, economic and social activities, and 2) the more local effect of interfering events, directly reflecting the intensity of urban activities adjoining the street network. The first type would then provide the currently missing linkage between the evolving spatial patterns in the urban area and their effect on the traffic system's performance. In this chapter, the investigation is limited to the effect of the interfering activities, which can be modelled as temporary blockages of the right lane, arising with different frequencies and over different durations. The "short-term" events capability of the NETSIM package is used for this purpose.

Clearly, this is not intended as a comprehensive or exhaustive assessment of the factors determining network performance, but as illustrative of the phenomena affecting traffic network performance, and of the direction that future work can take in seeking a further understanding of these phenomena within the framework proposed in this study. It does however begin to give answers about the relative magnitude of benefits in traffic service quality that could be reasonably expected under different types of improvements.

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The general approach for these comparisons consists of performing a series of simulation runs for each level of the experimental factor under consideration. Each run corresponds to a concentration level that is maintained constant throughout the simulation, as before. For the topological factors of link width and block length, as well as for the traffic signal timing coordination factor, each series consisted of five simulation runs, with target concentrations of 8, 20, 40, 60 and 80 vehicles/lane-mile; higher concentrations were not included in light of the results of the previous chapter. For the traffic interfering activities factor, only three simulation runs were performed, with target concentrations of 20, 40 and 60 vehicles/lane-mile, as discussed in section 5.4. The actual concentrations, though quite close to the target values, do not exactly match them due to the manner in which vehicles are loaded onto the network, as described in the previous chapter. Basically, the network configuration and all the simulation details for this investigation are the same as those used for the analysis of chapter 4, with the exception of those elements corresponding to the particular factor under investigation. These are detailed in conjunction with the discussion of the particular experimental factor under consideration. The next section addresses the network topology factors, followed by the traffic control factor in section 5.3. The effect of traffic interfering activities is examined in section 5.4, and concluding comments are presented in section 5.5.

## 5.2. NETWORK TOPOLOGY

We first examine the effect of the block length on network performance, followed by that of the street's number of lanes.

### 5.2.1. Link Length.

The variation of block length is generally not an option that a traffic engineer can turn to in trying to solve traffic problems in an existing system. However, examination of this factor yields insight into the effects on network traffic performance of the frequency of intersection interference (such as turning traffic and the associated delays incurred by both the of res

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in T conf para case prev exhil beha the through and turning traffic). Thus the general results pertaining to this factor would be of practical interest when considering a grade separation at a busy intersection, and the resulting insights useful in comparisons of network operations in cities with different characteristics as well as in the planning of new or rapidly developing communities.

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Three levels for the block length factor are considered: 400, 700 and 1000 feet, with the base or reference case being the 400 ft. length. In the simulation experiments, all other factors were unchanged. The resulting network-level V-K, Q-K, and  $f_s$ -K relations for these conditions are shown in Figs. 5.1, 5.2, and 5.3 respectively. The principal effect of link length on the network V-K relation is, as expected, higher average network speed for longer links, particularly at the lower concentrations. Longer links, resulting in greater distances between traffic signals, provide the opportunity to spend a higher fraction of time at or close to one's desired speed; however, at higher concentrations, this ability is offset by increasing congestion, thereby greatly reducing the influence of link length. The  $f_s$ -k curves in Fig. 5.3 indicate a general trend of decreasing average fraction of vehicles stopped, at a given concentration, with increasing block length. The improvement due to longer blocks is actually more dramatic at higher concentrations, with the fraction of time stopped reduced by about 30% as block length is increased from 400 to 700 ft., and by an additional 20% as it is increased to 1000 ft. (at the highest concentration level considered in this analysis).

Estimates of the parameters of the nonlinear v(K) (Eq. 14 in chapter 4) are shown in Table 5.1, and those of the two-fluid n and  $T_m$  are given in Table 5.2. These values confirm that the free mean speed,  $V_f$ , increases with the link length, along with the parameter  $\alpha$  (note however that the values of  $\alpha$  shown assume a constant  $K_m$  across all cases, because these two parameters cannot be independently identified, as discussed in the previous chapter), while d exhibits no particular pattern. Both of the two-fluid parameters exhibit clear patterns, with n increasing sharply, while  $T_m$  decreases, with link length. The behavior of  $T_m$  is expected and conforms to intuition; that of n is more subtle. The



Figure 5.1. Effect of Block Length: Speed-Concentration Relation



Figure 5.2. Effect of Block Length: Flow-Concentration Relation





# Table 5.1Parameter Estimates for Speed-Concentration Model:Effect of Block Length

Block Length (ft)	V <sub>f</sub> (mph)	b lifter	$\alpha^{\dagger}$
400	18.584	1.225	0.829
700	27.892	0.914	1.173
1000	29.598	0.979	1.204

<sup>†</sup>Note: Assumes that K<sub>m</sub> = 60 vch/lane - mile

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#### Table 5.2 Two-Fluid Parameter Estimates: Effect of Block Length

Block Length (ft)	n	T <sub>m</sub> (min/mile)
400	2.349	1.809
700	4.876	1.195
1000	8.148	0.878

# Table 5.3 Parameter Estimates for Speed-Concentration Model: Effect of Link Width

Link Width Number of Lanes	V <sub>f</sub> (mph)	d	$\alpha^{\dagger}$
400-ft. Links			
1	18.210	1.232	0.733
2	18.584	1.225	0.829
3	18.297	1.334	0.863
1000-ft. Links			
1	27.708	1.025	1.037
2	29.598	0.979	1.204

<sup>†</sup>Note: Assumes that  $K_m = 60$  veh/lane - mile

parameter n can be thought of as the approximate slope of the  $T_s$  vs. T trend; higher n values then indicate that average (total) trip time T is increasing with concentration at a faster rate than average stopped time Ts. This occurs in longer blocks because the average running time  $T_r$  (also the difference between T and  $T_s$ ) is more sensitive to congestion, since longer block distances allow higher average running speeds at low concentration.

#### 5.2.2. Link Width (Number of Lanes).

This factor has more direct traffic engineering applicability, as the number of travel lanes on city streets can be manipulated through changes in parking regulations, restriping or low-cost physical improvements. Parking may be eliminated or allowed along city streets, increasing or decreasing, respectively, the number of travel lanes by one for each side of the street affected. In addition, parallel parking may be converted to angle parking, or vice versa, generally reducing or increasing the number of travel lanes by one; (conversion from parallel to angle parking along a street also has serious safety considerations, which may override traffic flow considerations). Of course, lanes may be added or dropped by construction, generally at the expense or in favor of sidewalks and other pedestrian amenities.

The effect of link width on the network parameters is examined by considering link widths of one, two, and three lanes, for a network with 400-ft. block lengths, and widths of one and two lanes for a network with 1000-ft. block lengths. Only two link widths were considered for the latter network primarily because of computational cost considerations, given the very large number of vehicles needed to maintain the desired vehicular concentration. It is important to note in this regard that the comparisons in this section are made, as before, at constant concentration; thus, when a lane is added in the simulation, the number of vehicles is increased accordingly. Of course, when a lane is added in the field, there is generally no immediate corresponding increase in concentration, resulting in an improvement in service quality. What is examined in this analysis then is the effect of link width in terms of the greater freedom to maneuver when more lanes are available, and the

associated possibility of avoiding left-turning vehicles waiting for a gap in the opposing stream, etc.

The V-K, Q-K, and  $f_s$ -K relations for the three widths associated with the 400-ft. network are shown in Figs. 5.4, 5.5, and 5.6, respectively. As expected, the primary differences are manifested in the Q-K relation (Fig. 5.5), with average network flow increasing dramatically with the number of lanes, due to the larger number of vehicles required to maintain constant concentration. However, the differences are minimal on a per lane basis. The other two relations do not exhibit dramatic differences across link widths. An improvement in average speed can be noted at higher concentrations for the wider links, for the reasons mentioned above; for these same reasons, virtually no differences exist at low concentration, since interference from other vehicles is very limited then. Plots of the above relations for the network with 1000-ft. links, shown in Figs. 5.7, 5.8 an 5.9, in the same order as before, reveal similar results to the case with 400-ft. links, suggesting that the qualitative effect of number of lanes seems to be independent of link length.

The parameter estimates are presented in Tables 5.3 and 5.4, confirming that  $V_f$  does not vary significantly across the three cases. While the estimates of n (in table 5.4) exhibit little change between one and two lanes, it drops noticeably when the widths are increased to three lanes (for the 400-ft. network). This is due to the slower deterioration of the average running time with increasing concentration when drivers enjoy the greater freedom afforded by the greater number of lanes. It is nonetheless notable that this benefit seems to follow a threshold pattern, with meaningful improvement appearing in thetransition from two to three lanes. Similarly,  $T_m$  increases when the link widths are increased to three lanes, but shows little change between one and two lanes.

## 5.3. TRAFFIC CONTROL

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Three levels of traffic signal control are examined: 1) traffic signal interconnection to provide "perfect" progression, with the signal turning to green as it is reached by the



Figure 5.4. Effect of Link Width, 400-ft. Links: Speed-Concentration Relation



Figure 5.5. Effect of Link Width, 400-ft. Links: Flow-Concentration Relation



Figure 5.6. Effect of Link Width, 400-ft. Links: f\_-K Relation



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Table 5.4 Two-Fluid Parameter Estimates: Effect of Link Width						
Link Width Number of Lanes	n	T <sub>m</sub> (min/mile)				
400-ft. Links						
1	2.328	1.833				
2	2.349	1.809				
3	1.897	2.365				
1000-ft. Links						
1	8.963	0.708				
2	8.148	0.878				

# Table 5.5Parameter Estimates for Speed-Concentration Model:Effect of Signal Coordination

Control Scheme	V <sub>f</sub> (mph)	d	α
No Short-Term Events Sp	Decified		
Single Alternate Random Offset Simultaneous	29.598 28.541 25.128	0.979 1.005 1.175	1.204 1.170 1.030
With Short-Term Events	Present		
Single Alternate Random Offsets Simultaneous	31.170 30.086 25.345	0.860 0.881 1.100	1.284 1.258 1.062

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incoming platoon from the upstream intersection; 2) simultaneous operation, with all signal cycle beginning at the same time; and 3) isolated operation, with the signal cycles beginning at randomly selected times. Because the average desired speed of the vehicles in the network is 35 miles/hour, a network using 1000-ft. links was necessary in order to provide "perfect" progression over a reasonable distance through the network. Since a 40-second cycle length is used throughout this simulation, 1000-ft. links provide near-perfect progression using a single alternate offset scheme. Simultaneous operation was achieved by assigning identical offsets to all twenty-five traffic signals. These offsets yield the opposite signal indication at the immediately downstream intersection from that obtained under the single alternate progression, thereby guaranteeing that a vehicle travelling straight through at the average desired speed will stop at each intersection. Finally, isolated uncoordinated operation was simulated by using randomly selected offsets for each signal.

The V-K, Q-K, and  $f_s$ -K results are shown in Figs. 5.10, 5.11 and 5.12. The differences due to traffic control initially appear to be much less overwhelming than those due to the geometric features of the network examined in the previous section. Moreover, it is difficult to generalize when the same control strategy is used at all concentration levels. The nature of traffic control is such that it must be adapted to prevailing conditions, including concentration. Nevertheless, the single alternate scheme that provides progression along major directions seems to yield the highest average speed, and the lowest fraction of vehicles stopped, particularly at lower concentration, as expected. As concentration increases, the superiority of the progressive scheme becomes less evident. It should be noted however that the differences among the three timing strategies observed for concentrations up to ~40 vehicles/lane-mile are quite meaningful. Keeping in mind that the peak observed concentrations in field work in Austin and Dallas do not exceed ~30 vehicles/lane-mile, the practical significance of the above conclusions should not be dismissed on grounds that all schemes are equally bad under very heavy congestion; an

average network concentration of ~25 vehs/lane-mile already describes a heavily congested situation for most motorists circulating through the network.

In addition, the effect of traffic signal timing coordination was tested in conjunction with the "interfering traffic activities" factor, by conducting an additional series of simulation runs for each signal control strategy, but with the activation of the "short-term events" option in the simulation program. As described in more detail in the next section, this option provides an "activity level" which simulates interference to moving vehicles, in addition to that caused by the other moving vehicles, through the temporary blockage of a link's right lane. Introduction of these events, resulting in increased congestion (particularly at the higher concentration levels), further impedes the moving traffic, restricting the vehicles' ability to move at their desired speed (such as in the progression band). The short-term events were specified to occur stochastically, with a mean frequency of 30 times per hour (mean rate), and mean duration of 25 seconds each; this activity level is denoted AL1 in the next section, where the effects of the activity levels are specifically addressed). The results of these simulations with the "short-term events" option are shown in Figs. 5.13, 5.14 and 5.15, indicating the same general conclusions as in the case without interfering activities. The improvement due to progression timing is somewhat reduced in the presence of these short term blockages, since these further contribute to congestion in the system. Nevertheless, improvement at lower concentration can be of practical significance.

The parameter estimates are presented, for both cases (with and without short term events), in Tables 5.5 and 5.6, confirming the above comments regarding the effect of timing on  $V_f$ . The rank order of the magnitudes of the two-fluid parameter  $T_m$  for the three cases parallels that of  $V_f$ . On the other hand, the two-fluid parameter n does not exhibit a similarly consistent pattern. It is interesting to note that n increased as the timing went from random (isolated operation) to coordinated progression. While overall service quality is better under coordination, based on the other indicators discussed here, the increase in n is



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Figure 5.10. Effect of Traffic Control: Speed-Concentration Relation



Figure 5.11. Effect of Traffic Control: Flow-Concentration Relation



Figure 5.12. Effect of Traffic Control: f -K Relation



**CONCENTRATION ( vehicles/lane-mile )** 

Figure 5.13. Effect of Traffic Control (with Traffic Interfering Activities): Speed-Concentration Relation



Figure 5.14. Effect of Traffic Control (with Traffic Interfering Activities): Flow-Concentration Relation



Figure 5.15. Effect of Traffic Control (with Traffic Interfering Activities):  $f_s$ - K Relation

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due to the same type of phenomenon that resulted in a higher n for longer block length, discussed in the previous section. Essentially, progression allows drivers to achieve higher running speeds when moving, and therefore makes the average running speed relatively more sensitive to increasing concentration.

## 5.4 INTERFERING ACTIVITY LEVEL

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In this section, we consider the effect of differing levels of traffic-interfering activity in the test network on the quality of traffic service. The "activity level", for the purpose of this study, refers to the degree of interference experienced by moving vehicles. As noted earlier in this chapter, such interference may be due to intralink perturbations such as vehicles stopping for loading and unloading, pedestrian activity (other than at intersections), and many other similar activities which are an inherent feature of a city street network. By examining the effect of this factor on the parameters of the traffic models of interest, we can gain insight into the determinants of these parameters, and thus enhance their interpretability and usefulness, particularly in the context of comparisons between cities with different characteristics. In our simulations, this factor is modelled using the "short-term events" option of the simulation package, where the user may specify the mean frequency and mean duration of these events. These are then generated, in the simulation, stochastically and independently as blockages in the right lane in the center of the link. The average fraction of time that the right lane is blocked can be found by dividing the mean event duration by the inter-event time (the inverse of the event frequency).

In the experiments described herein, short-term events are identically specified for all 80 links in the test network at the four levels shown in Table 5.7. The first, denoted AL0, is the base case, with no events specified. The other three levels are denoted AL1, AL2 and AL3, and correspond to mean frequencies of 30, 72 and 30 events per hour, and mean durations of 25, 25 and 60 seconds, respectively. As noted earlier, only three runs

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were conducted at each level of this factor, with target concentrations of 20, 40 and 60 vehicles/lane-mile.

The estimates of the network level model parameters of interest are presented in Table 5.7 (for the nonlinear v(K) relation) and Table 5.8 (for the two-fluid parameters), for each of the activity levels under consideration. All parameters exhibit clear trends in response to the activity levels. However, we have to be cautious in interpreting these parameters, particularly those of the nonlinear v(K) relation, because we have only three observations per factor level. Generally, it appears that increasing activity levels and the accompanying impedence to moving vehicles results in greater sensitivity to the prevailing concentration level. This is manifested in the value of the parameter d in the v(K) model, which decreases with increasing interfering events, indicating a more rapid rate of deterioration of the average speed in the range of concentrations K<Km (which is where most of our simulated observations were). Similarly, the two-fluid parameter n increased with increasing activities, reflecting the greater sensitivity of running time.

On the other hand, the free-flow speed  $V_f$  increased, while the minimum running time  $T_m$  decreased, with increasing activity levels; this behavior appears to be counterintuitive, and is more of a statistical aberration than a reflection of a true phenomenon. Both values represent some condition under K=0, and are estimated by extrapolation from the points corresponding to concentration values in the range of 20 to 60 vehicles/lane-mile. Thus, for cases where the effect of concentration on average running speed was large, such as in the presence of high activity levels, lower intercepts (for K=0) were predicted than in the case where traffic interfering activities were not specified.

In all cases, it appears that parameters are more responsive to changes in mean event duration than in the mean frequency of these short term events, for a given fraction of time that the right lane is blocked. The behavior of the parameters d and n with respect to the activity level are shown in Figs. 5.17 and 5.18, respectively, where each parameter's variation is shown as a function of mean event frequency, mean event duration, and mean

# Table 5.6Two Fluid Model Parameter Estimates:Effect of Signal Coordination

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Control	n	т <sub>m</sub>	
No Short-Term Eve	ents Specified		
Single Alternate	8.148	0.878	
Random Offset	7.441	0.866	
Simultaneous	9.919	0.502	
		5. <del>16-1</del>	- the area in
With Short-Term E	vents Specified		
Single Alternate	7.643	1.023	
Random Offsets	6.746	1.078	
Simultaneous	8.954	0.681	

# Table 5.7 Two-Fluid Model Parameter Estimates: Effect of Activity Levels (Short Term Events)

Activity Level	Mean Frequency (Event/hour)	Mean Duration (Sec)	Frac. of Time Lane is Blocked	n	T <sub>m</sub> (min/mile)
0	0	0	0	1.831	2.011
1	30	25	0.208	2.259	1.822
2	72	25	0.500	2.583	1.804
3	30	60	0.500	2.700	1.764





fraction of time that the right lane is blocked. The greater influence exerted by the mean event duration is easily seen in these figures.

#### 5.5. SUMMARY AND CONCLUDING COMMENTS

As noted earlier, the factors specifically examined in this study were not intended to be comprehensive, but mainly to explore the sensitivity of the network-level models and their parameters to selected examples of each of the three categories of factors thought to influence the network's performance. In this section, we review the principal parameters' response to these factors, and discuss how these parameters might be correlated, as well as the relative impact of the various factors considered on the quality of service offered by the system.

In general, the network's physical features seem to have a greater effect on the network's performance than traffic control through conventional signal timing. Nevertheless, as indicated in section 5.3, meaningful improvements could be achieved in the concentration ranges under which most actual networks operate. Overall, the greatest positive impact onn the level of service, defined as higher average speed and lower fraction of vehicles stopped for a given concentration level, was achieved by increasing the block length. While it does not seem practical to redesign entire CBD's, the results indicate the possible improvements that could result from reducing the required stoppage at intersections.

The effect of more lanes (keeping concentration constant) on average speed and fraction of vehicles stopped is not as dramatic; however, a better perceived quality of flow is seemingly reflected in a lower value of the two-fluid parameter n, due to the greater freedom to maneuver available to motorists. Regarding the latter parameter's behavior, n does not appear to constitute a reliable objective to guide network improvements. For instance, the above-mentioned clearcut overall improvement due to longer blocks is accompanied by an increase in n, because the higher running speeds possible in the longer

O iı tı in 01 ev by te qu un ref cha per eve cha tern links are correspondingly more susceptible to rapid deterioration due to intralink friction generated at higher concentrations. The same type of phenomenon is manifested in the results of the traffic control experiments, where the clearly beneficial effects of coordinated operation at lower concentrations were accompanied by an increase in n. On the other hand, for a given link length and coordination scheme, a lower n seems to correspond to improved traffic conditions, as seen when an extra lane was added to an existing link, or when the level of traffic interfering activities was reduced. This suggests caution in making comparisons on the basis of n among networks with different link sizes or signal coordination strategies.

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It appears that the most direct and consistent mechanism for explaining the variation of the parameter n is the occurrence of short term traffic interfering activities. These directly interfere with the moving vehicles' running speed, and thus generate delays incurred in traversing the links themselves, as opposed to delays incurred while stopped at intersections (which do not affect the average running speed of the moving vehicles). While other factors naturally affect n, its most consistent determinant appears to be the short term events. From this standpoint, n might be a good measure of the quality of flow perceived by system users; this quality is not necessarily correlated with overall performance (e.g. in terms of average speed or fraction of vehicles stopped), but rather is a reflection of the quality of flow as vehicles are moving, since drivers can be expected to prefer travelling unimpeded at their desired speeds. To the extent that the intensity of these short term events reflect the character of life in a particular city, it can be expected that behavioral characteristics of the users as well as of the urban dwellers at large can greatly affect the performance of a traffic network. By the same token, measures to control these short term events, such as the provision of facilities for loading and unloading, better pedestrian channelization, and stricter enforcement of certain regulations (e.g. preventing illegal shortterm parking) can have a significant impact on the overall quality of service, in terms of lower average speed for a given concentration level as well as greater ease of movement reflected by a lower value of n.

The interpretablity of any of the speed-concentration relation parameters, taken individually, appears limited, particularly if based on few observations, as in the tests for the effect of traffic-interfering activities. The greatest effect on the parameter d was that of the traffic control and activity level factors. However, it did not exhibit a generally consistent behavior in response to network changes.

In terms of the joint variation of these various parameters, no consistent patterns have emerged from this limited set of experiments. The clearest trend observed is the negative correlation between the values of the two-fluid parameters n and  $T_m$ , illustrated in Fig.5.18, which depicts all the points generated by the simulations discussed in this chapter. Fig. 5.18 seems to indicate that measures that reduce  $T_m$ , i.e. improve the maximum running speed in the network, tend to increase n, i.e. the sensitivity of the average running speed to increasing vehicular concentration. None of the other parameters appear to be as consistently related; rather, opposite trends are present between any two parameters over the spectrum of observations. Further understanding of how these parameters are related, and of the interaction among various network features in determining the response of these parameters, can only be accomplished through a more extensive systematic investigation.

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## CHAPTER 6

## CONCLUSION

Several useful and promising directions for exploring, characterizing and understanding urban development patterns, as they affect and interact with transport in cities, have resulted from this study. The work was pursued along three levels: 1) the long term (since the turn of the century) evolution of several infrastructural attributes of cities, tracked primarily for Austin and San Antonio, and, to a more limited extent, for eleven other cities (Atlanta, Boston, Chicago, Cincinatti, Denver, Los Angeles, Miami, New York, Phoenix, Seattle and St. Louis), providing a means for comparing these cities; 2) the evolution of urban structure, in terms of the spatial density patterns of population and other variables, examined for four case areas; and 3) the characterization of traffic flow quality in urban networks, through the development of macroscopic network-level relations, and the investigation of their dependence on the physical and operational features of the network and the associated land use.

The spatial patterns of population density, household automobile ownership and other socio-demographic variables, as a function of distance from the central city core, were found to provide a useful characterization of urban structure, and of its evolution when taken at different time intervals. The four case cities (Austin, Atlanta, Dallas, Phoenix) considered in conjunction with this analysis illustrated several important continuing trends observed over the past three decades. In particular, the density functions captured the spatial dispersion away from the traditional central urban cores into the suburbs and exurbs, as well as the simultaneous densification of existing suburbs to levels almost comparable to the central cores. Parallelling this pattern has been a continuing growth of average household automobile ownership, in all parts of the urban area, with a distinct spatial and temporal pattern that seems to be robust across the case areas

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considered, as well as within radial corridors in the one case that was so analysed (Austin). These results suggest that average trip distances are likely to further increase, and that congestion levels in the densifying "suburban" communities will reach levels typically associated with CBD traffic systems. On the other hand, denser suburban communities and the emergence of stronger suburban foci might offer opportunities for the provision of mass transit services with more acceptable service levels than has traditionally been possible in low-density suburbs.

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However, suburban networks generally exhibit somewhat different characteristics from CBD systems, in terms of physical features, traffic control and adjoining land use and its generation of traffic-interfering activities. The implications of these differences on the performance of the traffic system, in terms of congestion and the associated quality of traffic service, were addressed by the third component of this work. Two principal objectives guided this part of the study. The first was to develop a system of relations that could comprehensively describe the joint behavior of traffic variables such as the average speed, flow and concentration, as well as the average fraction of vehicles stopped in the network, and the two-fluid stopped and running time variables. The second was to analyze the sensitivity of these relations and their parameters to the network's characteristics, particularly its topological features, prevailing control strategies and degree of interference from the adjoining land use. The latter objective is viewed as a preliminary step towards the more ambitious goal of relating the quality of traffic service and associated mobility level, to both network features and urban structure. Methodologically, both objectives were supported by microscopic simulation experiments, which provided useful macroscopic insights into network traffic behavior.

The principal conclusion from that investigation of traffic network performance is that it is possible to characterize traffic flow in urban street networks using relatively simple macroscopic models relating the principal networkwide traffic variables. Furthermore, it is remarkable that some of these relations closely parallel those that have been established at

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the individual facility level, despite the complex interactions that take place in a network. The analysis presented in Chapter 5 suggested that these relations and their parameters appear to follow systematic trends in response to the network features. The factors specifically examined in this study were not intended to be comprehensive, but illustrative of the phenomena affecting traffic network performance, and of the direction that future work can take in seeking a further understanding of these phenomena within the framework proposed in this study. However, the analysis yielded several useful indications about the relative magnitude of benefits from different types of improvements.

In general, the network's physical features seemed to have a greater effect on the network's performance than traffic control through conventional signal timing. Nevertheless, meaningful improvements could be achieved in the concentration ranges under which most actual networks operate. Overall, the greatest positive impact on the level of service, defined as higher average speed and lower fraction of vehicles stopped for a given concentration level, was achieved by increasing the block length. While it does not seem practical to redesign entire CBD's, the results indicate the possible improvements that could result from reducing the required stoppage at intersections. The effect of more lanes (keeping concentration constant) on average speed and fraction of vehicles stopped was not as dramatic; however, a better perceived quality of flow was reflected in a lower value of the two-fluid parameter n, due to the greater freedom to maneuver available to motorists.

Interesting insights were obtained regarding the effect of traffic interfering activities (short term events) typically present in an urban setting. Because the intensity of these short term events reflects the character of life in a particular city, it can be expected that behavioral characteristics of the users as well as of the urban dwellers at large can greatly affect the performance of a traffic network. By the same token, measures to control these short term events, such as the provision of facilities for loading and unloading, better pedestrian channelization, and stricter enforcement of certain regulations (e.g. preventing illegal short-term parking) could have a significant impact on the overall quality of service,

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in terms of lower average speed for a given concentration level as well as greater ease of movement reflected by a lower value of the two-fluid parameter n. A better understanding of these mechanisms would be useful in trying to understand and deal with the scenarios of deteriorating traffic conditions in densifying suburban communities. The private automobile has been an essential element in the development of these suburban development patterns, which initially seemed to offer congestion-free circulation. Rapid degradation of traffic conditions in these communities could have important consequences on the outcomes of the personal location, mobility and travel decisions of area residents, particularly with regard to automobile ownership and utilization.

## 6.1. FUTURE RESEARCH DIRECTIONS

Several opportunities for the continuation and expansion of the present research appear promising in terms of substantive and methodological contributions to the characterization of urban patterns, their evolution and the interaction with and effect on personal mobility and transportation. These opportunities exist in each of the three levels that formed the focus of the effort described herein, as well as in their integration into an overall operational framework that would provide the linkage between the evolution of the urban-wide attributes (considered in chapter 2), the spatial distribution of residents, firms and other activities, the resulting flow patterns and ultimately their effect on the performance of the transport network, given its features.

It is clear that much of the work in this report is of an exploratory nature. Thus the analysis of the attributes tracked for a small set of cities in chapter 2 can be enhanced through the consideration of additional descriptors and increasing the sample size, in order to gain greater confidence in the ability of some of these descriptors or combinations thereof to provide a robust characterization of urban evolution, and to subsequently support related predictions of future development.

Several directions for meaningful additional work are suggested by the results, presented in chapter 3, of the analysis of urban structure and its evolution, using the spatial density patterns of residence-based variables. First, it would be extremely valuable to consider the corresponding spatial patterns of the location of firms and businesses engaged in various professional, service or manufacturing activities. This can be accomplished using data sources such as industrial and business directories that give information at the firm level. Second, a larger set of case areas should be considered in order to further assess the robustness of some of the patterns seen here, as well as to possibly classify areas in terms of their respective spatial and temporal patterns. In particular, it would be interesting to examine areas such as San Francisco and Boston that have relatively more elaborate spatial patterns that have developed over longer time frames than many other U.S. cities. Third, it would be interesting to capture the characteristics of the transportation network serving the areas under consideration by examining the densities as a function of network distance or travel time instead of Euclidian distances from the CBD. Fourth, it is desirable to integrate the above spatial patterns into an approach to estimate flow patterns and aggregate travel descriptors (such as average trip lengths) resulting from the interaction between the spatial patterns of residence-based variables, and those of the location of firms and businesses. This would provide an important link to the study of the transport implications of evolving urban structures. Such an approach could additionaly incorporate the characteristics of the transport infrastructure.

Regarding the traffic network performance component of the present research, it has now reached a level of maturity which holds considerable promise for possibly very powerful results. A systematic investigation of an expanded list of factors would yield more definitive relations between the parameters of the traffic models and the network's features. A key factor to consider would be the flow (demand) pattern, in order to tie in with the spatial patterns of activities and residences discussed above. Methodologically, simulation experiments using a somewhat more realistic-looking network setting would be

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useful; interesting opportunities along these lines involve using a supercomputer to simulate larger networks, with more vehicles, over a longer period of time. In addition, combining the simulation-based work with carefully conceived observational field work could yield significant results.

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## REFERENCES

- Adams, John S. (1986), "The Geographical Evolution of U.S. Urban Areas at the National and Local Scales", National Academy of Engineering Workshop on Future Infrastructures, Woods Hole, Massachusetts.
- Anderson, John E. (1985), "The Changing Structure of a City: Temporal Changes in Cubic Spline Urban Density Patterns", *Journal of Regional Science* 25, pp. 413-427.
- Anderson, John E. (1982), "Cubic Spline Urban Density Functions," Journal of Urban Economics, 12, 155-167.
- Ardekani, Siamak (1984), "The Two-Fluid Characterization of Urban Traffic: Theory, Observation and Experiment", Ph.D. Dissertation, Department of Civil Engineering, The University of Texas at Austin.
- Ardekani, Siamak, Dona, Edgar, Govind, Shekhar and Herman, Robert (1986), "The Dynamic Characterization of Cities", National Academy of Engineering Workshop on Future Infrastructures, Woods Hole, Massachusetts.
- Ardekani, Siamak and Herman, R. (1982), "Quality of Traffic Service," Research Report 304-1, Center for Transportation Research, The University of Texas at Austin.
- Ardekani, S., Torres-Verdin, V., and Herman, R. (1985), "The Two-Fluid Model and the Quality of Traffic in Mexico City," published in Spanish as "El Modelo Bifluido y La Calidad del Transito en La Ciudad de Mexico", *Revisto Ingenieria Civil*, Calegio de Ingenierus Civiles de Mexico Jan/Feb.

Brotchie, J., Newton, P., Hall, P. and Nijkamp, P. (1985), "Introduction", in *The Future* of Urban Form: The Impact of New Technology, Nichols Publishing Co.

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City Directory of Austin (1959 to 1985), pub. R.L.Polk and Co., Dallas, Texas.

City Directory of San Antonio (1900 to 1985), pub. R.L.Polk and Co., Dallas, Texas.

- Clark, Colin (1951), "Urban Population Densities", Journal of the Royal Statistical Society, A, 114, 490-496.
- County and City Data Book (1949, 1956, 1962, 1967, 1972, 1977 and 1983), U.S. Bureau of Census, Washington D.C.
- Drake, J., Scofer, J. and May, A. D. (1967), "A Statistical Analysis of Speed-Density Hypotheses", *Proceedings of the Third International Symposium on Theory* of Traffic Flow, American Elsevier.
- Frankena, Mark W. (1978), "A Bias in Estimating Urban Population Density Functions," Journal of Urban Economics 5, 35-45.

General Directory of the City of Austin (1900 to 1958), pub. Morrison and Fourmy, Gavleston, Texas.

- Gerlough, D. L. and Huber, M. J. (1975), "Traffic Flow Theory: A Monograph", TRB Special Report 165, Washington, D.C. .
- Govind, Shekhar, Robert Herman and C. Michael Walton (1986) "Characterizing the Evolution of Cities", working paper, Center for Transportation Research, University of Texas at Austin, August.

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- Herman, Robert and Montroll, Elliott W., (1972) "A Manner of Characterizing the Development of Countries", *Proceedings of the National Academy of Sciences*, Vol. 69, No. 10, October.
- Herman R. and Prigogine, I. (1979), "A Two-Fluid Approach to Town Traffic," Science 204, pp. 148-151.
- Herman, R. and Ardekani, S. (1984), "Characterizing Traffic Conditions in Urban Areas," *Transportation Science* 18, pp. 101-139.
- Lakshmanar, T.R. and Chatterjee, L. (1985), "Technical Change and Metropolitan Adjustments: Some Policy and Analytical Implications", *Regional Science* and Urban Economics, 15.
- Mahmassani, H.S., Williams, J.C., and Herman, R. (1984), "Investigation of Network-Level Traffic Flow Relationships: Some Simulation Results," *Transportation Research Record* 971, pp. 121-130.
- McDonald, John and Bowman, H. Woods (1976), "Some Tests of Alternative Urban Population Density Functions," *Journal of Urban Economics* 3, 242-252.

Muth, Richard (1969), Cities and Housing, Chicago, University of Chicago Press.

- Nijkamp, P. and Schubert, U. (1985), "Urban Dynamics", in Brotchie, et al. (eds.) The Future of Urban Form, Nichols Publishing Co.
- Peat, Marwick, Mitchell and Company (1973), Network Flow Simulation for Urban Traffic Control System - Phase II, Volumes 1-5; prepared for the Federal Highway Administration, U.S. Department of Transportation, Washington, D.C..
- Poirier, Dale J. (1973), "Piecewise Regression Using Cubic Splines", Journal of the American Statistical Association 68, 515-524.

Pressman, N. (1985), "Forces for Spatial Change", in Brotchie, et al (eds.), *The Future of Urban Form*, Nichols Publishing Co.

- "Traffic Network Analysis with NETSIM A User Guide" (1980), Implementation Package FHWA-IP-80-3, Federal Highway Administration, U.S. Department of Transportation, Washington, D.C..
- Williams, J. C., Mahmassani, H.S. and Herman, R.(1985), "Analysis of Traffic Network Flow Relations and Two-Fluid Model Parameter Sensitivity", *Transportation Research Record* 1005, pp. 95-106.

Yeates, Maurice (1976), The North American City, Harper & Row, New York .