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DRYING SHRINKAGE AND TEMPERATURE DROP STRESSES  
IN JOINTED REINFORCED CONCRETE PAVEMENT

by

Felipe Rivero-Vallejo  
B. Frank McCullough

Research Report Number 177-1

Development and Implementation of the Design, Construction  
and Rehabilitation of Rigid Pavements

Research Project 3-8-75-177

conducted for

Texas  
State Department of Highways and Public Transportation

in cooperation with the  
U. S. Department of Transportation  
Federal Highway Administration

by the

CENTER FOR HIGHWAY RESEARCH  
THE UNIVERSITY OF TEXAS AT AUSTIN

May 1976

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## PREFACE

This report summarizes the results of a study to determine the effects of a drop in temperature and of drying shrinkage on the occurrence of cracks in a jointed concrete pavement. The purpose of this work was to develop a computerized method to analyze, or design, either a reinforced or a non-reinforced pavement slab.

The project is being conducted at the Center for Highway Research, The University of Texas at Austin, as part of the Cooperative Highway Research Program sponsored by the State Department of Highways and Public Transportation and the Federal Highway Administration.

This report would not have been possible without the help and assistance of many people. I also acknowledge Dr. W. R. Hudson, member of my graduate supervising committee. Special appreciation is extended to Mr. Thomas Hainze for his friendly help concerning the correction and analysis of the computer program. Thanks are also due to Mrs. Marie Fisher who has collaborated at different stages of this work.

Felipe Rivero-Vallejo  
B. Frank McCullough

Austin, Texas  
August 1975

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## LIST OF REPORTS

Report No. 177-1, "Drying Shrinkage and Temperature Drop Stresses in Jointed Reinforced Concrete Pavement," by Felipe R. Vallejo and B. Frank McCullough, describes the development of a computerized system capable of analysis and design of a concrete pavement slab based on drying shrinkage and temperature drop, August 1975.



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## ABSTRACT

This report deals with the development of a computerized system for analyzing and designing concrete pavement slabs subjected to drying, shrinkage, and drop in temperature stresses with time.

The system is capable of analyzing a given jointed reinforced concrete pavement slab design for crack occurrence. It is also capable of designing either a reinforced or a non-reinforced slab.

It has been found that the main factor acting in crack generation is the friction between the slab and the underlying pavement course, with higher stresses in the slab occurring with high friction values.

This work is a useful tool in the study of cracking in concrete pavement slabs because it is relatively simple to superimpose the stresses due to drying, shrinkage, and drop in temperature on the stresses generated by factors such as wheel load, warping, etc. in order to get a more realistic "state of stress" in the slab.

KEY WORDS: jointed reinforced concrete pavement slabs, computer program JRCP-1, drying shrinkage and drop in temperature cracking, crack width, crack width, crack occurrence, subbase friction.

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## SUMMARY

A computerized system to analyze a concrete pavement slab for drying shrinkage and drop in temperature stress with time has been developed.

The main purpose of developing the system was to search for possible cracking of the slab. The system was capable of

- (a) analyzing a given slab design (length, width, thickness, steel percentage, etc.), checking the width of the cracks and the steel stresses against maximum values;
- (b) designing the percent reinforcement for a concrete pavement slab, based on a maximum allowable crack width and stress in the steel; and
- (c) designing a non-reinforced concrete slab.

This option will result in a slab length that will not give a cracked slab.

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## IMPLEMENTATION STATEMENT

This study resulted in a mathematical model that can be used to design more reliably the reinforcement steel for jointed reinforced concrete pavement. A computer program has been prepared that can be used now by the Highway Design Division of the State Department of Highways and Public Transportation. In order to obtain maximum utilization of this computer program, the following implementation steps are recommended.

- (1) A range in temperature conditions should be selected on the basis of Texas geographic areas to be used for studying variations in performance with respect to temperature and shrinkage cracking. These geographic areas should be the same as those recommended for implementation of computer program CRCP-1.
- (2) The wheel load stresses should be superimposed on those predicted by temperature changes and drying shrinkage. There is evidence from studies of concrete pavement that wheel load stresses may influence the formation of transverse cracks, especially during the early life of the pavement.
- (3) A user's manual should be prepared for the State Department of Highways and Public Transportation, to permit field usage of the program. The operating manual in Appendix 1 of this report could be used as a guideline.
- (4) The temperature data developed in connection with recommendation (2) should be used to develop a range of solutions, crack widths, crack spacings, and steel stresses for different material properties.
- (5) The information from (4) should be used to develop a design manual for CRCP that would reflect more variables than are taken into account at the present time; in this way, the performance level of CRCP would be improved.

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## CHAPTER 1. INTRODUCTION

In 1921 and 1922, the Pittsburg, California, Road Test was designed and performed to determine the efficiency of both reinforced and non-reinforced pavement of varying design. The results indicated that longitudinal joints were effective in preventing longitudinal cracks.

Although concrete pavements were first used in about 1900, uncontrolled cracking caused problems for many years. As a result, joints were introduced to control cracking. From 1930 through 1936, the Bureau of Public Roads conducted the Arlington Test Road at Arlington, Virginia. The results supplied much of the basis for modern pavement design criteria (Ref 1).

In the late 1930's, many highway engineers became concerned about the use of contraction joints where expansion joints were also used. The use of dowels in closely spaced contraction joints and other problems in the jointing of pavements were also studied in view of service records. To study these questions, the Bureau of Public Roads authorized the construction of long-range experimental road tests in California, Kentucky, Michigan, Minnesota, Missouri and Oregon. After World War II, research programs in several phases of pavement technology were intensified to meet the ever-increasing demand of postwar traffic; two of the more significant programs are the Maryland Road Test (HRB SR-21) and the AASHO Road Test (SR 61E).

At the present time, significant concrete pavement research is directed toward the study of transverse cracking, which is a major contributor to pavement deterioration. Cracking in jointed reinforced concrete pavement is a prime factor leading to a reduction in pavement performance, depending on crack width. Water percolation, spalling, loss in load-carrying capacity, and pumping are some of the distress manifestations which vary with cracking in a slab.

Extensive research has been done to determine causes of cracking. It has been found that cracks occur when the tensile strength of the concrete is exceeded by the stresses generated by internal and external forces. The external forces are basically due to wheel loads, and the internal forces are due

to temperature changes (curling, shrinkage) and loss in moisture. Warping and curling have been studied at Purdue University and in many other places; the load effect has been studied at The University of Texas, but shrinkage in jointed pavements still has not been studied.

#### THE NEED

Concrete pavement is generally classified as either plain, continuously reinforced (CRCP), or jointed reinforced concrete pavement (JRCP). Reinforced concrete was recommended in 1914 to counteract cracking caused by thermally induced expansion and contraction. In 1916 it was recommended that all concrete roads be reinforced and specifications were written to cover several problems. In 1931, the common pavement slab was of the thickened edge design, and contained 30 to 69 pounds of steel, wire mesh, or bar mat per 100 square feet. Reinforcement design for rigid pavement is based on the concept that since it is often not economically possible to prevent the formation of cracks, it is necessary to control the opening of cracks in such a manner that the original load-carrying capacity of the slab is preserved. If the crack is permitted to open, contact between the faces of the crack is lost, with a corresponding loss in shearing resistance, and continued application of load results in progressive breakage. Since the main function of steel reinforcement in rigid pavement is to hold the interlock faces of the concrete at a crack in tight contact to provide for good load transfer, and to avoid water entering and washing out the subbase material, it is only necessary to furnish sufficient steel area to resist the forces tending to pull the crack faces apart. These forces develop when the slab tends to shorten as a result of a drop in temperature, concrete shrinkage, or moisture reduction. As the slab contracts, the movements are resisted by the friction between the slab and the underlying subgrade or subbase. The resistance to movement produces a direct tensile stress and may cause the concrete to crack. As soon as the concrete cracks, the tensile stress is transferred to the steel reinforcement.

In order to obtain the benefit of a better pavement design, reliable predictions of shrinkage and temperature stresses are required to complete the study of the pavement slab stresses. The reinforced slabs are designed to control random cracks; in other words, to minimize crack openings so that load transfer is provided by the aggregate interlock, thereby avoiding the distress manifestations that could lead to total deterioration. Stresses in the

manifestations that could lead to total deterioration. Stresses in the pavement are caused by different factors such as:

$$\begin{aligned} \sigma_{\text{concrete}} = & \sigma_{\text{load}} + \sigma_{\text{curling}} + \sigma_{\text{moisture shrinkage}} \\ & + \sigma_{\text{drop in temperature}} \end{aligned}$$

The crack formation mechanism is represented conceptually in Fig 1.1. Cracking of the concrete slabs occurs when the tensile stresses generated by external and internal forces exceed the concrete tensile strength. Obviously cracking will occur only with tension or contraction, with expansion not being a problem. Therefore, the concrete slab will experience cracking when at some time the tensile stresses are greater than the tensile strength of the concrete. If at some time the combination of tensile stresses due to load, curling, shrinkage, and drop in temperature exceeds the tensile strength cracking will occur. This can be represented in the following conceptual equation:

$$(\sigma_{\text{load}} + \sigma_{\text{curling}} + \sigma_{\text{shrinkage}} + \sigma_{\text{drop in temperature}}) > f_{\text{concrete}}$$

Temperature drop is defined as the daily drop in temperature from the curing temperature. As previously mentioned, stresses due to load and curling have been studied; remaining for study are the shrinkage and drop in temperature stresses. The need for studying shrinkage and drop in temperature became apparent when slabs at the Dallas-Fort Worth Regional Airport experienced a range of transverse cracking. From the study of such cracks (Ref 2), it can be seen that the combination of slab movement with subbase type is the cause of the cracks. Slab length or joint spacing was varied from 37.5 to 75 feet, and it was found that joint spacing of 37.5 feet gave a reduced cracking. Initially the construction engineers hypothesized that by changing the amount of steel, the problem would be solved, but in order for the steel to be effective, cracks must be present. Several subbase conditions were tried to study their effect on cracking. The studies confirmed the hypothesis that the stresses in the concrete would increase with increased sub-grade friction and joint spacing. For the low sub-grade friction, it can happen that no crack occurs, but, the movement of the slab still exists, leading to a joint width

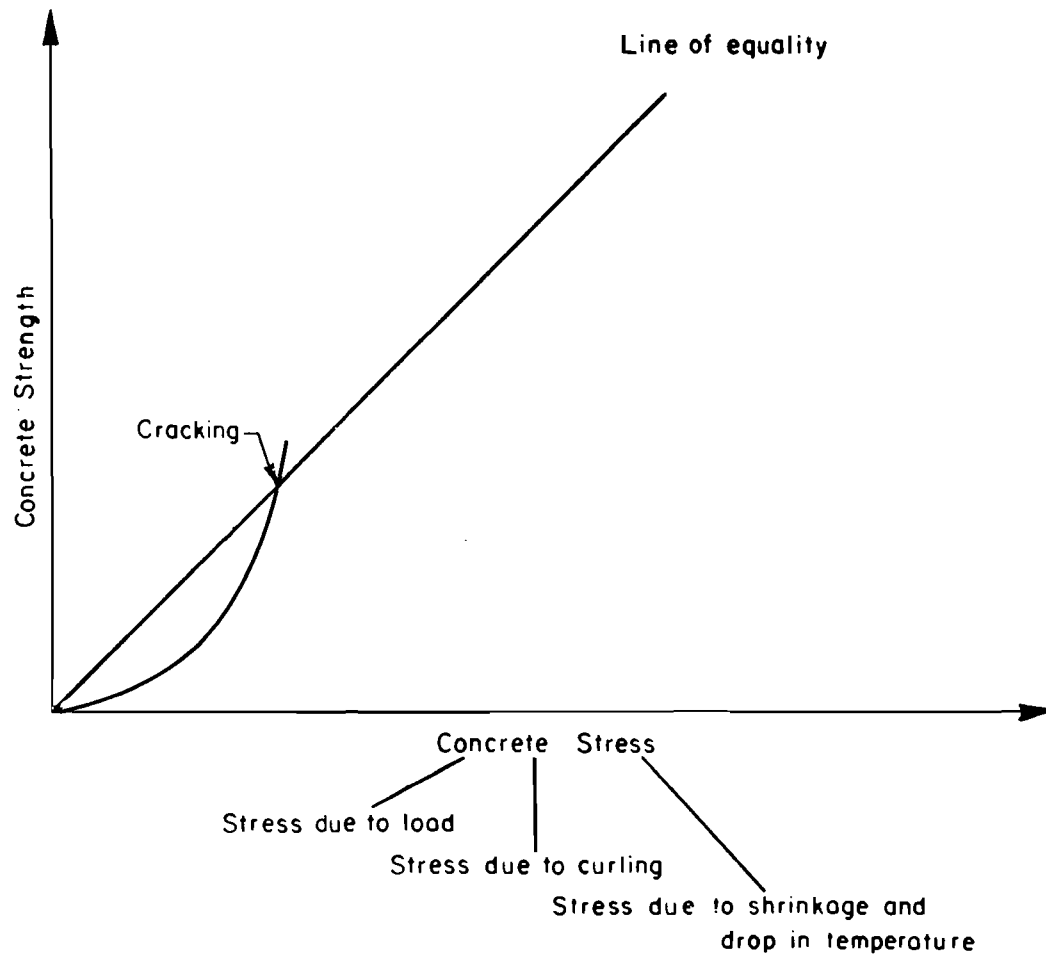


Fig 1.1. Graphical representation of a concrete pavement slab distress mechanism.

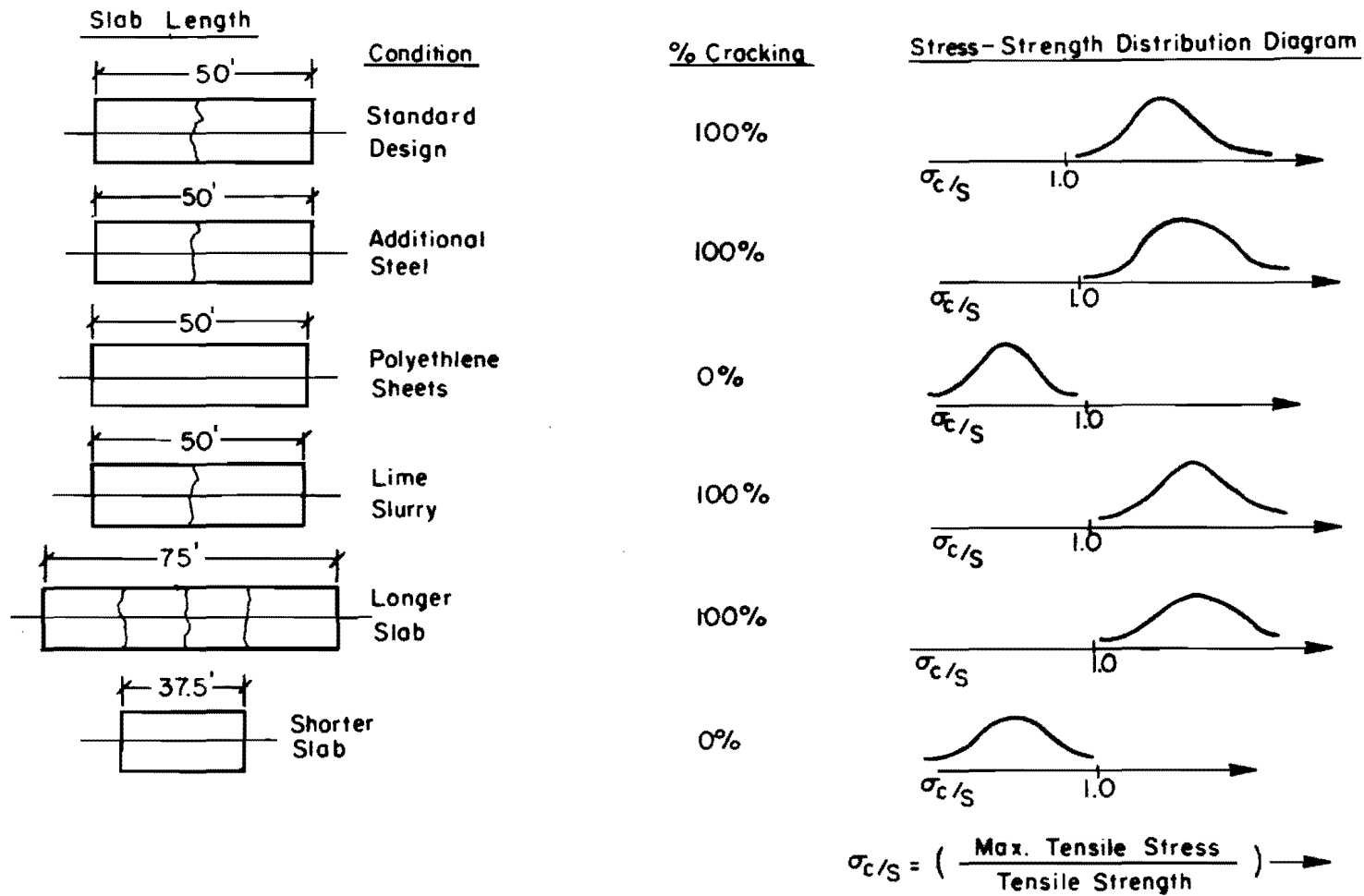


Fig 1.2. Summary of the findings of the Dallas-Ft. Worth study (Ref 1).

that can be harmful. In Fig 1.2, a brief graphic summary of the findings of Austin Research Engineers, is presented. In this figure, percent cracking is defined as the percent of slabs expressing one or more transverse cracks at or near mid-span. The distribution diagram shown on the right of the figure is a hypothetical condition based on percent cracking; thus, if one hundred percent cracking is reported, then the concrete tensile stress due to volume change must be greater than the concrete tensile strength for every slab, that is, the ratio must be greater than 1.0.

The restriction of slab movement will also be increased if the dowels at joints are not greased or have poor alignment as shown in Fig 1.3. This means that dowels hold the slab when it tends to contract, thus creating additional stresses that are very difficult to predict because of the infinite number of positions in which the dowels can be placed.

#### OBJECTIVES

This report describes studies of the stresses induced in the pavement due to shrinkage and drop in temperature in an effort to make a more complete and realistic study of the concrete stresses, and also to have a better feeling of how the stresses are going to be affected by the combination and interaction of shrinkage, drop in temperature, slab length, subbase friction, and concrete characteristics.

The concrete slab will experience contraction movements due to drying shrinkage and drop in temperature; those movements will be restrained by the reinforcing steel, and the subbase friction; the restraint provided by dowels and tie bars is not taken into account.

#### SCOPE OF THE STUDY

This study is focused on the effects of drying shrinkage and drop in temperature in the crack formation in a concrete pavement slab. The study is intended to provide a useful tool in the design and analysis of jointed concrete pavement. As previously discussed, the concrete contraction movement will be restrained by the reinforcing steel and the subbase friction, the last parameter being the most important one in the development of cracks. The goal of this study was to develop a computerized model capable of analyzing either a reinforced or a non-reinforced slab for temperature drop and drying shrinkage stresses.

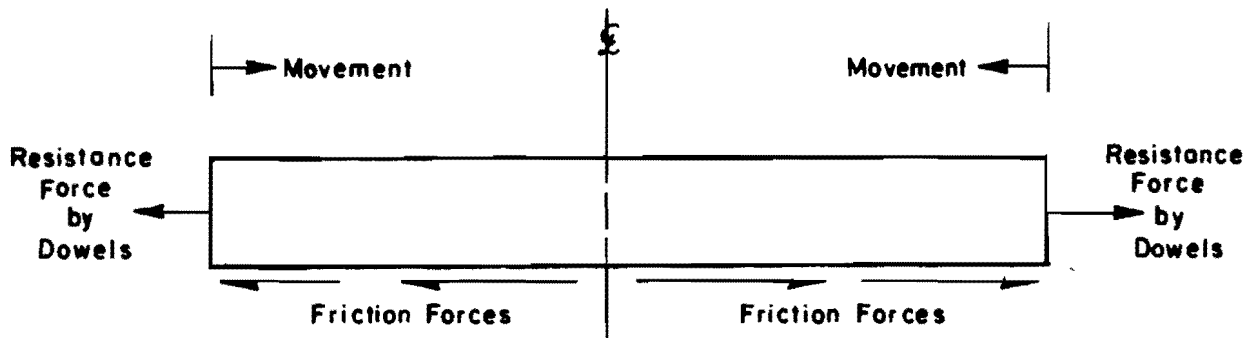
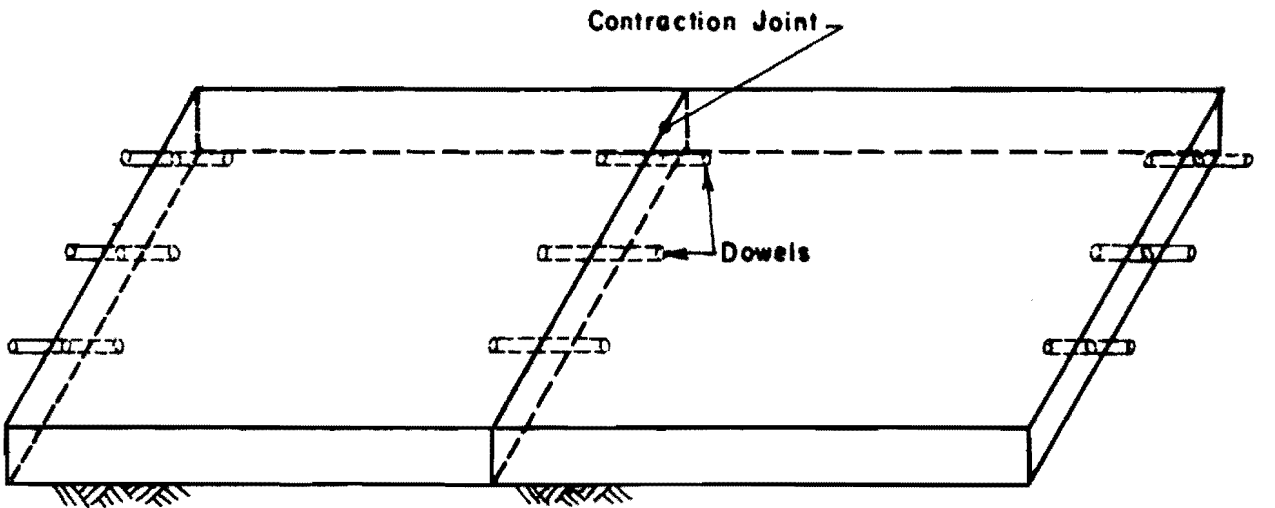


Fig 1.3. Forces generated by poorly placed dowels in a contracting slab.



This first chapter of the report is intended to introduce the reader to the subject. Chapter two gives a general view of the cracking mechanism in concrete. Chapter three deals with the theory and background on which the study is based, explaining in a comprehensive manner the shrinkage and drop in temperature phenomena as well as concrete properties related to the study. Chapter four describes the mathematical approach used in the solution of our problem, including the geometric models as well as the solutions. Chapter five gives a description of the computer program and its usefulness.

## CHAPTER 2. CONCEPT OF CRACKING

A brief conceptual explanation of why jointed reinforced concrete pavements crack is helpful to a better understanding of the problem. Cracking results when the concrete-tensile stress produced by contraction volume changes resulting from temperature drop, concrete shrinkage or both, exceeds the tensile-strength of the concrete which increases with time. The drying shrinkage is the reduction in length obtained when a saturated sample is dried under certain conditions; drying shrinkage depends on the cement and, in particular, certain conditions, including fineness, the richness of the mix, the water/cement ratio and the kind of curing, especially at early ages. The rate at which movement or shrinkage takes place depends on the permeability of the concrete. Drying shrinkage generally decreases as the strength of the aggregate increases (Ref 3).

It is fairly well established that shrinkage takes place over considerable time and the rate of increase of shrinkage decreases with time. The following figures have been given by Patten (Ref 3) to indicate the ranges of shrinkages at different times after placement:

after 2 weeks, 14-34 percent of the 20-year shrinkage;  
after 3 months, 40-80 percent of the 20-year shrinkage; and  
after 2 years, 66-85 percent of the 20-year shrinkage.

In Fig 2.1 approximately average curves for the shrinkage strains for concrete made from ordinary portland cement, rapid hardening portland cement, and high alumina cement are given. It should be pointed out that the steepest portion of the curves occurs between time of placing and two months, emphasizing the importance of drying shrinkage in crack formation at an early concrete age (Ref 3). The volume changes alone do not produce stresses, but they occur as a result of the restriction provided by the friction between concrete and subbase. This may be seen in Fig 2.2 where two friction subbases, one low and the other high, are plotted (Ref 2). Stresses can be set up in rigid pavements as a result of uniform temperature changes which cause the slab to contract or expand. If a slab cools uniformly, a crack will generally occur at about the center of

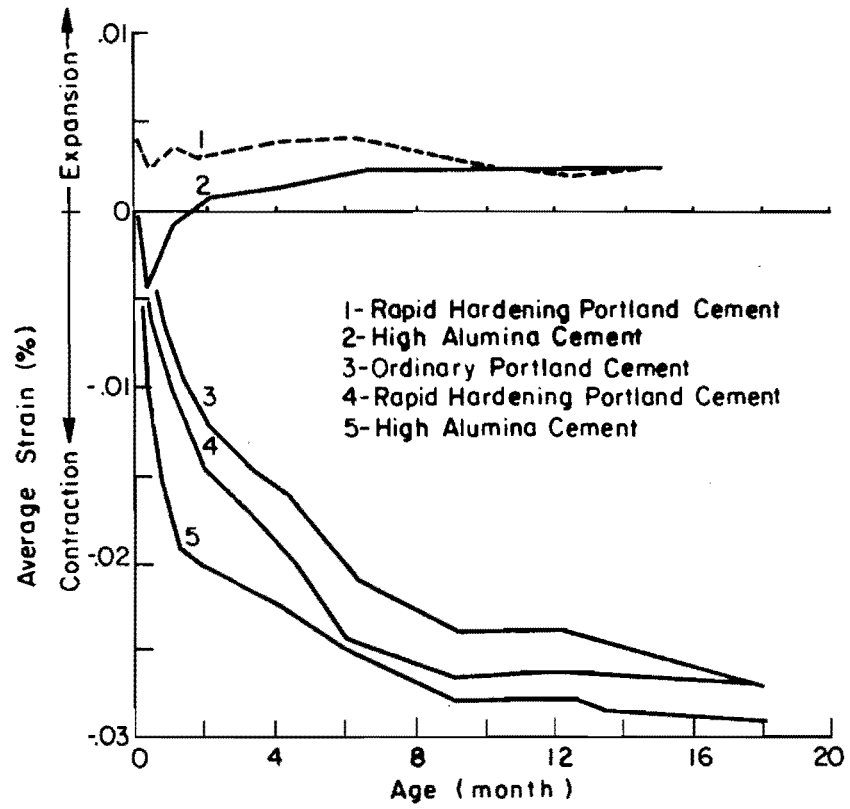


Fig 2.1. Shrinkage strains for three types of cement, after Glanville (Ref 3).

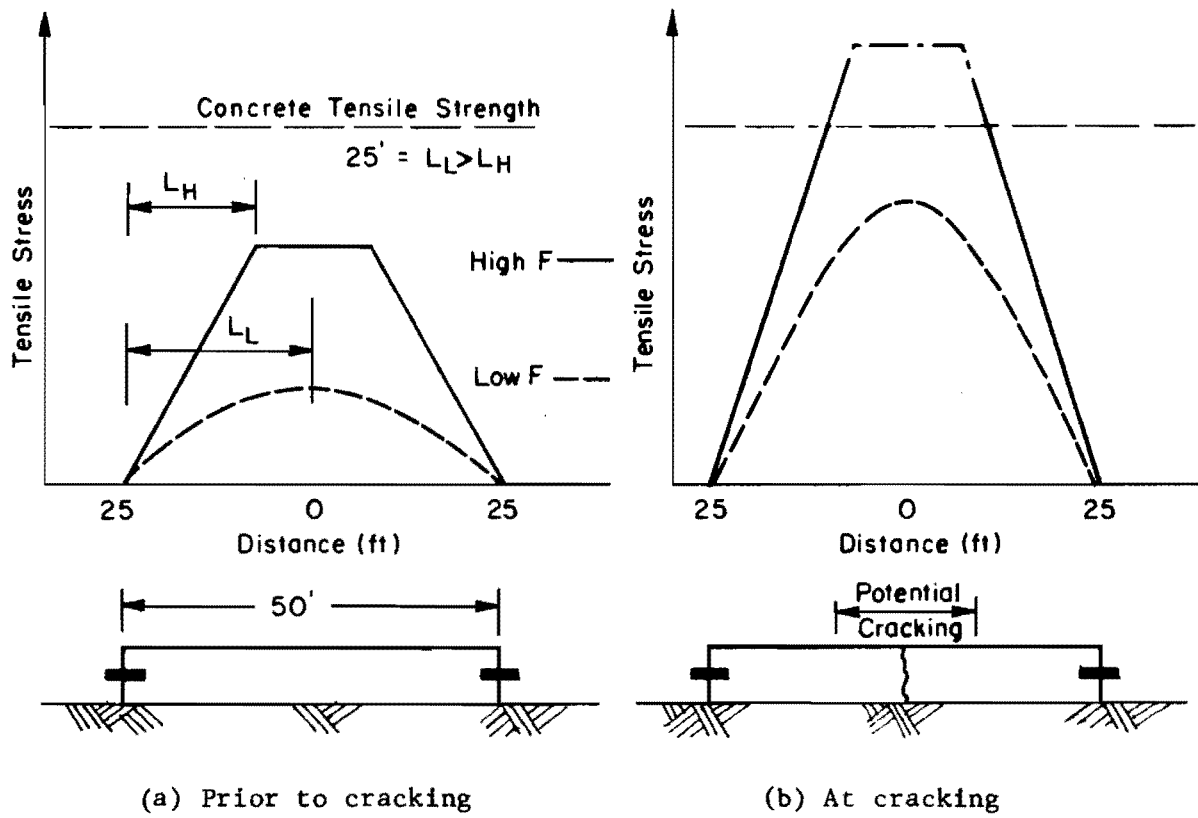


Fig 2.2. Longitudinal stress distribution in a concrete slab prior to and at cracking (Ref 2).

the slab. Shrinkage of the concrete also causes the same phenomenon to occur. In order to generate frictional resistance during contraction, movement between slab and subgrade must occur, which means the slab is going to slide when contracting. Research Studies indicate minimum displacement of 0.06-inches is needed for friction to be fully developed (Ref 4). The slab movement will be in a decreasing pattern going from a maximum at its free end to zero (no movement) at a point in the interior, where the maximum concrete tensile stress will develop. Kelly (Ref 4) has suggested, based on results of "tests", that fully mobilized frictional resistance is realized for the distance  $\left(\frac{L}{2} - x\right)$  as shown in Fig 2.3, but from there to the geometric center of the slab, the shape of the stress distribution is parabolic. From this, it is obvious stresses due to frictional resistance in slabs will vary with slab length, but it is doubtful whether or not, on short slabs, sufficient friction will be developed to cause tensile stresses in the concrete that can lead to a distress manifestation (cracking).

#### THE PROBLEM

As discussed previously, the cracking occurrence in concrete slabs for pavements is a direct function of time, that is, the concrete slab will gain strength with time and also will contract due to temperature drop and drying shrinkage; both of which are also functions of time. The drop in temperature will be the difference between setting temperature and the lowest daily recorded temperature. This study is based on the early age of the concrete, from placement to 28 days, when concrete is approaching its full strength.

This study then is based on the need to find the stresses that the concrete is going to have with time and to determine if those stresses will produce a crack at or near maximum values. After knowing the concrete tensile stress distribution for a specific time and knowing the concrete tensile strength for that same time, it is fairly easy to predict a crack (Fig 2.4(a)); then, if a crack happens to occur, it is necessary to find the new concrete tensile stress distribution, which is going to be different from the previous one, because at the crack the concrete will have no stress, Fig 2.4(b); then by comparing this new stress pattern against concrete strength, more possible cracks can be detected, Fig 2.4(c).

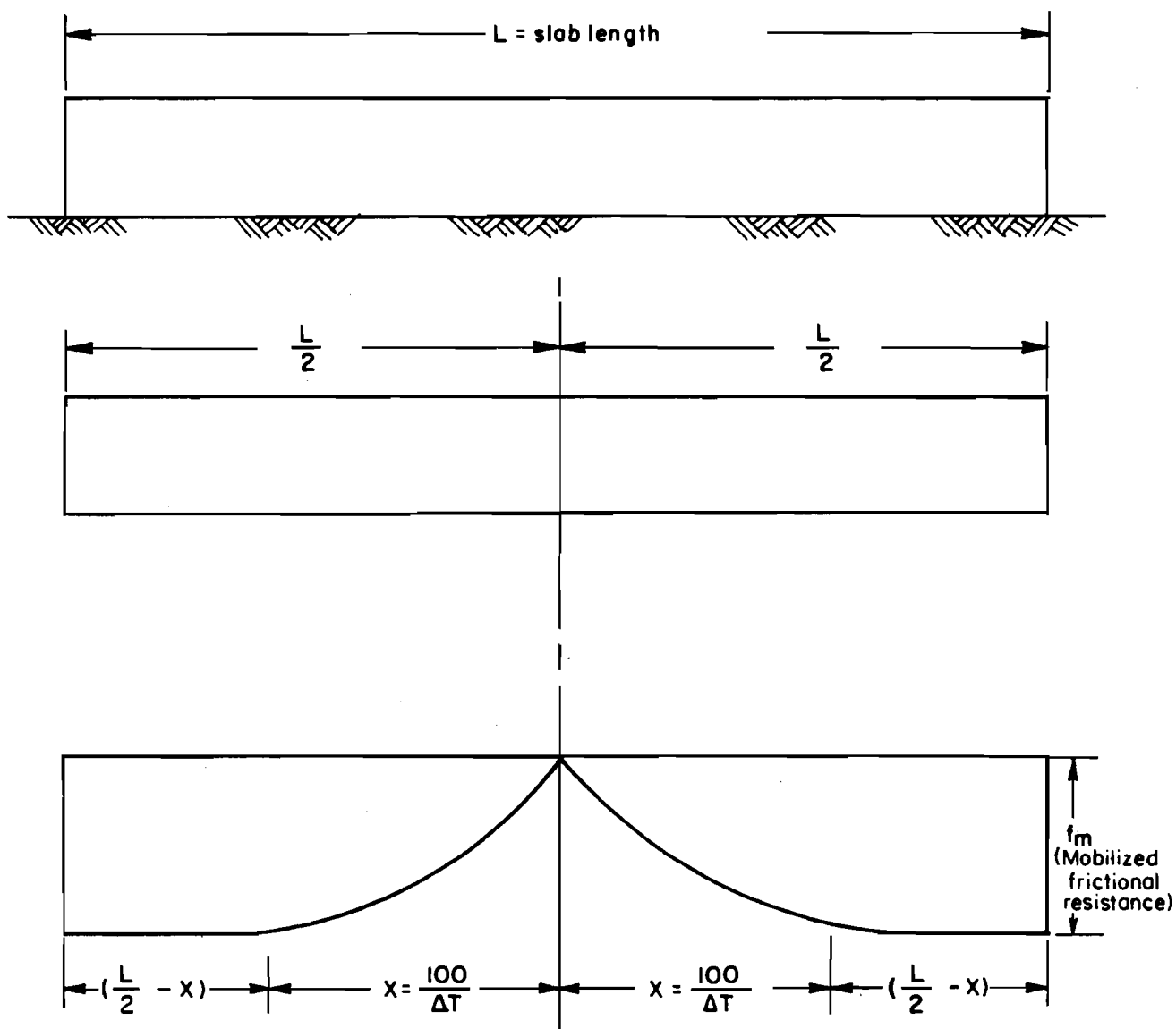
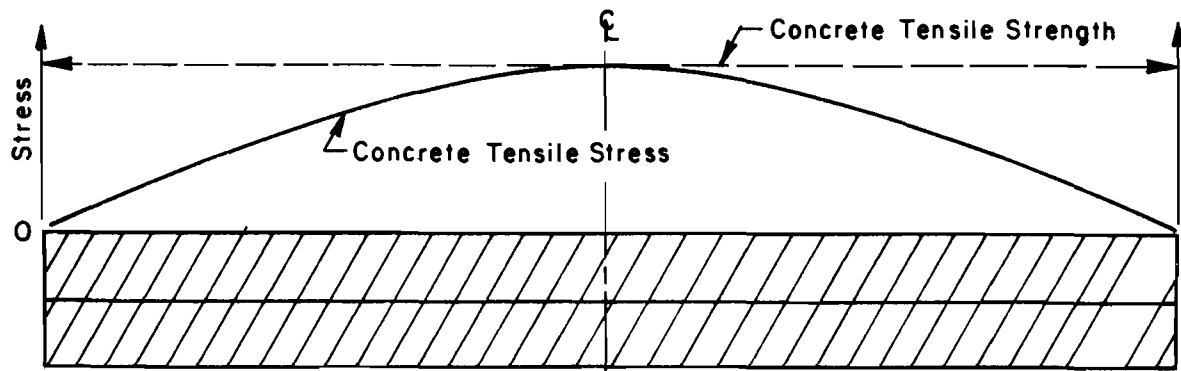
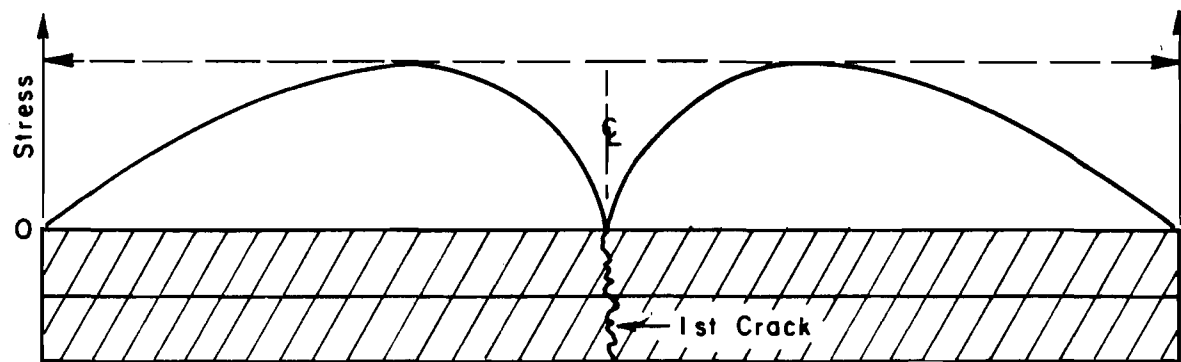


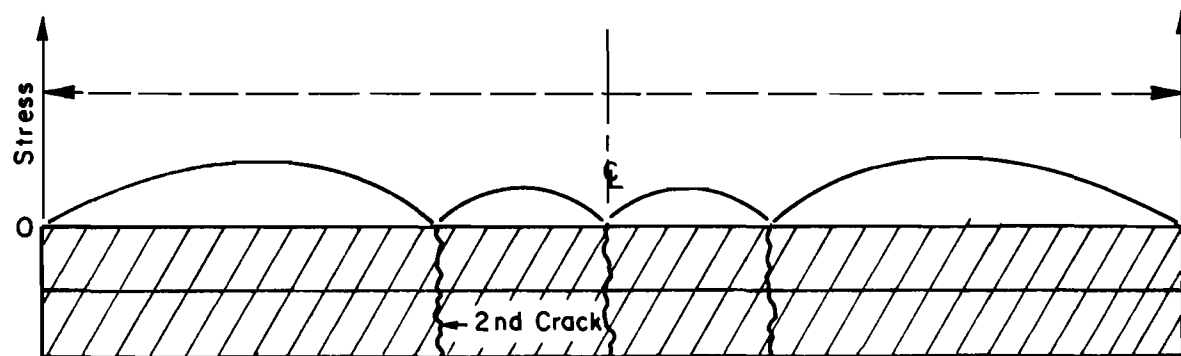
Fig 2.3. Mobilized frictional resistance distribution (Ref 4).



(a) Concrete slab prior to cracking



(b) Concrete slab after first crack



(c) Concrete slab after second crack

Fig 2.4. Crack occurrence in a concrete slab.

The present work will only analyze the possible occurrence of two cracks in the slab, because it is felt that the first crack will be the one with the worst conditions, namely excessive crack width.

Therefore, the first task is to find the concrete stresses at each time. To do this, it is necessary to remember that those stresses are going to be a direct function of frictional resistance, which is going to depend on the slab movement, and the movement depends on slab length, drying shrinkage and temperature drop. The task now is to relate all these factors and predict the concrete stress.



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### CHAPTER 3. THEORY

Temperature drop and shrinkage are variables with time, as is the concrete strength; therefore, the problem is to relate the state of stresses in the slab at every time, from the concrete placement until the concrete gains its full strength. The solution is to find the stress in the concrete due to shrinkage and temperature drop at several time increments, and then compare this stress with the concrete strength also at that time as illustrated in Fig 3.1. At times, shrinkage and temperature drop alone will not cause cracking, but, if we superimpose the stresses due to load, warping or curling, they can produce stresses higher than the concrete strength.

At an early age concrete, the cracking pattern is due basically to the external forces generated by restraint of contractional movements developed by shrinkage and drop in temperature. The restraint is provided by the type of subbase friction and the reinforcing steel and thus generates tensile stresses in the concrete. This phenomenon can be better understood by observing the concrete behavior information taken from Ref 4 which tells us that:

"When cement is mixed with water to form a soft paste, it gradually stiffens until it becomes a solid. The cement is said to have set when it has gained sufficient rigidity to support an arbitrarily defined pressure, after which it continues for a long time to harden. The water in the paste dissolves material at the surfaces of the cement grains and forms a gel which gradually increases in volume and stiffness. This leads to a rapid stiffening of the paste two to four hours after water has been added to the cement. Hydration continues to proceed deeper into the cement grains, at decreasing speed, with continued stiffening and hardening of the mass. In ordinary concrete the cement is probably never completely hydrated. The gel structure of the hardened paste seems to be the main reason for the volume changes which are caused in concrete by variations in moisture, such as the shrinkage of concrete as it dries. According to H. Rusch, for complete hydration of a given amount of cement, an amount of water equal to about 25 percent of that of cement by weight, is needed chemically. An additional 10 to 15 percent must be present, however, to provide mobility for the water in the cement paste during the hydration process so that it can reach the cement particles, this makes for a total minimum water-cement ratio of 0.35 to 0.40 by weight and this ratio corresponds to 4 to gallons (15.14 - 17 lbs) of water per sack of cement. Any amount of water above the 25 percent consumed in the chemical reaction produces pores in the cement paste. The strength of the hardened paste decreases

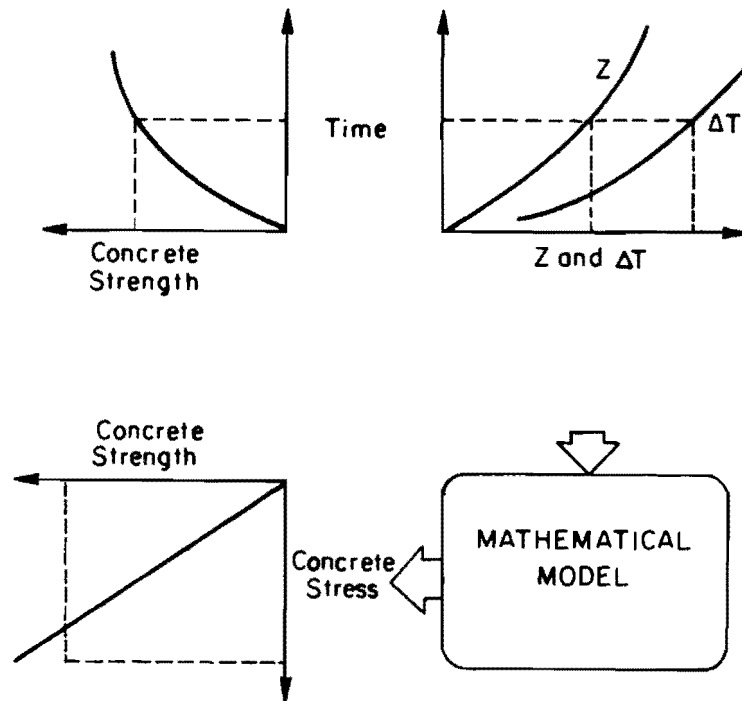


Fig 3.1. Flow chart to relate concrete strength and concrete stresses due to shrinkage ( $Z$ ) and drop in temperature ( $\Delta T$ ) as a function of time.

in inverse proportion of the fraction of the total volume occupied by pores. This is why the strength of the cement paste depends primarily on, and decreases directly with, increasing water cement ratio" (Fig 3.2).

## SHRINKAGE

As discussed above, any workable concrete mix contains more water than is needed for hydration. If the concrete is exposed to air, the larger part of this free water evaporates in time, the rate and completeness of drying depending on ambient temperature and humidity conditions. As the concrete dries, it shrinks in volume, probably due to the capillary tension which develops in the water remaining in the concrete. Now, if dry concrete is immersed in water, it expands, regaining much of the volume loss from prior shrinkage. Shrinkage, which continues at a decreasing rate for several months, is a detrimental property of concrete in several aspects. When not adequately controlled, it will cause unsightly and often detrimental cracks. In structures which are statically indeterminate, it can cause large and harmful stresses. So, the chief factor which determines the amount of final shrinkage is the unit water content of the fresh concrete, as illustrated in Fig 3.3.

It is evident from this, that the chief means of reducing shrinkage is to reduce the water content of the fresh concrete to the minimum compatible with the required workability. In addition, careful and prolonged curing is helpful for shrinkage control (Ref 4). Values of final shrinkage for ordinary concretes are generally in the range of 0.0002 to 0.0007 inch per inch, depending on initial water content, ambient temperature and humidity conditions, and the nature of the aggregate (Ref 7). Highly absorptive aggregates, such as some sandstones and slates, result in shrinkage values twice those obtained with less absorptive materials such as granites and some limestones. Some lightweight aggregates, in view of their great porosity, easily cause much larger shrinkage than ordinary concretes. Hansen and Matlick (Ref 6) made studies of the variability of shrinkage with time. According to them, this variation is a hyperbolic function of time, which can be expressed mathematically as follows:

$$\frac{Z_t}{Z_f} = \frac{t}{M + t} \quad (3.1)$$

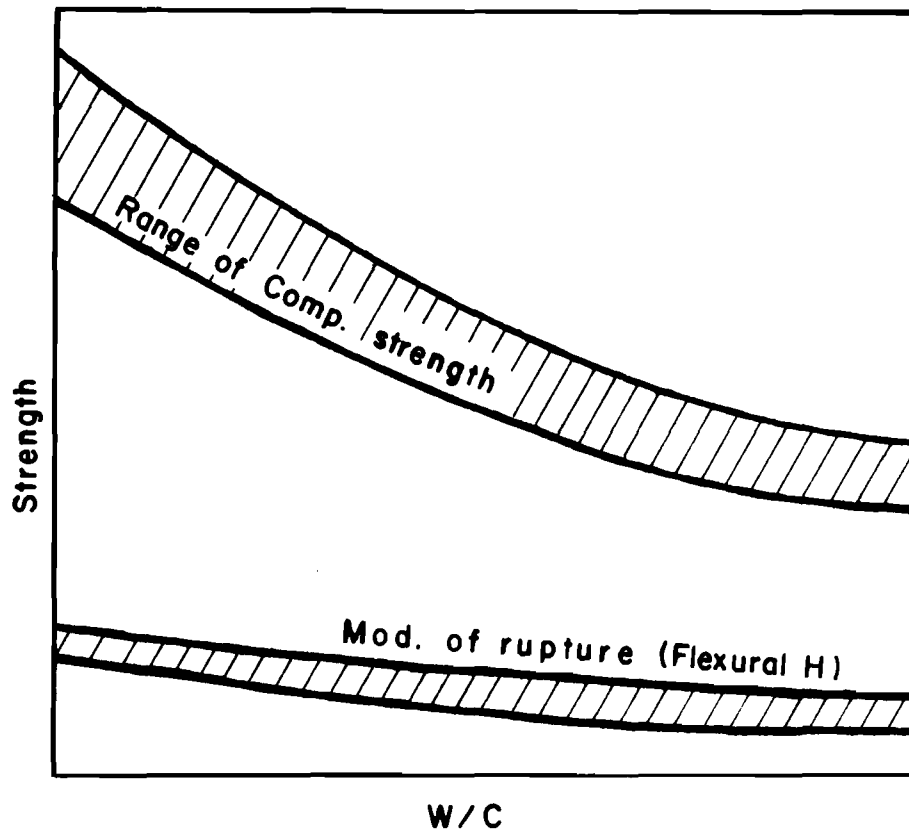


Fig. 3.2. Relationship between concrete strength and W/C ratio (Ref 4).

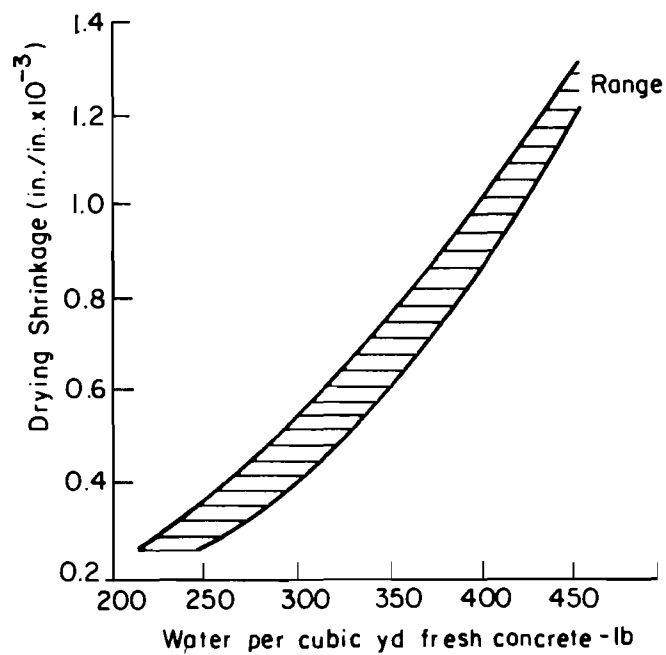


Fig. 3.3. Relationship between drying shrinkage and unit water content (Ref 4).

$$\frac{Z_t}{Z_f} = \frac{t}{M + t} \quad (3.1)$$

$$M = 26e^{0.36} \left( \frac{v}{s} \right) \quad (3.2)$$

- $e$  = base of Napierian log,  
 $t$  = time in days after concrete setting  
 $v$  = volume of the member (inches<sup>3</sup>),  
 $s$  = exposed surface area (inches<sup>2</sup>),  
 $Z_t$  = drying shrinkage at time  $t$ , nad  
 $Z_f$  = final drying shrinkage.

For concrete slabs with dense graded and chemically stabilized sub-bases, the drying occurs from the top surface; thus the  $\left(\frac{v}{s}\right)$  ratio equals to the concrete thickness  $D$ , resulting in the following relationship:

$$Z_t = \left( \frac{t}{26e^{0.36D} + t} \right) Z_f \quad (3.3)$$

Using the above equation and having the final drying shrinkage, the drying shrinkage for any time  $t$  can be obtained for a slab with  $D$  thickness. The slab thickness is a function of the loads that are going to act on the pavement.

#### TEMPERATURE CHANGES

Concrete expands with increasing temperature and contracts with decreasing temperature. The effects of such volume changes are similar to those caused by shrinkage. That is, temperature contraction can lead to undue cracking particularly when superimposed with shrinkage; in indeterminate structures, deformations due to temperature changes can cause large and occasionally harmful stresses. The coefficient of expansion varies somewhat, depending on the type of aggregate and richness of mix. It is generally within the range

of 0.000004 to 0.000006 inch per inch per degree Fahrenheit (Ref 8). A value of  $5.5 \times 10^{-6}$  is generally accepted as satisfactory for calculating stresses and deformations caused by temperature changes. Other factors besides type of aggregate and richness of the mix that cause the coefficient of expansion of thermal coefficient to vary are temperature range, water-cement ratio, concrete age, and relative humidity.

That work assumes that the temperature distribution in the concrete slab is constant, with depth as an approximation. Tomlinson's work demonstrates that this assumption is not true in reality. Tomlinson's theory assumes the temperature varies according to a simple harmonic law. The temperature ( $\theta$ ) at any given depth ( $x$ ) below the surface at any time ( $t$ ) is obtained by means of the following relationships:

$$\theta = \theta_0 e^{-\frac{x}{h} \sqrt{\frac{\pi}{T}}} \sin \left( \frac{2\pi}{T} t - \frac{x}{h} \sqrt{\frac{\pi}{T}} \right) \quad (3.4)$$

and

$$\theta_0^* = \frac{1.5 \theta_{a \max} - \theta_{a \min}}{2} \quad (3.5)$$

where

- $\theta_0$  = amplitude of the temperature cycle at the free surface of the slab,
- $e$  = base of Napierian log,
- $h$  = diffusiveness of the concrete in inches<sup>2</sup>/hour,  
=  $\frac{\text{thermal conductivity}}{\text{heat capacity per unit volume}}$
- $T$  = periodic time of the temperature cycle (24 hours for the daily cycle),
- $\theta_{a \max}$  = maximum air temperature on a particular day, and
- $\theta_{a \min}$  = minimum air temperature.

---

\*Valid only for a six inch slab

## CONCRETE PROPERTIES

Besides shrinkage, other concrete properties in which we are interested for the scope of this work are: thermal coefficient, strength, modulus of elasticity and bond.

Thermal Coefficient. The thermal properties of concrete are primarily a heat transfer process, extracting the excess heat from the concrete keeping the differential volume change at a minimum.

The mineralogical composition of the aggregate is the chief factor affecting the thermal properties of the concrete. From Ref 6, Table 3.1 can be used for recommended values for the thermal coefficient. Other factors are richness of the mix, relative humidity, water-cement ratio, concrete age, and temperature range.

Strength, Modulus of Elasticity and Bond. These three properties are related, and are functions of time. Knowing the tensile strength-time relationship, the flexural strength, the compressive strength, the bond stress, and the modulus of elasticity can be obtained as follows (Ref 7).

The split-tensile strength has a relation with the flexural strength that depends on the coarse aggregate type of the concrete:

<u>Concrete Type</u>	<u>Ratio of Split-tensile Strength to Flexural Strength</u> *
Gravel	5/8
Limestone	2/3
Light-weight Aggregate	3/4

To have a clearer understanding of how to find the compressive strength, bond stress and modulus of elasticity of the concrete, a step-by-step summary will be discussed (Ref 7).

- (1) Find the flexural strength using the above relationship.
- (2) Find the compressive strength ( $f'_c$ ) by using

---

\* Average value



TABLE 3.1. CONCRETE THERMAL COEFFICIENT AS DEPENDENT  
OF AGGREGATE TYPES (Ref 6)

<u>Type of Coarse Aggregate</u>	<u>Concrete Thermal Coefficient (<math>10^{-6}</math> in/in/°F)</u>
Quartz	6.6
Sandstone	6.5
Gravel	6.0
Granite	5.3
Basalt	4.8
Limestone	3.8

$$f'_c = \frac{4000 f_r}{1000 - f_r} \quad (3.6)$$

where

$f_r$  = flexural strength (psi) and  
 $f'_c$  = compressive strength (psi).

(3) Compute modulus of elasticity of the concrete by

$$E_c = \gamma^{1.5} 33 \sqrt{f'_c} \quad (3.7)$$

where

$\gamma$  = unit weight of the concrete (pcf) and  
 $E_c$  = modulus of elasticity of concrete (psi).

(4) Compute the bond stress by using

$$\mu = \frac{9.5 \sqrt{f'_c}}{\phi} \quad (3.8)$$

where

$\mu$  = bond stress (psi) and  
 $\phi$  = bar diameter (inches).

If age-tensile strength data cannot be provided, the solution may still be possible if the 28-day compressive strength is provided, and used with the United States Bureau of Reclamation formula (Ref 3) which gives the percent of the 28-day compressive strength for various intermediate ages as seen in Fig 3.4.

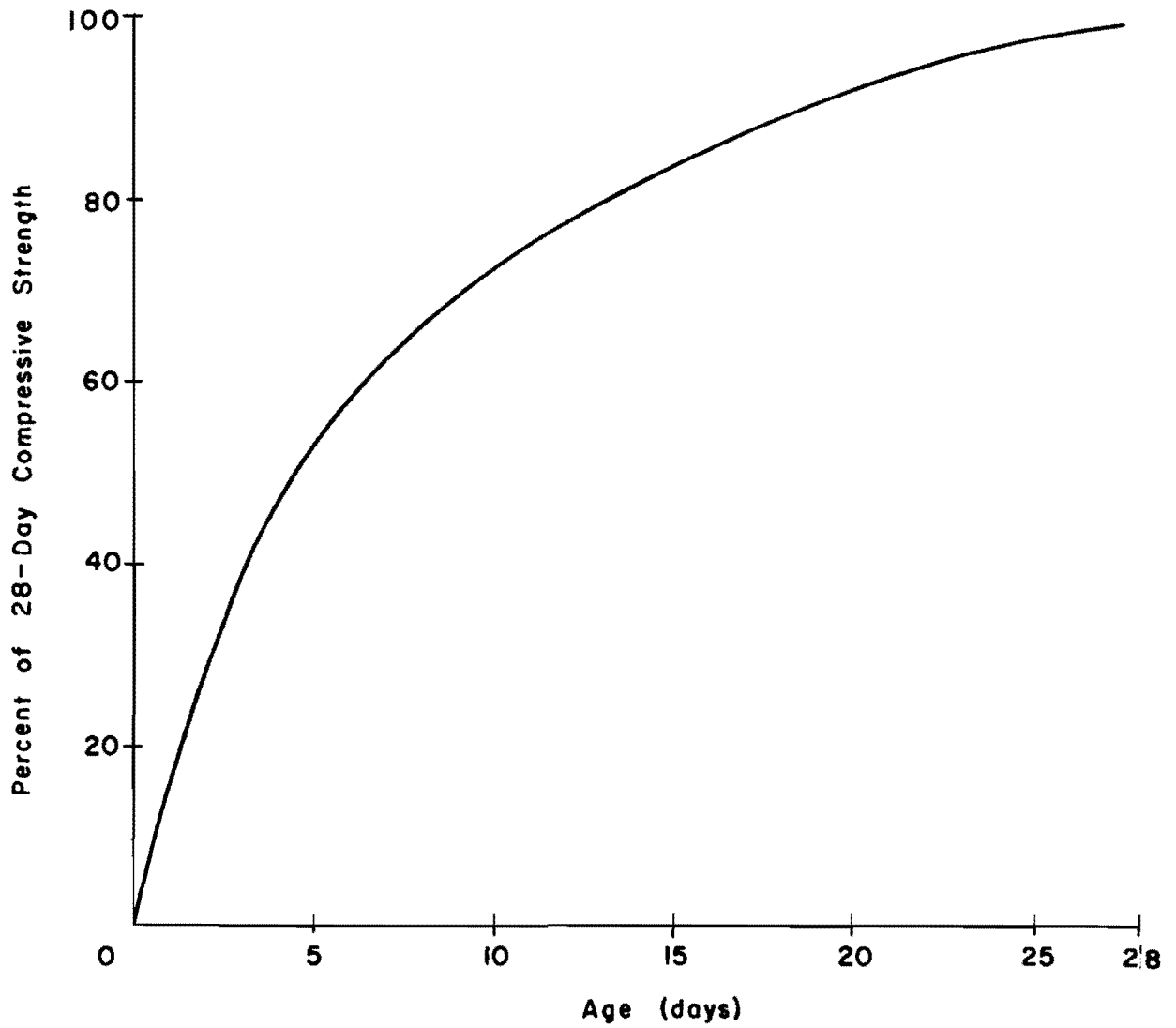


Fig 3.4. Average variation of compressive strength of concrete with age (Ref 3).

From this, it is clear that the concrete compressive strength can be known for each day and the modulus of elasticity for each also can be obtained applying the equation previously mentioned:

$$E_c = \gamma^{1.5} 33 \sqrt{f'_c} \quad (3.7)$$

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## CHAPTER 4. GEOMETRIC MODELS

In Jointed Reinforced Concrete Pavement (JRCP), crack occurrence is due primarily to internal stresses induced by changes in temperature and drying shrinkage. A set of basic equations that describe the stress variations with time is developed in the following sections. The externally induced stresses due to wheel load and other factors are not within the scope of this study, but the stress solutions due to other factors can be easily superimposed.

Two models are necessary for the derivation of the basic equations to represent the behavior of the slab. A JRCP slab is a symmetrical element with each portion having a free end and a fixed end at the centerline of the slab where no movement will occur as graphically represented in Fig 4.1. This model is termed Model-1, and is used to determine the first crack occurrence. If a crack occurs using this model, the behavior of the slab will be different, because there will be two concrete free ends, but the steel is fixed in one end, creating the need of a different model, this model to be termed as Model-2, and is graphically represented in Fig 4.2.

### ASSUMPTIONS

In order to solve the problem, the following assumptions are made:

- (1) The steel and concrete are linearly elastic.
- (2) A crack occurs when the concrete stress is equal to or exceeds the concrete strength.
- (3) After cracking, the concrete stress at the crack is zero.
- (4) The relative movement between concrete and reinforcing steel is zero in the fully bonded sections.
- (5) The frictional resistance to movement of dowels and tie bars is neglected.
- (6) Temperature variations and drying shrinkage are distributed uniformly throughout the slab.
- (7) Material properties are independent of space.
- (8) The friction force-displacement curve is elastic.
- (9) The steel is placed at the neutral axis of the slab.

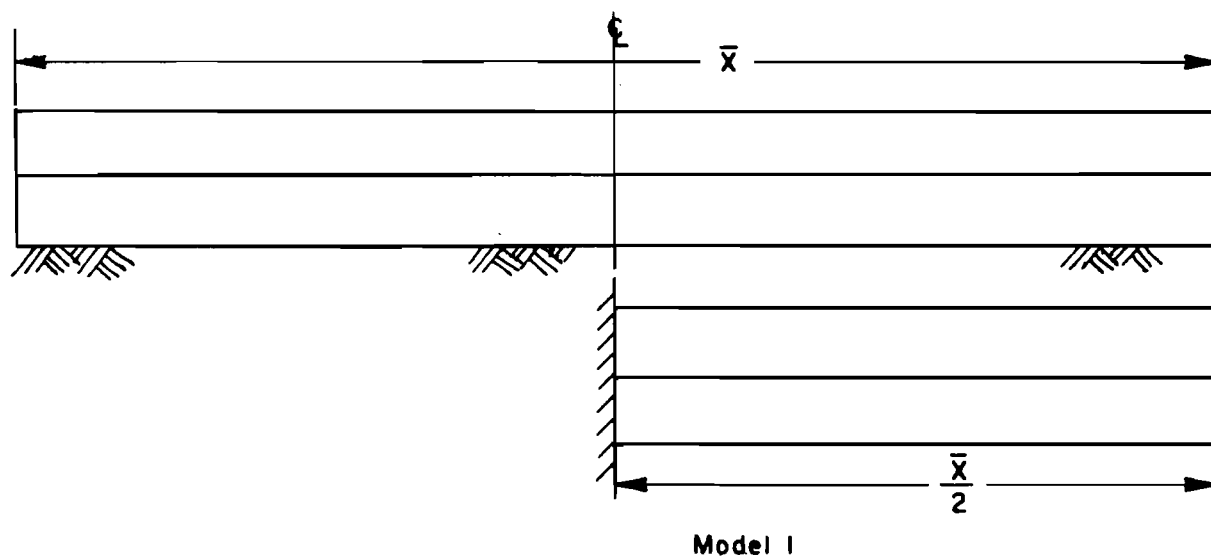


Fig. 4.1. JRCP Geometric model, namely Model-1.

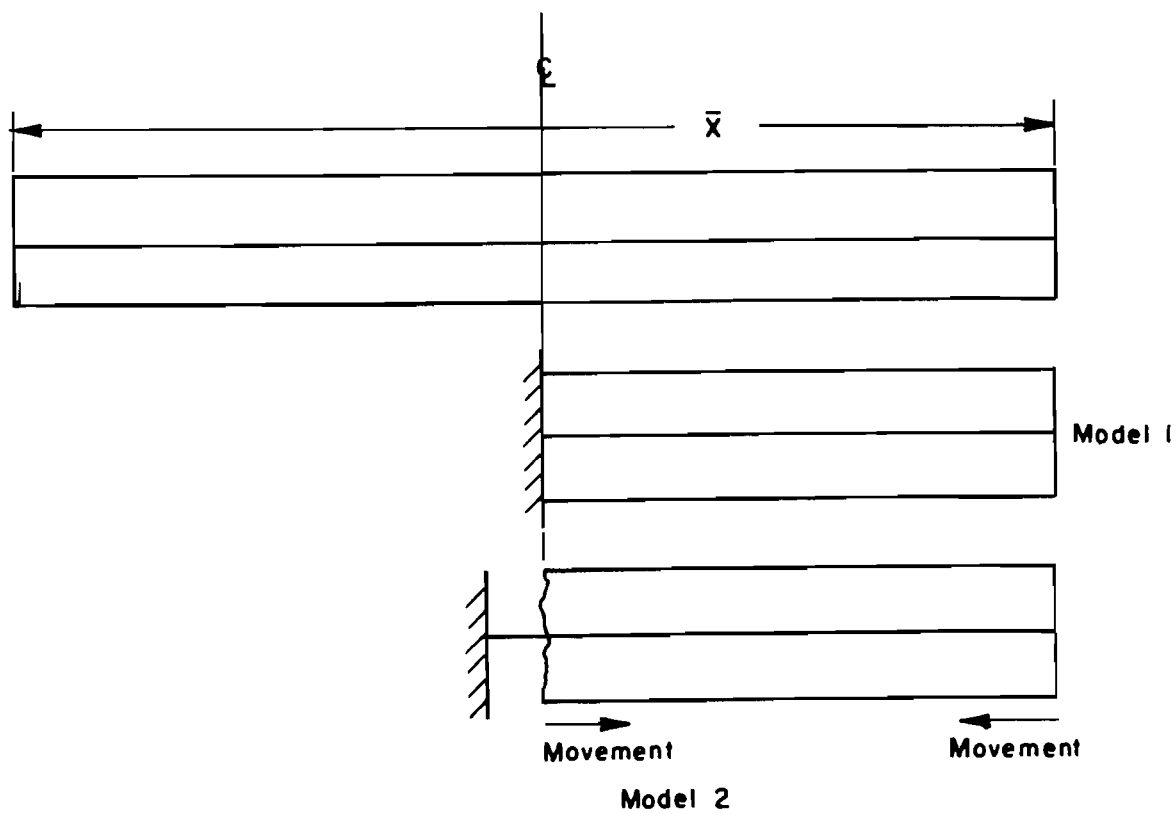


Fig. 4.2. JRCP Geometric model used to search for the second crack, namely Model-2.

## SIGN CONVENTION

- (1) Tension is positive.
- (2) Friction forces in the x-direction are positive.
- (3) Temperature drop is defined as the difference between the temperature at which the concrete set and the minimum temperature at the time of consideration.
- (4) Movements in the x-direction are positive.

Basic Equations for Model-1

For modeling the interaction between concrete, steel and the underlying soil when subjected to drying shrinkage and drop in temperature contractions, the several equations were developed. The concepts developed in Ref 7 for a continuously reinforced concrete pavement were taken as a starting point to solve the geometric Model-1. These equations can be categorized into the following groups:

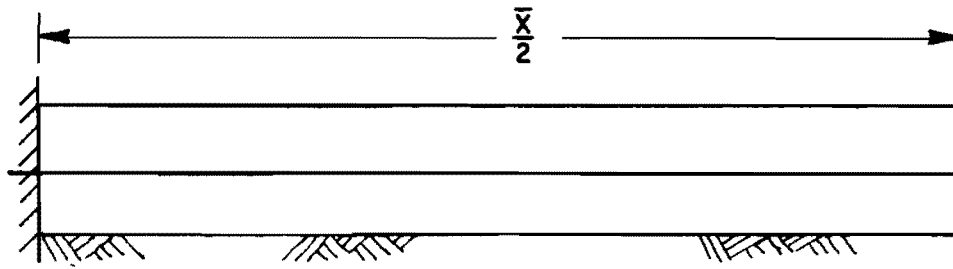
- (1) general equilibrium, and
- (2) compatibility,
  - (a) shrinkage,
  - (b) temperature drop, and
  - (c) friction.

General Equilibrium. A free body diagram for Model-1, and stress distribution in the steel and concrete for a given drying shrinkage strain ( $Z$ ) and temperature drop ( $\Delta T$ ) are shown in Fig 4.3. The steel stress in the fixed end of the model might be tension or compression, depending on the magnitude of the shrinkage and drop in temperature. The concrete stress is always in tension, going from a maximum at the fixed end to zero at the free end;  $\Sigma F_x = 0$  must be satisfied for equilibrium of the system, gives:

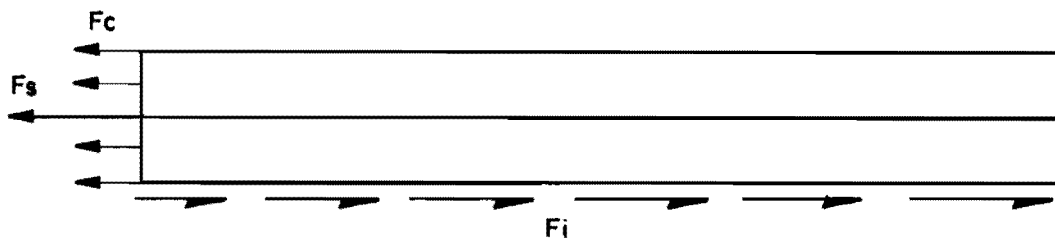
$$\Sigma F_x = 0$$

$$F_c + F_s = \int_0^x F_f dx$$

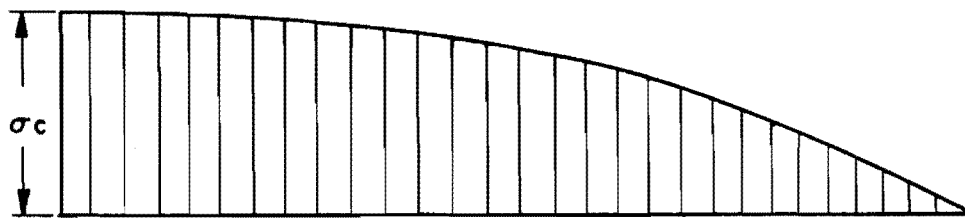




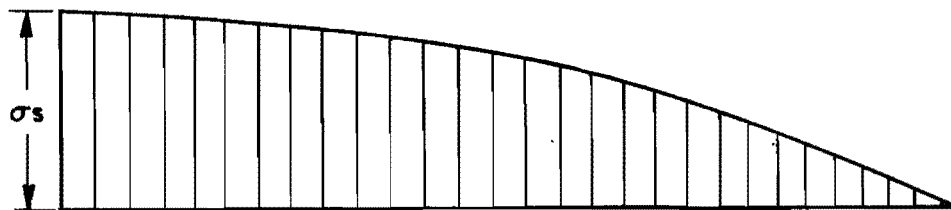
(a) Model-1



(b) Free-body diagram of Model-1



(c) Stress distribution in concrete



(d) Stress distribution in steel

Fig. 4.3. Free body diagram and corresponding stress distribution of Model-1.

or

$$F_c + F_s - \int_0^x F_i' dx = 0 \quad (4.1)$$

where

- $F_c$  = force in the concrete (lb),  
 $F_s$  = force in the steel (lb), and  
 $F_i'$  = friction force per unit length along the slab,  
 $F_i$  = friction force per unit length per unit width.

As we are interested in determining the stresses, then equation 4.1 may be transformed to a stress equation by

$$A_c \sigma_c + A_s \sigma_s - \int_0^x F_i' dx = 0 \quad (4.2)$$

where

- $\sigma_c$  = stress in the concrete, psi,  
 $\sigma_s$  = stress in the steel, psi,  
 $A_s$  = cross-sectional area of longitudinal steel, in<sup>2</sup>, and  
 $A_c$  = cross-sectional area of concrete, in<sup>2</sup>.

For a unit width slab (L), equation 4.2 can be rewritten as

$$D \sigma_c + \frac{A_s}{L} \sigma_s - \int_0^x F_i dx = 0$$

where  $D$  = slab thickness (inches).

Therefore, dividing by  $D$ , the equation becomes

$$\sigma_c + \frac{A_s}{L A_c} \sigma_s - \frac{\int_0^x F_i dx}{D} = 0$$

where

$$L = \text{slab width.}$$

Substituting

$$p = \frac{A_s}{A_c} = \frac{A_s}{DXL}$$

implies

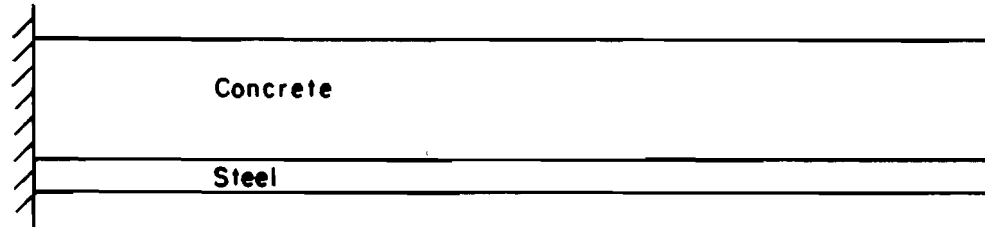
$$\sigma_c + p\sigma_s - \frac{\int_0^x F_i dx}{D} = 0. \quad (4.3)$$

Compatibility Equations for Model-1. The compatibility equations reflect the influence of the interaction between the slab contraction due to shrinkage and drop in temperature and friction in the concrete and steel stresses. For a more clear understanding, separate equations are derived for shrinkage and temperature drop, and then the principle of superimposition is applied to account for the total effect. In the development of the equations for shrinkage and drop in temperature, it was assumed there was no relative movement between concrete and steel.

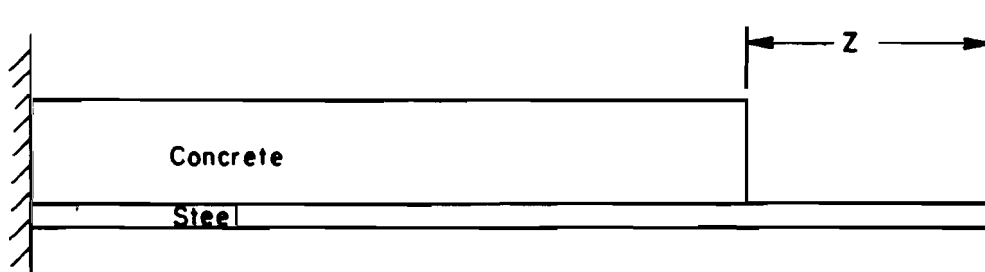
(1) Shrinkage. The development of an equation is achieved by first assuming no bond between steel and concrete; that means that if the concrete contracts in the horizontal direction, no strain will develop because there is no restraint to that movement. But, if the restraint provided by the reinforcing steel (Fig 4.4) is taken into account, the concrete and the steel will experience strains, and the following relationship exists:

$$\epsilon_{cz} + \epsilon_{sz} = Z$$

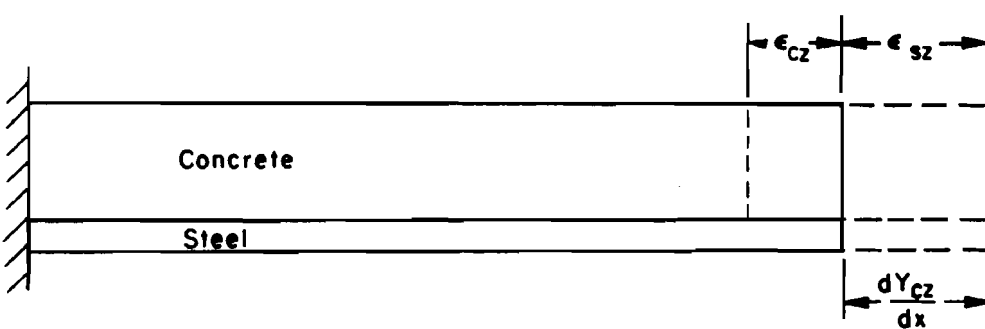
where



(a) State of no shrinkage



(b) Shrinkage without bond between two materials



(c) Shrinkage for a fully bonded condition

Fig. 4.4. Reinforced member behavior when subjected to a uniform shrinkage  $Z$ .

where

- $Z$  = free drying shrinkage strain of concrete,  
 $\epsilon_{cz}$  = concrete strain due to shrinkage (strain of concrete due to restraint of steel),  
 $\epsilon_{sz}$  = steel strain due to shrinkage (strain of steel due to shrinkage of concrete).

The concrete will be in tension, and the steel in compression, then according to the sign convention

$$Z = \epsilon_{cz} + \epsilon_{sz}$$

Converting to stress with sign convention (tension is positive),

$$Z = \frac{\sigma_{cz}}{E_c} + \left( -\frac{\sigma_{sz}}{E_s} \right)$$

rearranging terms,

$$\frac{\sigma_{cz}}{E_c} = Z + \frac{\sigma_{sz}}{E_s}$$

let

$$n = \frac{E_s}{E_c}$$

solving for  $\sigma_{cz}$ ,

$$\sigma_{cz} = E_c Z + \frac{\sigma_{sz}}{n} \tag{4.5}$$

where

$$\begin{aligned}\sigma_{cz} &= \text{stress in the concrete due to shrinkage, } Z, \\ \sigma_{sz} &= \text{stress in steel due to shrinkage, } Z, \\ E_c &= \text{elastic modulus of concrete,} \\ n &= \text{modulus ratio, and} \\ E_s &= \text{elastic modulus of steel.}\end{aligned}$$

(2) Drop in Temperature. The variations in temperature tend to cause volume changes in both the steel and the concrete. As the air temperature goes below the casting temperature, the material contracts and induces tensile stresses in the concrete. In this work, both steel and concrete thermal properties are characterized by the linear coefficient of contraction or expansion. As previously pointed out, the aggregate type governs the concrete thermal coefficient.

To solve the problem, the concrete and steel are assumed to be fully bonded, meaning that both materials will have the same movement. From Fig 4.5 for a unit length slab, the following may be derived:

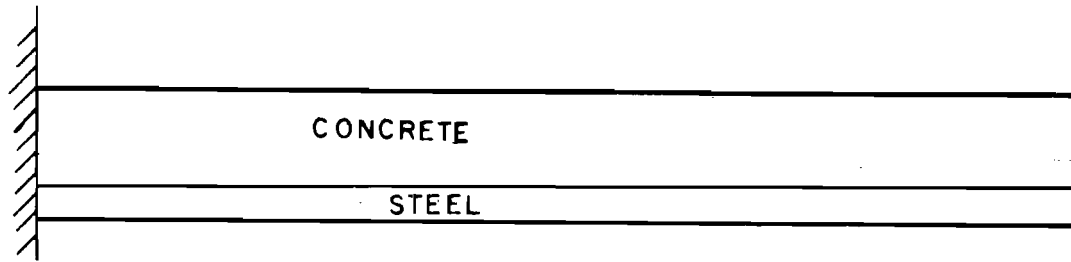
$$\begin{aligned}\epsilon_{c\Delta T} - \epsilon_{s\Delta T} &= \Delta T (\alpha_c - \alpha_s) \\ \epsilon_{c\Delta T} &= \Delta T (\alpha_c - \alpha_s) + \epsilon_{s\Delta T}\end{aligned}\tag{4.6}$$

where

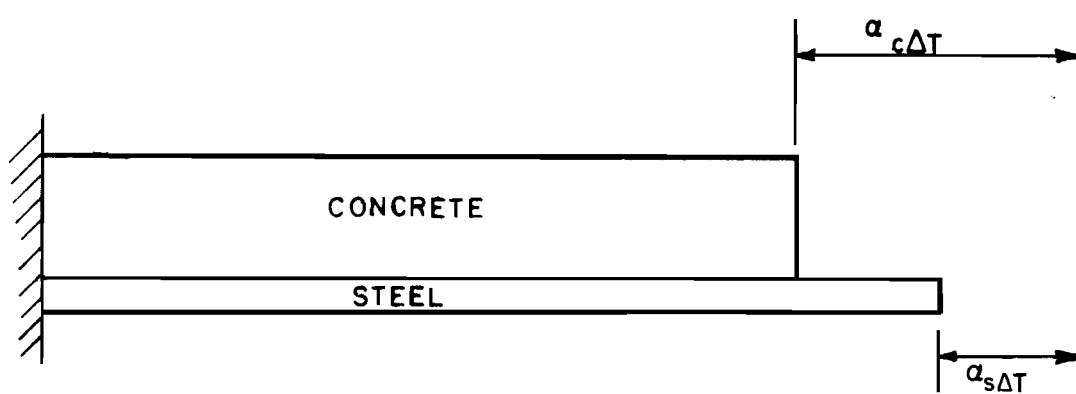
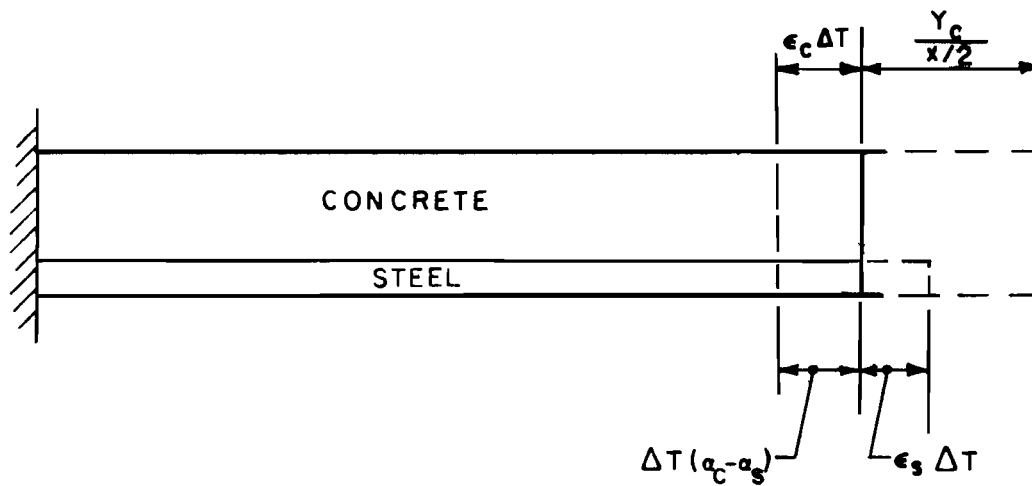
$$\begin{aligned}\epsilon_{c\Delta T} &= \text{strain in the concrete due to a temperature drop } \Delta T, \\ \epsilon_{s\Delta T} &= \text{strain in the steel due to a temperature drop } \Delta T, \\ \Delta T &= \text{drop in concrete temperature } (^{\circ}\text{F}), \\ \alpha_c &= \text{concrete linear thermal coefficient } (^{\circ}\text{F}), \text{ and,} \\ \alpha_s &= \text{steel linear thermal coefficient } (^{\circ}\text{F}).\end{aligned}$$

For a stress equation, equation 4.6 can be written

$$\sigma_{c\Delta T} = \Delta T (\alpha_c - \alpha_s) E_c + \frac{\sigma_{s\Delta T}}{n}\tag{4.7}$$



(a) Undisturbed state

(b) Contraction due to  $\Delta T$  with complete slippage between concrete and steel. No restriction condition(c) Contraction due to  $\Delta T$  with no slippage between concrete and steel.Fig 4.5. Reinforced element subjected to uniform temperature drop  $\Delta T$ .

where

$$\begin{aligned}\sigma_{c\Delta T} &= \text{stress in the concrete due to } \Delta T \text{ (psi),} \\ \sigma_{s\Delta T} &= \text{stress in the steel due to } \Delta T \text{ (psi).}\end{aligned}$$

If the principle of superimposition is applied to the concrete and steel stresses due to  $Z$  and  $\Delta T$ , the total stress can be predicted as follows:

$$\begin{aligned}\sigma_c &= \sigma_{cz} + \sigma_{c\Delta T} \\ \sigma_s &= \sigma_{sz} + \sigma_{s\Delta T}\end{aligned}$$

Substituting the values of  $\sigma_{cz}$  and  $\sigma_{c\Delta T}$  from Eqs 4.5 and 4.7,

$$\sigma_c = \frac{\sigma_s}{n} + E_c [Z + \Delta T (\alpha_c - \alpha_s)] \quad (4.8)$$

Equation 4.8 represents the effects of shrinkage and drop in temperature in the concrete slab.

(3) Friction. When a concrete slab contracts due to loss in moisture and drop in temperature, the local movement of the slab increases from zero at the geometric center of the slab to a maximum at the edges as shown in Fig 4.6. This movement, if restrained, will produce stresses in the slab as happens when the base friction acts. The stresses produced in the slab by the base restraint will decrease from a maximum at the geometric center of the slab to zero at the free edges. Therefore, tensile stresses will be generated by this restraint to the slab, increasing the tensile stresses created by the reinforcing steel which also restrains the contraction of the concrete.

The frictional resistance increases with movement; therefore, its effect should be represented by the complete curve defining the friction-movement relationship. Considering the free body diagram of a slab element of length  $dx$ , which experiences a movement  $Y_c$  and a corresponding friction force  $F_i$  (Fig 4.7), then  $\sum F_x = 0$  gives



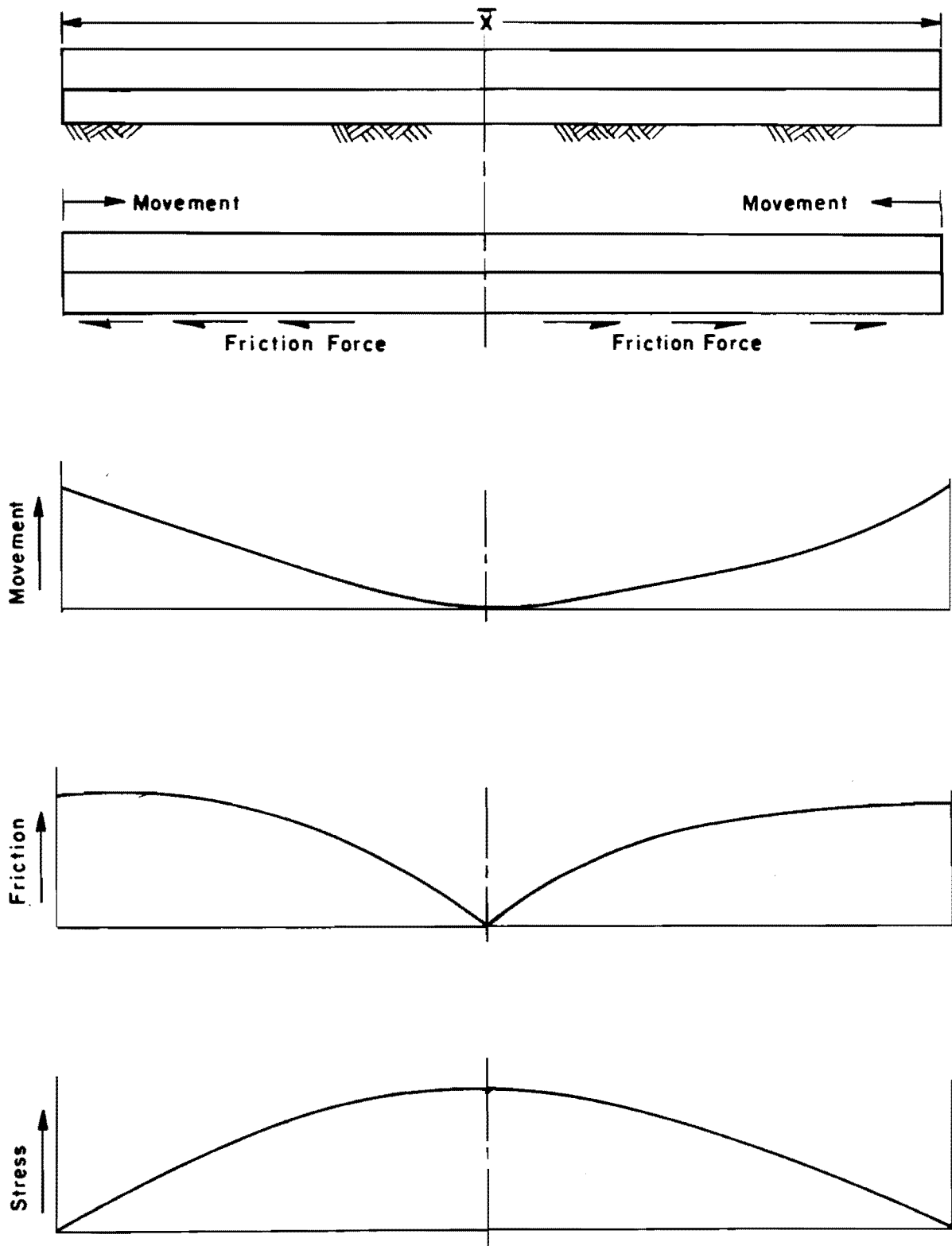
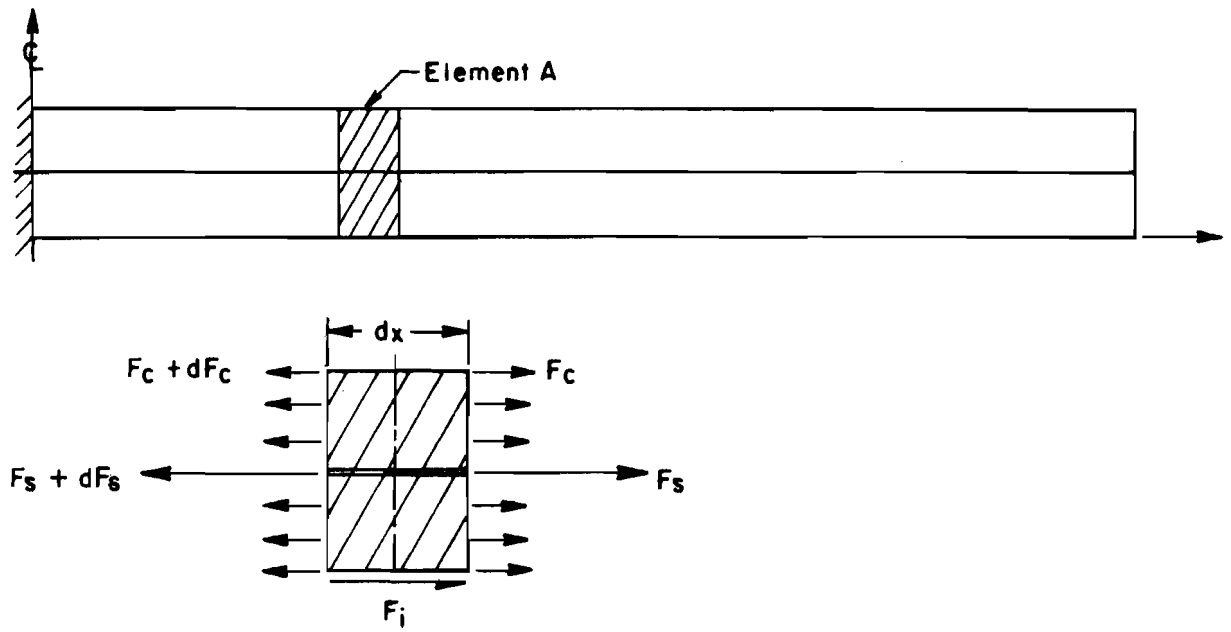
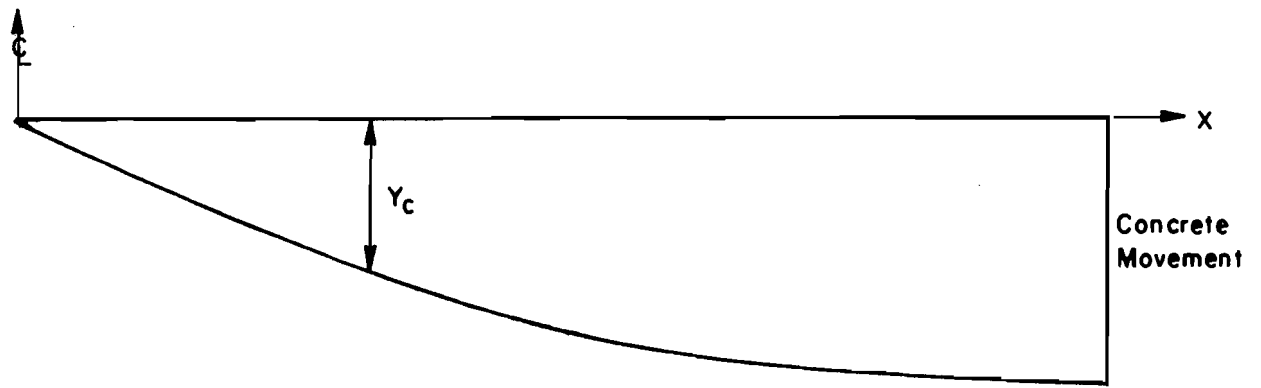


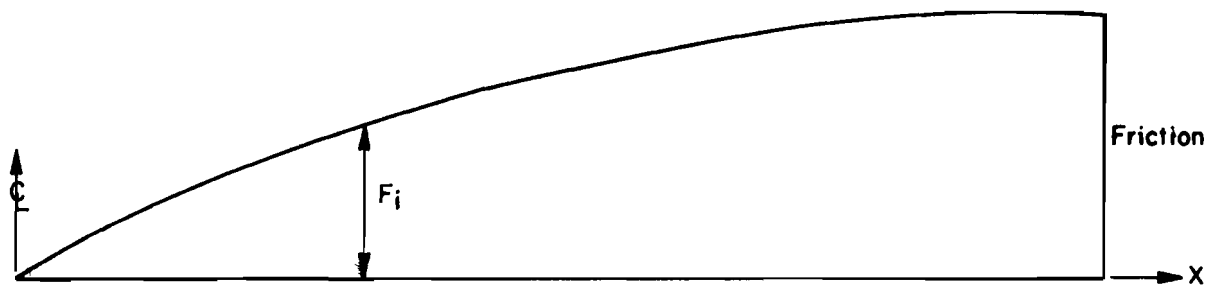
Fig 4.6 Effect of the restraint, provided by the subbase on a concrete slab.



(a) Free body diagram of element A.



(b) Concrete movement



(c) Frictional resistance

Fig. 4.7. Free body diagram of an element in Model-1.

$$dF_c + dF_s = -F_i' dx$$

or expressed into a stress equation:

$$\begin{aligned} A_c d\sigma_c + A_s d\sigma_s &= -F_i' dx \\ d\sigma_c + p d\sigma_s &= -\frac{F_i}{D} dx \end{aligned} \quad (4.9)$$

but from Eq. 4.8 and since material properties are assumed to be independent of space (assumption 7) we conclude:

$$\sigma_c = \frac{\sigma_s}{n} + E_c [Z + \Delta T (\alpha_c - \alpha_s)] \quad (4.8)$$

Differentiating, with respect to  $x$ ,

$$\frac{d\sigma_c}{dx} = \frac{d\sigma_s}{dx} \times \frac{1}{n} + 0$$

and solving for  $d\sigma_s$

$$d\sigma_s = n d\sigma_c \quad (4.10)$$

Substituting into equation 4.9

$$\begin{aligned} d\sigma_c + p n d\sigma_c &= \frac{F_i dx}{D} \\ \frac{d\sigma_c}{dx} &= \frac{F_i}{D} \frac{1}{(1 + pn)} \end{aligned} \quad (4.11)$$

With equation 4.11, the inclusion of the friction forces into the generalized system of equations is possible.

Equation 4.11 shows the concrete stress changes at a rate along the slab, which is a function of the frictional resistance between the base and the slab.

(4) Movement of Concrete. The local movements of the slab are required in order to compute the frictional resistance. As pointed out before, different points along the slab will experience different movements which go from a maximum value at the free edges to zero at the geometric center of the slab.

The slab movement can be obtained when superimposing the movements due to shrinkage and drop in temperature as follows:

for shrinkage:

$$\frac{dY_{cz}}{dx} = \epsilon_{cz} - Z$$

Integrating:

$$Y_{cz} = \int_0^x \epsilon_{cz} dx - Zx + k_1 \quad (4.12)$$

for temperature:

$$\frac{d Y_{c\Delta T}}{dx} = \epsilon_{c\Delta T} - \alpha_c \Delta T$$

Integrating:

$$Y_{c\Delta T} = \int_0^x \epsilon_{c\Delta T} - \alpha_c \Delta T x + k_2 \quad (4.13)$$

Thus,

$$Y_c = Y_{c\Delta T} + Y_{cz} \quad (4.14)$$

where

$$\begin{aligned}
 Y_{cz} &= \text{concrete movement due to shrinkage (inches)} \\
 Y_{c\Delta T} &= \text{concrete movement due to drop in temperature (inches)} \\
 Y_c &= \text{total concrete movement at the joint due to } Z \text{ and } \Delta T \\
 &\quad \text{(inches), and} \\
 k_1, k_2 &= \text{constants of integration.}
 \end{aligned}$$

Then, from 4.12, 4.13, and 4.14

$$Y_c = \int_0^x \epsilon_{c\Delta T} dx - \alpha_c \Delta T x + \int_0^x \epsilon_{cz} dx - Zx + k_2 + k_1$$

If

$$\epsilon_c = \epsilon_{c\Delta T} + \epsilon_{cz}$$

$$k_3 = k_2 + k_1$$

then

$$Y_c = \int_0^x \epsilon_c dx - (Z + \alpha_c \Delta T)x + K_3$$

But at  $x = 0$ ,  $Y_c = 0$ .

Therefore,

$$Y_c = \int_0^x \epsilon_c dx - (Z + \alpha_c \Delta T)x \quad (4.15)$$

or if expressed into a stress equation,

$$Y_c = \int_0^x \frac{\sigma_c}{E_c} dx - (Z + \alpha_c \Delta T)x \quad (4.16)$$

(5) Joint Width. From equation 4.15, it is possible to evaluate the joint width, by integrating at  $x = \frac{\bar{x}}{2}$  as follows:

$$Y_j = \int_0^{\frac{\bar{x}}{2}} \frac{\sigma_c}{E_c} dx - (Z + \alpha_c \Delta T)x$$

But  $Y_c$  will be the concrete movement of one half of the slab, thus if  $\Delta X$  is the joint width, it can be written that

$$\begin{aligned} \Delta X_j &= 2 Y_c = 2 \left( \frac{\sigma_c}{E_c} \frac{\bar{x}}{2} - (Z + \alpha_c \Delta T) \frac{\bar{x}}{2} \right) \\ \Delta X_j &= \bar{x} \left[ \frac{\sigma_c}{E_c} - (Z + \alpha_c \Delta T) \right] \end{aligned} \quad (4.17)$$

where

$\Delta X$  = joint width (inches), and

$\bar{x}$  = total length of the slab (inches).

It is very important to know the width of a joint, because limiting it to a maximum value that will provide load transfer and avoid percolation, the design of the required steel percentage to produce that condition can be determined using a trail and error procedure.

With the equations previously developed, Model-1 can be solved for stresses, strains, movements and joint width, but these equations are not sufficient enough to solve Model-2 which is required after the first crack occurs.

#### Basic Equations for Model-2

After the first crack occurs, Model-1 will change into Model-1 plus Model-2, because the portion of the slab going from the crack to the free end will have one end with longitudinal steel in the crack resisting and the other end free. A problem of bond development length is present at the crack, because the steel requires some finite length to transmit the stress to the concrete. Both ends will contract, but the one with the steel, in a fixed

condition, will have more restraint. Consequently, the point of zero movement will be more towards the crack side as represented in Fig 4.8.

From Fig 4.9 the need for Model-2, that consists of a portion of the slab with a fixed end can be seen. The boundary conditions for Model-2 are similar to the model developed in Ref 7 to solve a continuously reinforced concrete pavement.

The basic equations for Model-1 are also useful for this model taking into account the signs, but they are not sufficient to solve the problem. As previously discussed, the steel stress at the crack will be transmitted to the concrete through a development length or a bond slip length. The steel at the crack is under considerable tension since the concrete provides no resistance. However, beyond the crack, the concrete does resist moderate amounts of tension stresses, reducing the tensile forces in the steel, creating a variable force in the bar. From this, it can be seen that an equation for this bond slip zone is needed.

Bond Slip Zone Equation. Since the steel bar must be in equilibrium, the change in bar force is resisted at the contact surface between concrete and steel. From the free body diagram in Fig 4.10 for the steel bar,  $\Sigma F_x = 0$  yields:

$$F_s - (F_s + dF_s) + Udx = 0$$

where

$$U = \text{average bond force per unit length of the slab.}$$

Therefore:

$$\frac{dF_s}{dx} = U \quad (4.18)$$

Since

$$U = \mu \Sigma_o \quad (4.19)$$

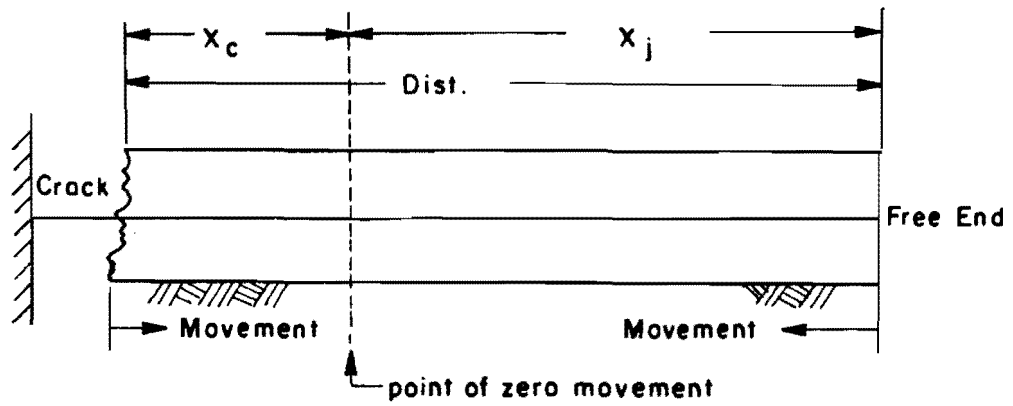


Fig 4.8. Behavior of the slab after the first crack.

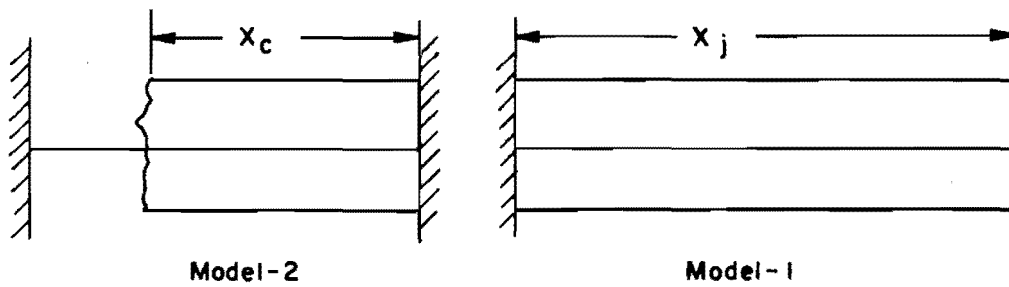


Fig 4.9. Geometric models needed to search for the second crack.



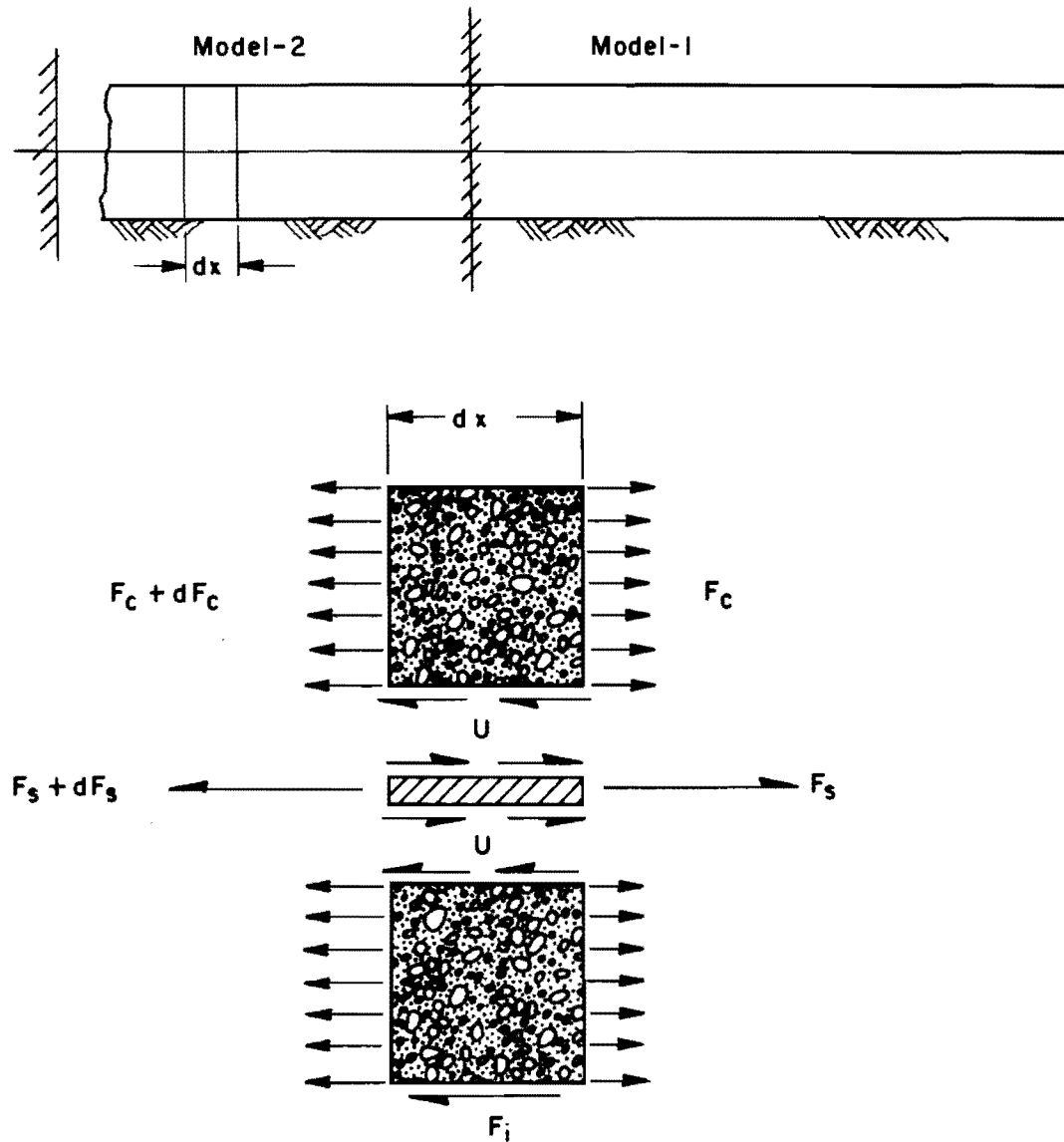


Fig. 4.10. Free body diagram of an element in the bond slip zone of Model-2.

where

$$\begin{aligned} \mu &= \text{bond stress; } \mu = \frac{9.5 \sqrt{f'_c}}{\phi} , \\ f'_c &= \text{compressive strength of concrete,} \\ \Sigma_o &= \text{perimeter of the bar(s).} \\ \phi &= \text{bar diameter.} \end{aligned}$$

Substituting the value of  $U$  from Eq 4.19 into Eq 4.18

$$\frac{dFs}{dx} = \mu \Sigma_o \quad (4.20)$$

and transforming equation 4.20 to a stress equation using

$$Fs = \sigma_s A_s$$

yields

$$A_s \frac{d\sigma_s}{dx} = \mu \Sigma_o$$

and

$$\frac{d\sigma_s}{dx} = \frac{\mu \Sigma_o}{A_s}$$

Since

$$A_s = \frac{\pi \phi^2}{4}$$

and

$$\Sigma_o = \pi \phi$$

then

$$\frac{d\sigma_s}{dx} = \frac{\mu\pi\phi}{\frac{\pi\phi}{4}} = \frac{4\mu}{\phi}$$

Therefore:

$$\frac{d\sigma_s}{dx} = \frac{4\mu}{\phi} \quad (4.21)$$

For a constant bond stress  $\mu$ , the variation of the distribution of steel stress in the bond slip zone is linear. The slope in the concrete stress curve in the bond slip zone also depends on the bond properties; then, if  $\Sigma F_x = 0$  is applied to the concrete element in Fig 4.10, the following is obtained:

$$F_c - (F_c + dF_c) - F'_i dx - U dx = 0$$

$$dF_c + F'_i dx + U dx = 0$$

$$dF_c = -F'_i dx - U dx$$

$$\frac{dF_c}{dx} = -F'_i - U$$

Since

$$p = \frac{A_s}{A_c} \text{ and } \sigma_c = \frac{F_c}{A_c}$$

then

$$\frac{d\sigma_c}{dx} \cdot A_c = -F'_i - \mu \Sigma_o$$

$$\frac{d\sigma_c}{dx} = \frac{F'_i}{A_c} - \frac{\mu p \Sigma_o}{A_s}$$

$$\frac{d\sigma_c}{dx} = \frac{-F'_i}{A_c} - \frac{\mu p \pi \phi}{\frac{\pi \phi^2}{4}}$$

$$\frac{d\sigma_c}{dx} = \frac{-F'_i}{A_c} - \frac{4\mu p}{\phi}$$

For a unit width slab  $A_c = D \times 1$ , then

$$\frac{d\sigma_c}{dx} = -\frac{F'_i}{D} - \frac{4\mu p}{\phi} \quad (4.22)$$

The shape of the concrete stress curve can be linear if the maximum frictional resistance force is developed, because the slope of that curve is a function of bond as well as bond properties as can be seen in Eq 4.22.

Also, the general equilibrium for Model-2 is different than the one for Model-1, because of the steel being fixed at one end of the slab. Figure 4.11 shows the free-body diagram for Model-2, and solving for equilibrium of the system,  $\sum F_x = 0$  yields

$$F_{so} + F_{co} - F_{sc} - \int_0^x F'_i dx = 0 \quad (4.23)$$

where

- $F_{so}$  = force in the steel at point of zero movement (lb),
- $F_{co}$  = force in the concrete at point of zero movement (lb),
- $F_{sc}$  = force in the steel at the crack (lb), and
- $F'_i$  = friction force per unit length along the slab (lb/in).

Transforming Eq 4.23 to a stress equation,

$$A_s \sigma_{so} + A_c \sigma_{co} - A_s \sigma_{sc} - \int_0^x F'_i dx = 0 \quad (4.24)$$

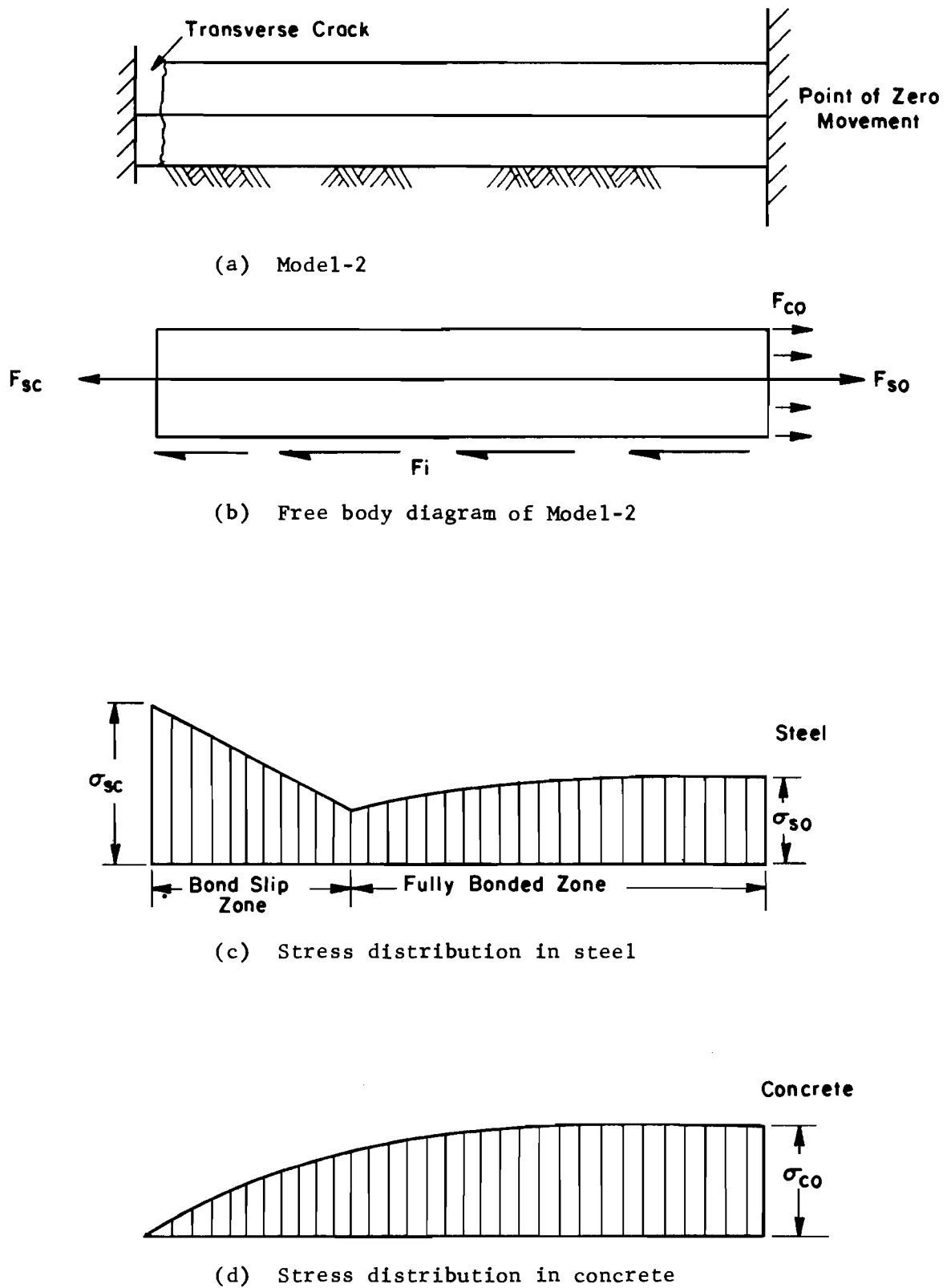


Fig 4.11. Free-body diagram and corresponding stress distribution of Model-2.

and for a unit width slab

$$p\sigma_{so} + \sigma_{co} - p\sigma_{sc} - \frac{\int_0^x F dx}{D} = 0$$

or

$$\sigma_{co} + p\sigma_{so} = p\sigma_{sc} + \frac{\int_0^x F dx}{D} \quad (4.25)$$

At transverse cracks, local lateral movement will not be experienced by the steel. This means that the length of the steel bars will remain constant with temperature changes, then,

$$e_s = \alpha_s \Delta T$$

for  $x$ ,

$$\int_0^a e_s dx = \alpha_s a \Delta T$$

$$\int_a^b e_s dx = \alpha_s b \Delta T$$

where

$X_c$  = the distance between the first crack and the point of zero movement.

Since

$$X_c = a + b$$

substituting for  $a + b$ ,

$$\int_0^a e_s dx + \int_a^b e_s dx = \alpha_s \Delta T X_c$$

and

$$\sigma_s = \epsilon_s \cdot E_s$$

therefore

$$\int_0^a \sigma_s dx + \int_a^b \sigma_s dx = E_s \alpha_s X_c T \quad (4.26)$$

where

- a = fully bonded length of  $X_c$  ,  
 b = bond slip zone.

#### Summary of Equations

A summary of equations for each model follows to clarify for the reader which equations apply to each model:

Model-1:

(1) Equilibrium

$$\sigma_c + p\sigma_s - \frac{\int_0^x F_i dx}{D} = 0 \quad (4.3)$$

(2) Concrete stress due to shrinkage and drop in temperature

$$\sigma_c = \frac{\sigma_s}{n} + E_c \left[ Z + \Delta T(\alpha_c - \alpha_s) \right] \quad (4.8)$$

(3) Friction

$$\frac{d\sigma_c}{dx} = \frac{-F_i}{D} \times \frac{1}{(1+pn)} \quad (4.11)$$

(4) Concrete movement at joint

$$Y_c = \int_0^x \frac{\sigma_c}{E_c} dx - (Z + \alpha_c \Delta T)x \quad (4.16)$$

(5) Joint width

$$\Delta X_j = x \left[ \frac{\sigma_c}{E_c} - (Z + \alpha_c \Delta T) \right] \quad (4.17)$$

Model-2:

(1) Equilibrium

$$\sigma_{co} + p\sigma_{so} - p\sigma_{sc} + \frac{\int_0^x F_i dx}{D} \quad (4.25)$$

(2) Concrete stress due to shrinkage and drop in temperature,

$$\sigma_c = \frac{\sigma_s}{n} + E_c [Z + \Delta T (\alpha_c - \alpha_s)] \quad (4.8)$$

(3) Friction,

$$\frac{d\sigma_c}{dx} = - \frac{F_i}{D} \times \frac{1}{(1+pn)} \quad (4.11)$$

(4) Crack width

$$\Delta X_c = 2 \left[ \int_0^{x_c} \frac{\sigma_c}{E_c} dx - (Z + \alpha_c \Delta T) X_c \right]$$

(5) Steel boundary conditions

$$\int_0^a \sigma_s dx + \int_a^b \sigma_s dx = E_s \alpha_s X_c \Delta T \quad (4.26)$$



### The Approach

The work done in Research Project NCHRP 1-15 (Ref 7) reduced the degree of difficulty in solving this problem. The mathematical model developed in the above research project corresponds to the Model-2 and makes the solution of this work less problematic.

The first step in solving this problem is to search for the time and slab position at which the crack will occur. The approach used will be to divide the slab length into  $N$  number of increments and solve the basic equation for Model-1 ( $N/2$ ) times for a fixed time and change the length of the model by adding one  $\Delta X$  to the previous one for each new cycle, as illustrated in Fig 4.12. This means that for a given time, the concrete stress-distance relationship will be known and will change with time as shown in Fig 4.13.

To know if cracking of the slab is going to occur, the concrete stress-distance relationship for each time is equated to the concrete strength at the corresponding time. The remaining equation is solved for distance, and this distance is compared with  $\bar{x}/2$  and if it is equal or less, a crack is going to occur. If the distance is greater than  $\bar{x}/2$ , there will be no crack.

If a crack does occur, say at time  $t_1$ , then the problem changes into a different one, because now the slab will have only the steel at the crack. This steel bar takes all the tensile stresses generated at that point, and then throughout the bond-slip zone, the concrete receives part of the total tensile stresses. Due to shrinkage and temperature drop, this portion of the slab will tend to contract. The restraint to the movement of contraction at the free end will be provided by the friction resistance between slab and base, and by the reinforcing steel. At the other end, that is where the first crack occurred, the same restrictions as for the other end apply plus the restriction given by the steel that is fixed to the other face of the crack as shown in Fig 4.14.

It is obvious that the solution for the second crack is not possible to achieve by using one model. The approach to find the solution is to solve Model-1 and Model-2 separately for the time which follows the occurrence of the first crack. Then find the corresponding curves for each model of the concrete stress-distance relationship (Fig 4.15a) and then find the

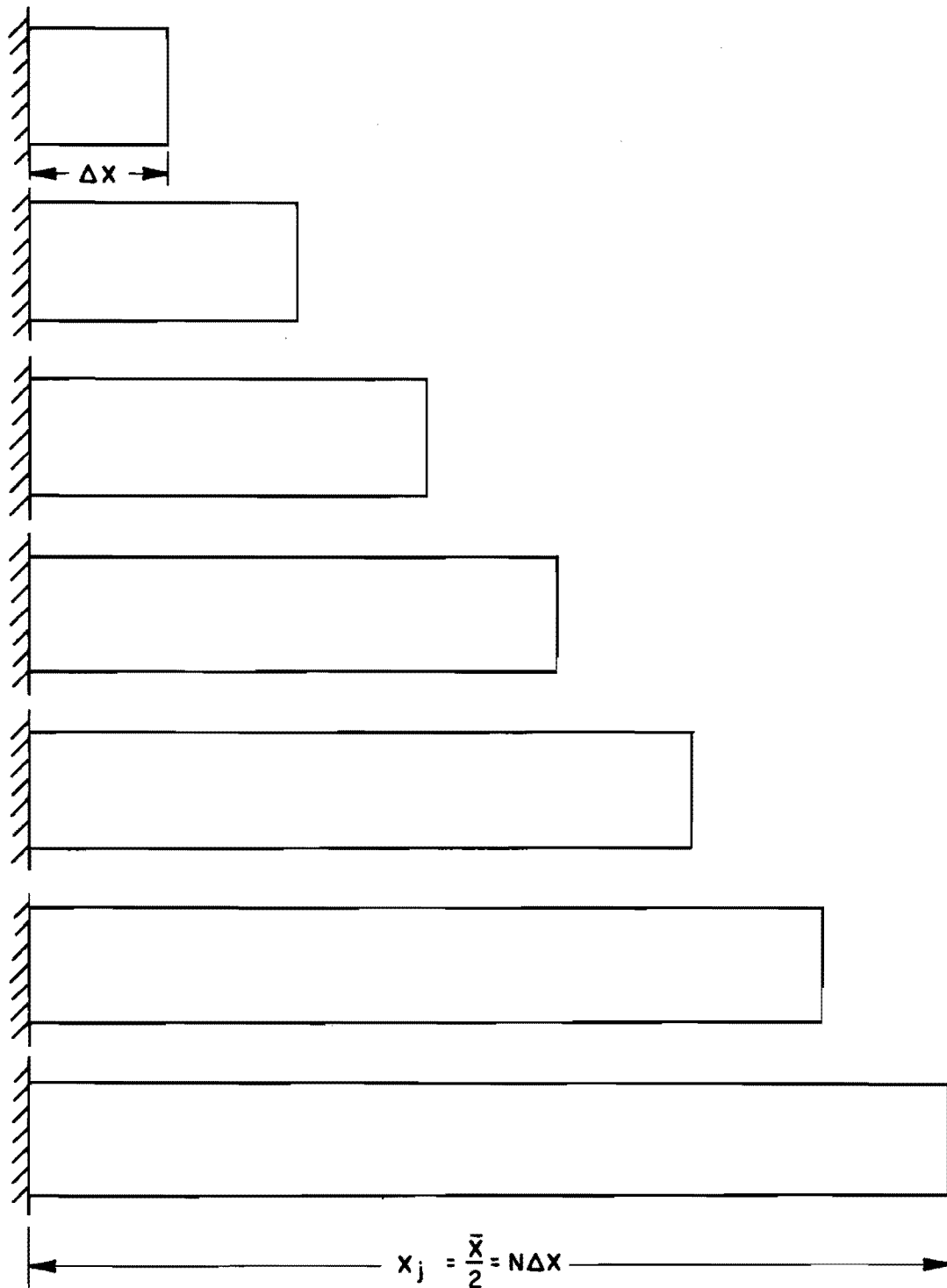


Fig. 4.12. Change in length of the model, increasing  $\Delta X$  by  $\Delta X$  each time.

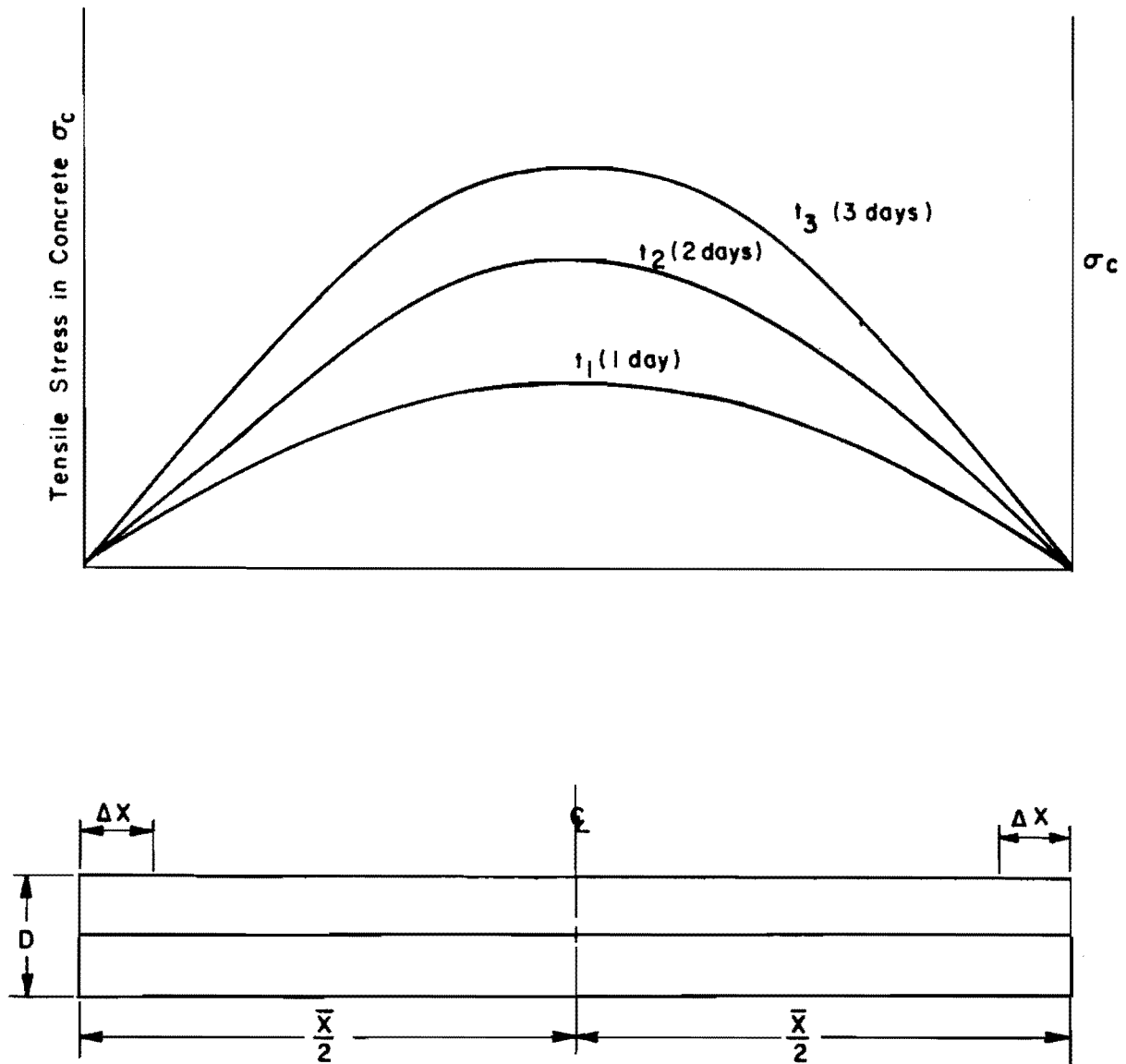
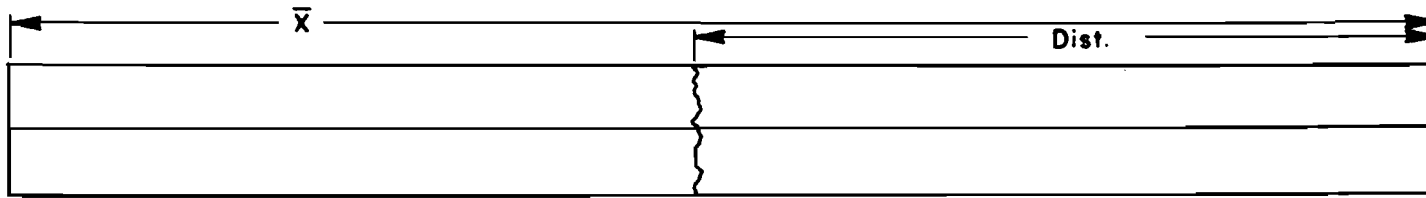
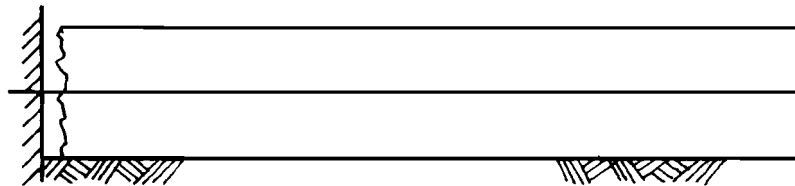


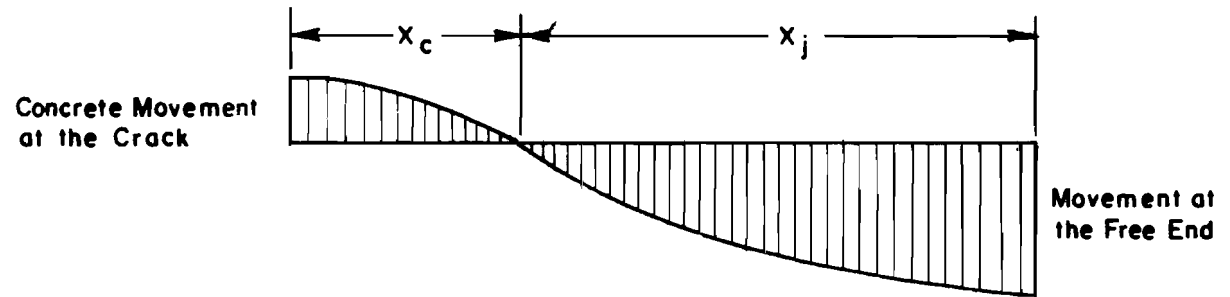
Fig 4.13.: Concrete stresses with time.



(a) View of slab after first crack.



(b) Right portion of slab after first crack



(c) Contraction movement of slab portion

Fig. 4.14. Slab portion after first crack.

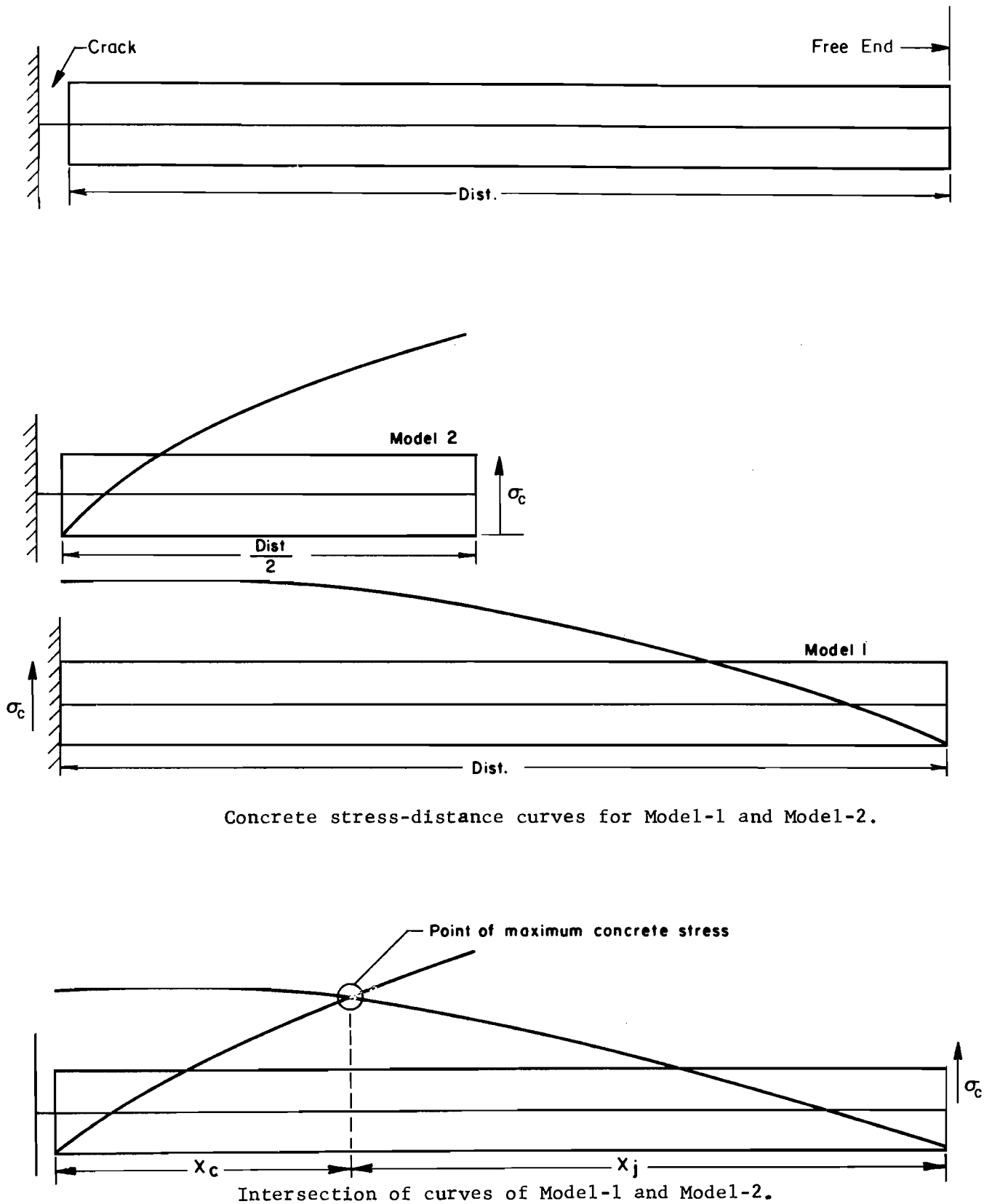


Fig. 4.15. Method used to search for the second crack.

intersection point of the two curves. Now, the maximum concrete stress can be found that will correspond to the point of zero movement (Fig 4.15b). A crack can be detected by comparing the maximum stress with the concrete tensile strength at the same time.

#### SOLUTION OF THE BASIC EQUATIONS

As the primary purpose of this work is to search for cracks in jointed reinforced concrete pavement slabs, knowing that a crack is going to occur if the concrete tensile stress is greater than the concrete tensile strength, the equations will be solved first for the stress in the concrete as follows:

##### Model-1

Solving Eq 4.8 for  $\sigma_s$  yields

$$\sigma_s = n\sigma_c - nE_c[Z + \Delta T(\alpha_c - \alpha_s)]$$

and substituting  $\sigma_s$  into Eq 4.3 yields

$$\sigma_c + pn\sigma_c - pnE_c[Z + \Delta T(\alpha_c - \alpha_s)] - \frac{\int_0^x F_i dx}{D} = 0$$

Solving for  $\sigma_c$

$$\sigma_c(1 + pn) = pnE_c[Z + \Delta T(\alpha_c - \alpha_s)] + \frac{\int_0^x F_i dx}{D}$$

$$\sigma_c = \frac{pnE_c[Z + \Delta T(\alpha_c - \alpha_s)] + \frac{\int_0^x F_i dx}{D}}{[1 + pn]} \quad (4.27)$$

Using the friction-movement relationship provided by the user, and using Eq 4.16, the friction force can be obtained, thus Eq 4.27 can be solved. An iterative procedure must be used, because the concrete movement is a direct function of the concrete stress, and the concrete stress is dependent on the

friction force. Using the findings from Research Project NCHRP 1-15, this problem was solved by using a binary search technique by which the concrete stress is computed by assuming  $F_1 = 0$  and then the concrete movement  $Y_1$  is computed using that concrete stress. Movement  $Y_1$  is then used to determine  $F_3$  from the experimental curve, with  $F_2$  being the upper boundary. The basic equation is again solved for concrete stress using  $F_2$  and computing the concrete movement  $Y_2$ , which will correspond to  $F_3$ , the lower boundary, from the experimental curve. Now,  $F_4$  will be the arithmetical average of  $F_3$  and  $F_2$ . To determine the relative location of  $F_4$  with respect to the closure point,  $Y_4$  is computed and compared with the experimental  $Y_{4e}$  that corresponds to  $F_4$ . If  $Y_4$  is greater than  $Y_{4e}$ , then  $F_4$  to find  $F_5$ , and if  $Y_{4e}$  is greater than  $Y_4$ , then  $F_4$  is above the closure point, and then  $F_5$  will be the average of  $F_3$  and  $F_4$ , and continue to relative closure (Fig 4.16).

Then the values of  $\sigma_c$  and  $F_1$  corresponding to the friction-movement closure point are used to compute the stress in the steel by using the following equation:

$$\sigma_s = \frac{\int_0^x F_1 dx}{pD} - \frac{\sigma_c}{p} \quad (4.28)$$

With the above information, Model-1 is solved for any point along the slab.

The method of attack to search for a crack consists of the following steps:

- (1) Divide the total slab length into  $N$  number of increments to have an increment length equal to  $\Delta X = \bar{x}/N$ ,
- (2) for a given time, solve Model-1 for a distance equal to  $\Delta X$ , the increment length
- (3) increment the Model-1 length into another  $\Delta X$  and solve for  $\sigma_c$  and  $\sigma_s$ ,
- (4) continue incrementing  $\Delta X$  by one  $\Delta X$  and compute  $\sigma_c$  and  $\sigma_s$  until  $\Delta X$  is equal to half the total slab length,
- (5) having the stress in the concrete for each  $\Delta X$ , an equation relating  $\sigma_c = f(\text{distance})$  is computed,

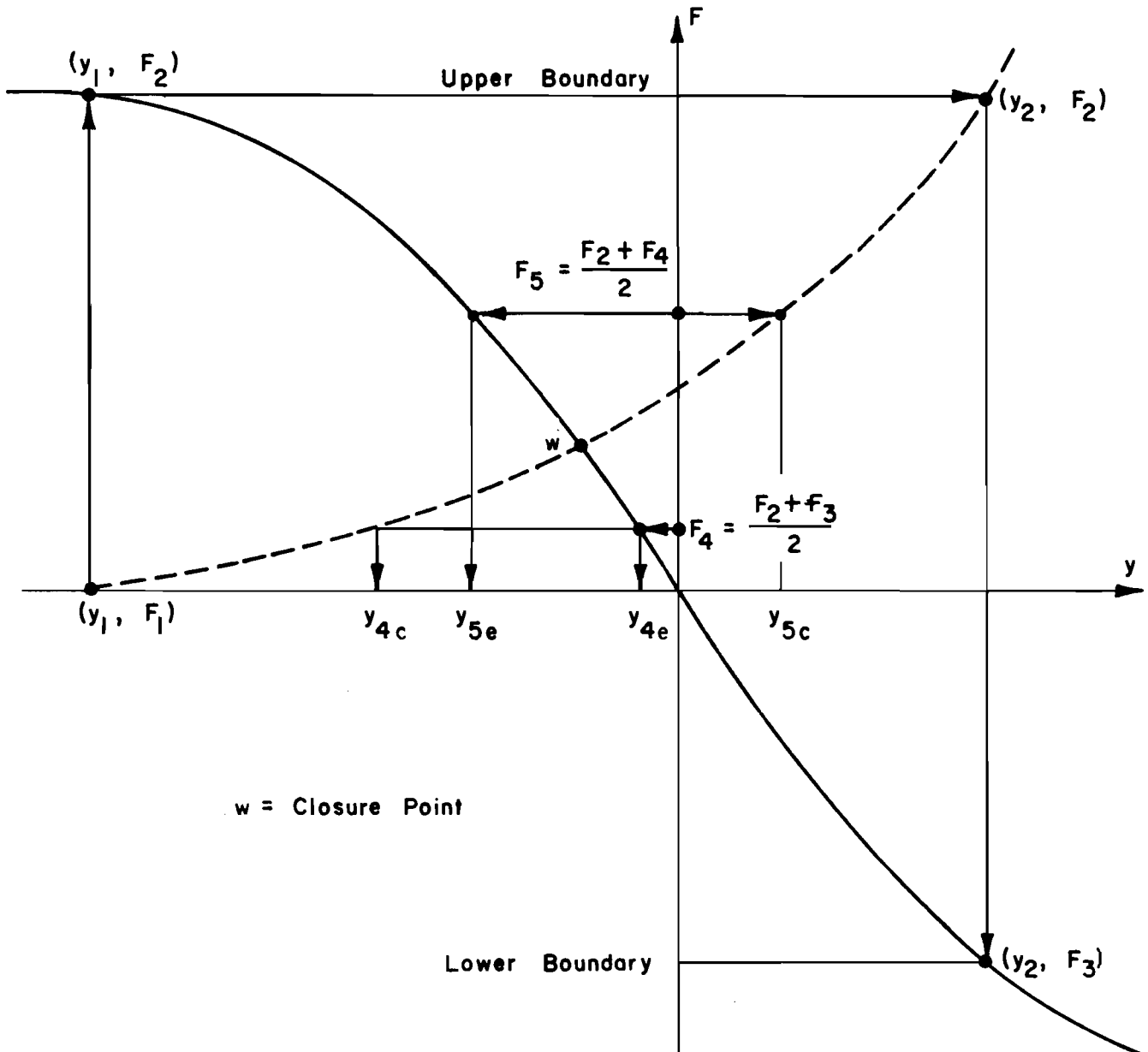


Fig. 4.16. Binary search technique as applied to frictional resistance-movement curve.



- (6) substitute the value of  $\sigma_c$  in the above equation by the concrete strength  $f'_t$  at that time and find the corresponding distance,  $\text{Dist} = f(f'_t)$ , and
- (7) if that distance is greater than half the slab length, no crack will occur at that time, but if the distance is less than or equal to half the slab length, then a crack occurs at that same distance.

This process is shown in the flow diagram in Fig 4.17.

#### Model-2

For information on how Model-2 is solved, the reader is referred to Ref 7 where a complete discussion and explanation of the solution of the Model-2 is given.

If the first crack occurs, say at time  $t_7$ , then, Model-1 is used as described above for time  $t_8$ , and Model-2 is also solved for that time  $t_8$ .

The solution of Model-2 is achieved by using the solution given by Research Project NCHRP 1-15 (Ref 7) to the CRCP model and is the same as for Model-2. The only variation is that the concrete stress is computed for each  $\Delta X$  until  $\Delta X$  is equal to half the length between the crack and the free end. At the end of each time, there will be a stress-distance relationship, and when intersected with the one for Model-1 at the same time (age), it will indicate the magnitude and location of the maximum concrete stress for that age, so that when compared with the concrete strength at the same age it will indicate if a second crack will occur.

#### Combining Models 1 and 2

- (1) Model-1 is solved for concrete stress at any point along the slab for one-half the slab length using the first five steps of the procedure described previously.
- (2) Model-2 is solved for concrete stress at any point along the slab for one-fourth the slab length using procedure described in NCHRP 1-15 Report.
- (3) The stress distance relationships from Models-1 and 2 are equated to find the point of zero movement. The distance point of intersection from the Model-1 relationship is designated as distance from joint to point of zero movement ( $x_j$ ). The equivalent movement from Model-2 is designated as distance from crack to point of zero movement ( $x_c$ ).
- (4) The concrete stress at the point of equal movement is checked against the concrete strength at that time. If the concrete strength is exceeded, a crack is assumed at that point. Its width is computed and the procedure halts.

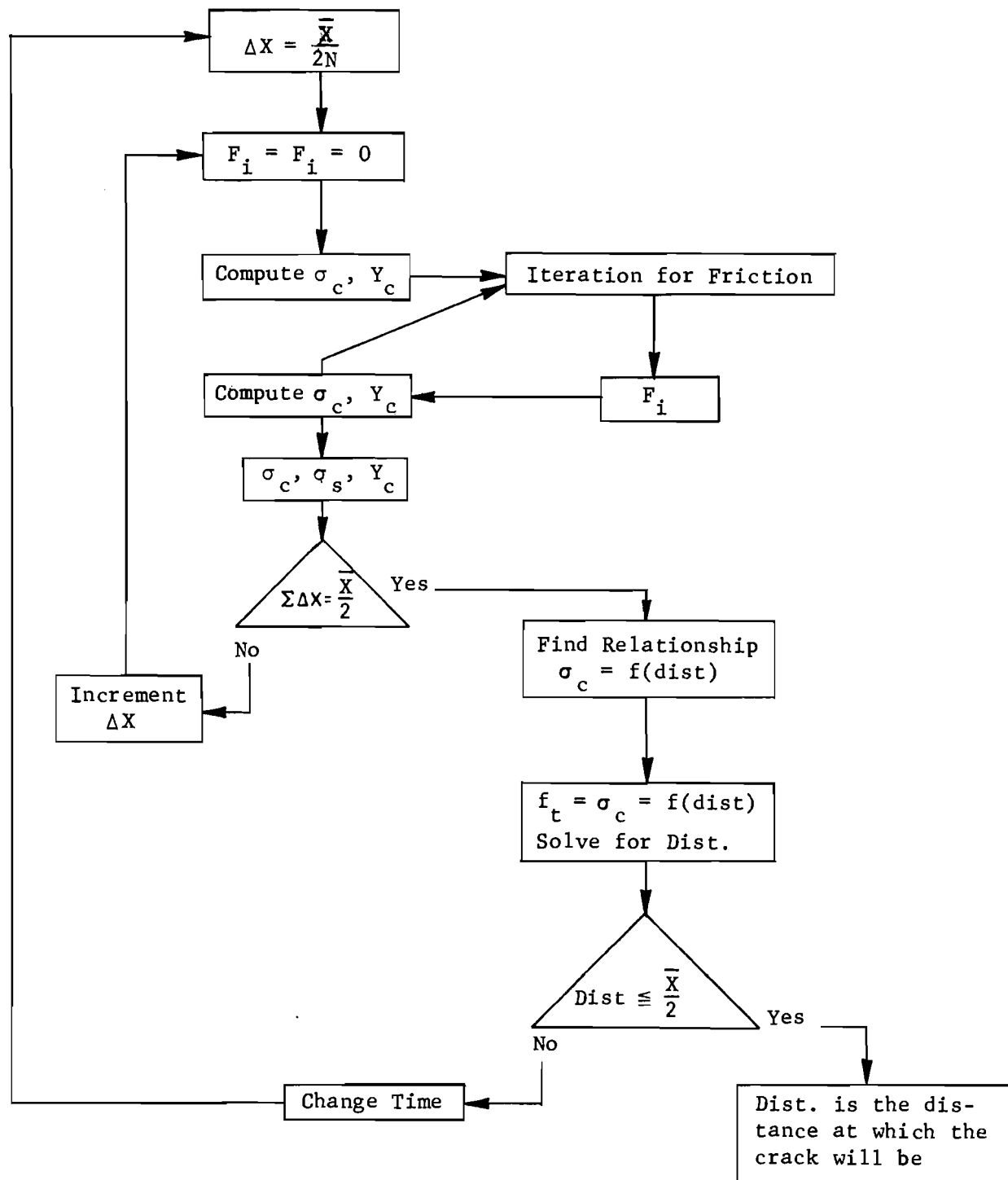


Fig. 4.17. Flow diagram for the search for the first crack.

- (5) If the concrete strength is not exceeded at the point of zero movement, the time is incremented. This procedure continues until the concrete strength is exceeded, the concrete reaches full strength, or the steel stress at the first crack rises above a specified maximum.

If the concrete reaches full strength, the procedure is performed one more time using the minimum temperature expected for the area to test the stresses in the steel and concrete.

If the specified maximum (.75 X yield stress) is exceeded by the steel stress at the crack, a message is printed and the problem terminates.

## STEEL DESIGN

The methods currently used to determine the percent reinforcement for the JRCP originated from several questionable assumptions and limitations, and the present pavements are having different performance problems. To explain and avoid the performance differences, a better qualitative evaluation is required.

The subgrade drag theory is the most recent approach in the solution of the reinforcing steel design, and because of that, the present work will use this method as a first approximation to find the steel percentage that will hold the cracks tightly together.

The process will be as follows:

- (1) Compute steel percentage by subgrade drag theory (Ref 19).

$$p = \frac{LF}{2f_s} \times 100 \quad (4.29)$$

where

p = percentage steel required (cross-sectional area) (percent),  
 L = distance between free edges (feet),  
 $f_s$  = allowable working stress in steel (0.75 of yield strength),  
 F = friction factor of subbase.

- (2) With the computed steel percentage, analyze the slab and search for a crack, and if a crack does not occur, remove the steel.
- (3) If a crack occurs, check crack width, and if it is less than the maximum crack width, the steel design is checked for stress versus strength.

- (4) If a crack occurs, check crack width, and if it is greater than the maximum crack width, the steel percentage is increased in half of its previous value and is checked again.
- (5) If a crack occurs, and the crack width is within the range, the stress in the steel at the crack is checked for its allowable working strength, and if the stress is greater than its allowable working strength, the steel percentage is increased by half of its value and checked again.

Table 4.1 suggest values of the friction factor  $F$  for use in equation 4.28. When the steel percentage using the maximum crack width criteria is obtained, the steel spacing is computed by means of the following relationship (Ref 19):

$$Y = \frac{A_B}{D \times p} \times 100 \quad (4.30)$$

where

- $p$  = percentage steel required,  
 $D$  = slab thickness (inches),  
 $A_B$  = cross-sectional area of steel bar or wire (square inches),  
 and  
 $Y$  = center to center spacing (inches).

The procedure used can be explained as follows. Each time the slab length is divided into  $NT$  increments; for each increment the concrete and steel stresses are solved. At the completion of the study of half the slab length, a stress equation as a function of slab length is obtained by using the stress values of each increment. So, for each day there will be a stress-distance relationship. The concept used to search for a crack was to equate the stress equation with the value of the strength of the concrete at the same time; then, by solving the equation for distance, the distance at which the concrete stress is equal to the concrete strength is obtained, and if that distance is less than or equal to half of the slab length, a crack will occur at that distance; but, if the distance obtained is greater than half of the slab length, there will be no crack (Fig 4.18).

TABLE 4.1. RECOMMENDED FRICTION FACTORS (Ref 19).

Subbase Type	Subbase Friction Factor
Surface Treatment	2.2
Lime Stabilization	1.8
Asphalt Stabilization	1.8
Cement Stabilization	1.8
River Gravel	1.5
Crushed Stone	1.5
Sandstone	1.2
Natural Subgrade	0.9

Note: These are approximate values derived from experimental observations. The friction factors in this table cannot be equated with the slab-base friction relationship required to properly characterize the restraint forces.

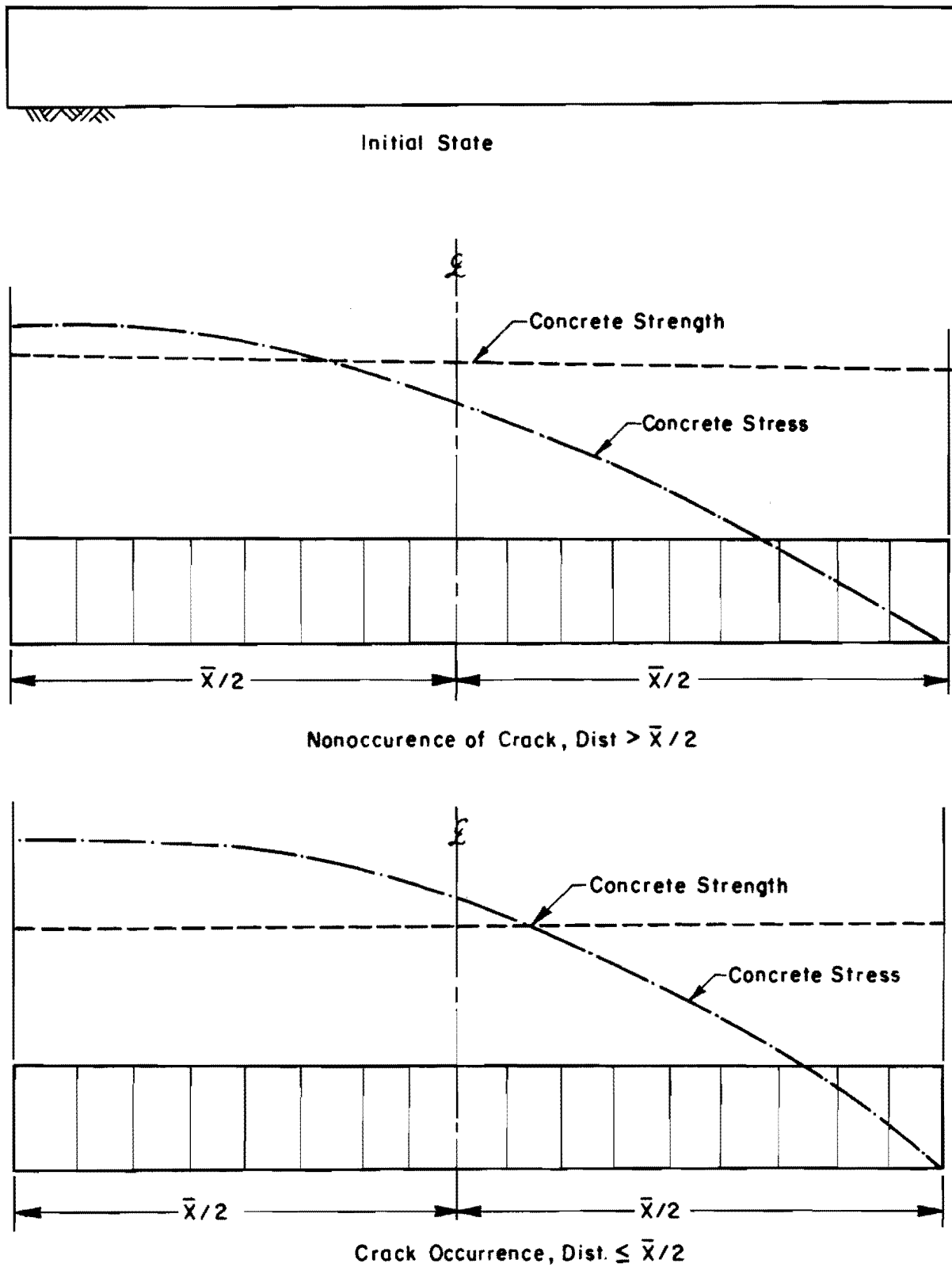


Fig. 4.18. Search for first crack.

If a crack occurs, the corresponding crack width is calculated and compared with a maximum allowable value of crack width\*; when the crack width is within this range, the program will change to the Model-2 at the time when the first crack occurred; the stress in the steel is obtained and is checked against the steel strength, and if the stress is greater or equal to the allowable working strength, the steel percentage is increased and the analysis starts again. If the stress in the steel is less than its allowable working stress, the program continues searching for the second crack occurrence for the following day. The solution for the second crack occurrence is achieved by solving Model-1 and Model-2, as previously discussed. At the intersection of these two curves, the value of the maximum concrete stress is obtained; then, by comparing this value with the concrete strength for that same time, it is possible to see if a second crack is going to appear, following the computation of the width of that second crack. If a second crack occurs, the crack width of this second crack is checked by using the above procedure, and then the program is terminated. If either the first or second crack width is not within the range, the steel percentage will be changed, incrementing its value in  $P/2$  if the crack width is greater than its maximum value, or reducing its value in  $P/2$  if the crack width is less than 0.012 inch. Then the new design is analyzed again starting from day one. The program is finished when both the first and second crack widths are within the specified range and the stress in the steel at the crack is less than its allowable working strength.

#### NON-REINFORCEMENT DESIGN

For possibly obtaining a less expensive pavement slab, a design procedure for non-reinforced slabs was included in the program. This design procedure will give a slab length which will provide a non-cracked slab, which is the desired state of a non-reinforced pavement slab. In order to get a realistic design, the slab is analyzed at each time until the twenty-eighth day, and if for each of the days the concrete stress curve intersects the

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\*Maximum value for crack width is provided by the user.

concrete strength curve between 0.50 and 0.75 of the slab length, this slab length will be taken as optimum and is the one that will be given as the result (Fig 4.19).



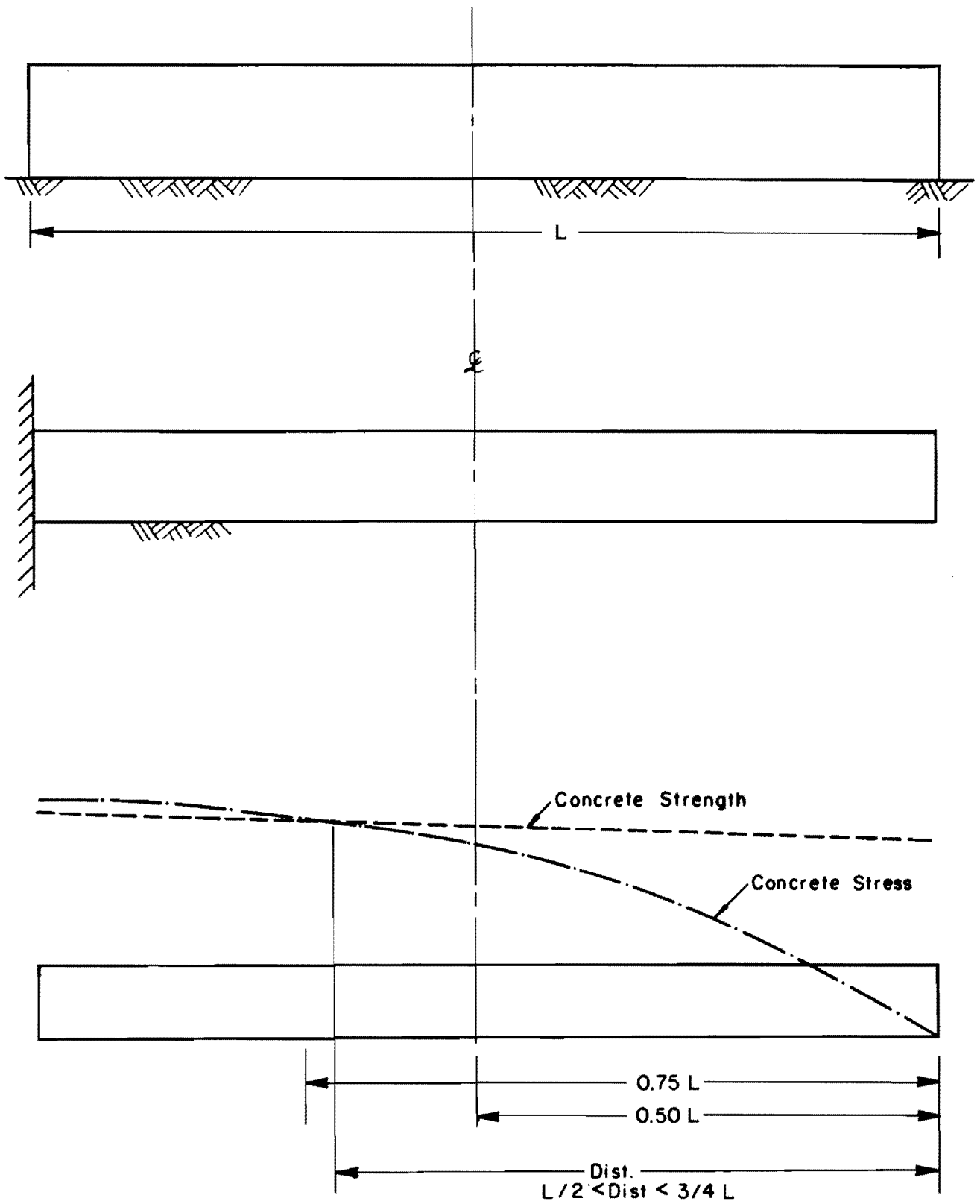


Fig 4.19. Criteria used for the non-reinforced slab design.

## CHAPTER 5. REINFORCEMENT ANALYSIS PACKAGE

The computer program developed is designated by JRCP-1. The number 1 signifies that this is the first version of the chronological sequence intended for future development.

The program is written in FORTRAN IV computer language for the Control Data Corporation 6600 digital computer, which has a 60-bit word length. The compile time for the basic program is less than 12 seconds. If desired, normal operating decks may be compiled on binary cards, thus reducing compiler time in the computer significantly. The exact storage requirement for the program presently is 60,000 locations. The program can be adapted for use with the IBM 360/370 computer by very slight modifications.

The time required to run problems varies, of course, with the complexity of the system, e.g., the nature of the friction-movement relationship, the variation of the concrete strength with time, increment length, and the number of iterations required to obtain the desired accuracy and the option being used. To give a general idea of the operating time, for a relative closure tolerance of one percent and an average problem similar to the sample problems in the report, the computer time is in the range of 70 to 80 seconds for the steel design option. By considering the number of nonlinearities involved in the encountered problem it can be concluded that the algorithms developed in the various nonlinearities provide extremely fast convergence. The cost of seconds of computer time is negligible compared to the benefits derived from the fact that this computer program provides a new and better way of solving highly complex JRCP problems.

### THE INPUT DATA

The format used for inputting data into the program is arranged as conveniently as possible. The problem input deck starts with two cover cards which identify the program and the particular run being made. The information on these cards is alphanumeric and is used to denote projects, coding dates, a

description of the problems being run, etc. After these two alphanumeric cards the following cards come in this order:

- (1) Problem number card with alphanumeric description of the problem.
- (2) Slab Dimensions - one card. This card includes the length of the slab, the width of the slab, the friction factor used to compute the initial percent of steel, the maximum allowable crack width, the steel design option and the non-reinforcement option. The format and units used are fully described in the user's guide (Appendix 1). It is important to point out that even if the non-reinforcement option is used a slab length must be provided.
- (3) Steel Properties - one card. Information on this card includes the type of longitudinal reinforcement, bar diameter, yield stress, modulus of elasticity, thermal coefficient, and spacing of transverse wires in the case of deformed wire fabric. The format used to input the required information is shown in the Guide for Data Input in Appendix 1.
- (4) Concrete Properties - two or more cards. The first card contains the slab thickness, thermal coefficient, final or total drying shrinkage, unit weight, and 28-day compressive strength. On the second card is Age-Tensile Strength relationship; if unavailable, the data will be generated internally using the recommendations suggested by the United States Bureau of Reclamation.
- (5) Slab-Base Friction Relationship. The number of cards is variable depending on the number of points defining the F-y relationship. It is worth noting that according to the sign convention adopted in this study, the input movements should be negative and the friction forces should be positive. The program assumes a symmetric curve with respect to the origin.
- (6) Temperature Data. This part of the input data deals with the analysis period directly after concrete placement where the average curing temperature and the minimum daily temperature for the desired number of days are input. The number of cards required is variable and depends on the number of data points.
- (7) Maximum Iterations and Closure Tolerance - one card. The primary objective for the maximum number of iterations is to prevent excessive computation. Most pavement problems should close to a reasonable tolerance within ten iterations; an allowed maximum of 20 is usually adequate. Relative closure tolerance is used for all the nonlinearities involved in the problem. It should be expressed in percent. If the tolerance is unreasonably small, closure may be difficult to achieve. A value of one percent is recommended.

## PROGRAM OPTIONS

In order to obtain the major benefit of the program capability, the user is provided with three options. The options are as follows:

- (1) Analysis of a given design. The user by using this option can analyze a given design (slab dimensions, steel percentage) for crack occurrence and crack width. Also, when there is a crack, the program will tell the user if the crack width is bigger than the maximum allowable value of crack width for aggregate interlock provided by the user.
- (2) Steel reinforcement design. For a given slab geometry, the program designs the steel for two different kinds of reinforcement, deformed bars and deformed wire mesh. The steel design is based on the concept of having a crack width between 0.023 inch and 0.012 inch.
- (3) Design of the required length for a non-reinforced slab. Given a tentative slab length, the program will analyze the slab for a non-crack occurrence state, and will give the optimum length for that case, based on the concept of optimization for non-reinforced slab length previously discussed.

## ADDITIONAL RESEARCH NEEDED

A basic theoretical procedure which analyzes the effects of drying, shrinkage, and drop in temperature in a concrete pavement slab (either reinforced or non-reinforced) has been developed; it is a useful tool to the man trying to simulate nature with theory. The design procedures developed tend to be more realistic, but in order to make a real, or better said, more real, representation of the "real world conditions," the following points need to be studied:

- (1) frictional resistance of the sub-base layer,
- (2) the inclusion of the restriction to movement of the slab provided by the dowels,
- (3) variability of concrete properties,
- (4) prediction of the concrete temperature from air temperature,
- (5) effects of the slab movement in the transverse direction,
- (6) addition of load and warping stresses, and
- (7) field studies to test the reliability of the program.

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## CHAPTER 6. STUDY OF VARIABLES

The purpose of this chapter is to describe how temperature drop and subgrade friction influence the concrete tensile stress pattern. These two factors are considered to be the most important for the scope of this study. Also, a graph of steel stress at the crack versus time is presented to emphasize the importance of having the steel stresses checked versus its allowable working stress each day.

### STUDY OF SUB-BASE FRICTION

It is important to note as shown in Figs 6.1 through 6.4, the concrete-tensile stress versus the number of increments in which the slab length was divided is plotted for high and low sub-base frictions. The increment numbers start at the joint and increase toward the center. The large difference in the stress levels demonstrates the great effect the sub-base friction has on the crack occurrence in the concrete slab. For this graph, all elements except daily drop in temperature remain constant for each sub-base friction.

### STUDY OF DROP IN TEMPERATURE

For this study, all the factors, but temperature drop, were held constant for each day. The concrete-tensile stresses versus the number of increments were plotted for drops in temperature of ten and thirty degrees Fahrenheit as shown in Figs 6.5 and 6.7. From these figures it can be seen that for large drops in temperature, the concrete-tensile stresses may exceed the concrete-tensile strength, leading to a crack formation.

### STUDY OF THE STRESSES OF THE STEEL AT THE CRACK

After a crack occurred in the concrete slab, the reinforcing steel was subjected to the tensile stresses that the concrete had before the crack, and, at the crack, the only element capable of resisting the tensile stresses was the reinforcing steel. As the slab attempted to contract with time, the tensile

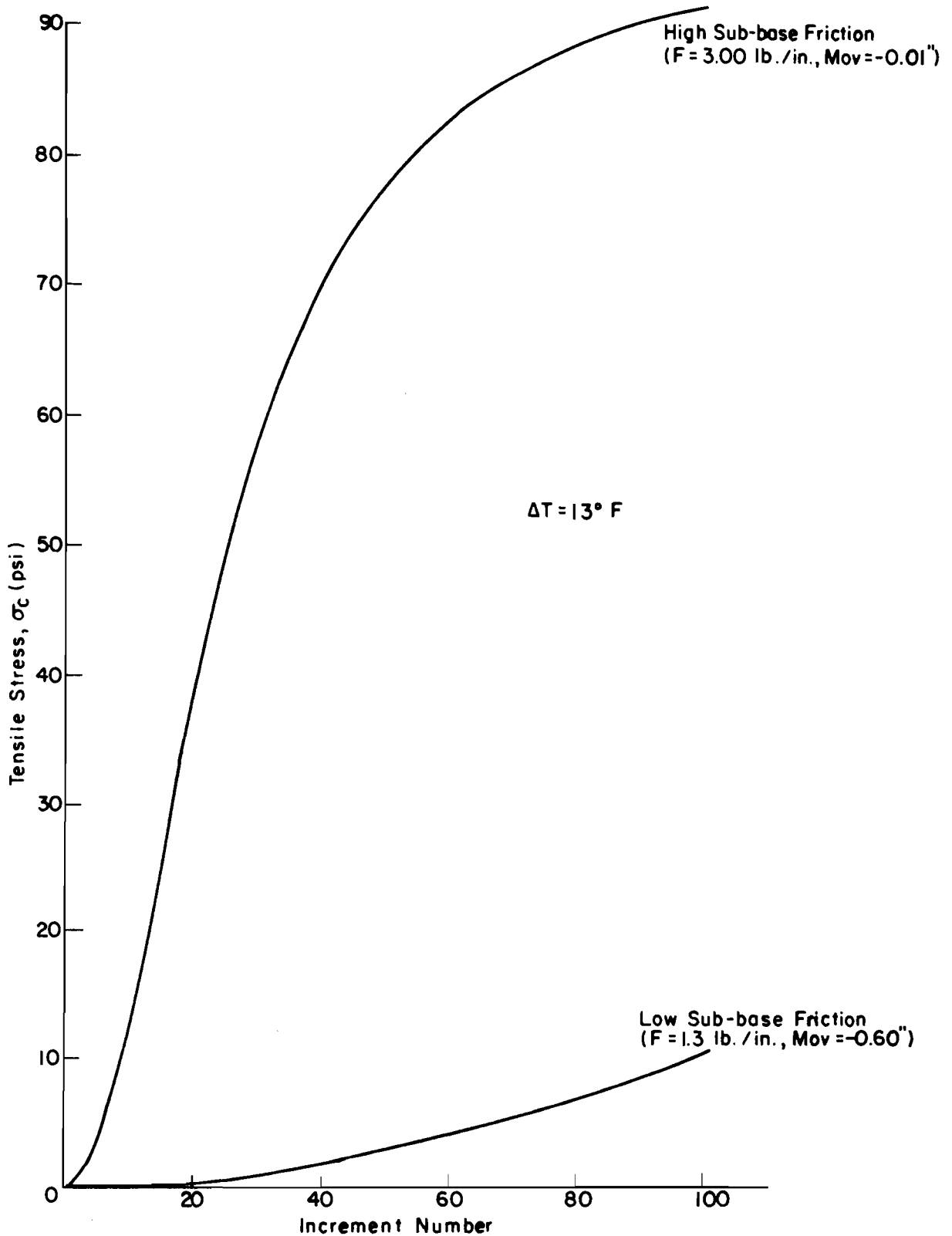


Fig 6.1. Concrete tensile stress for two sub-base frictions at the first day after concrete placement.

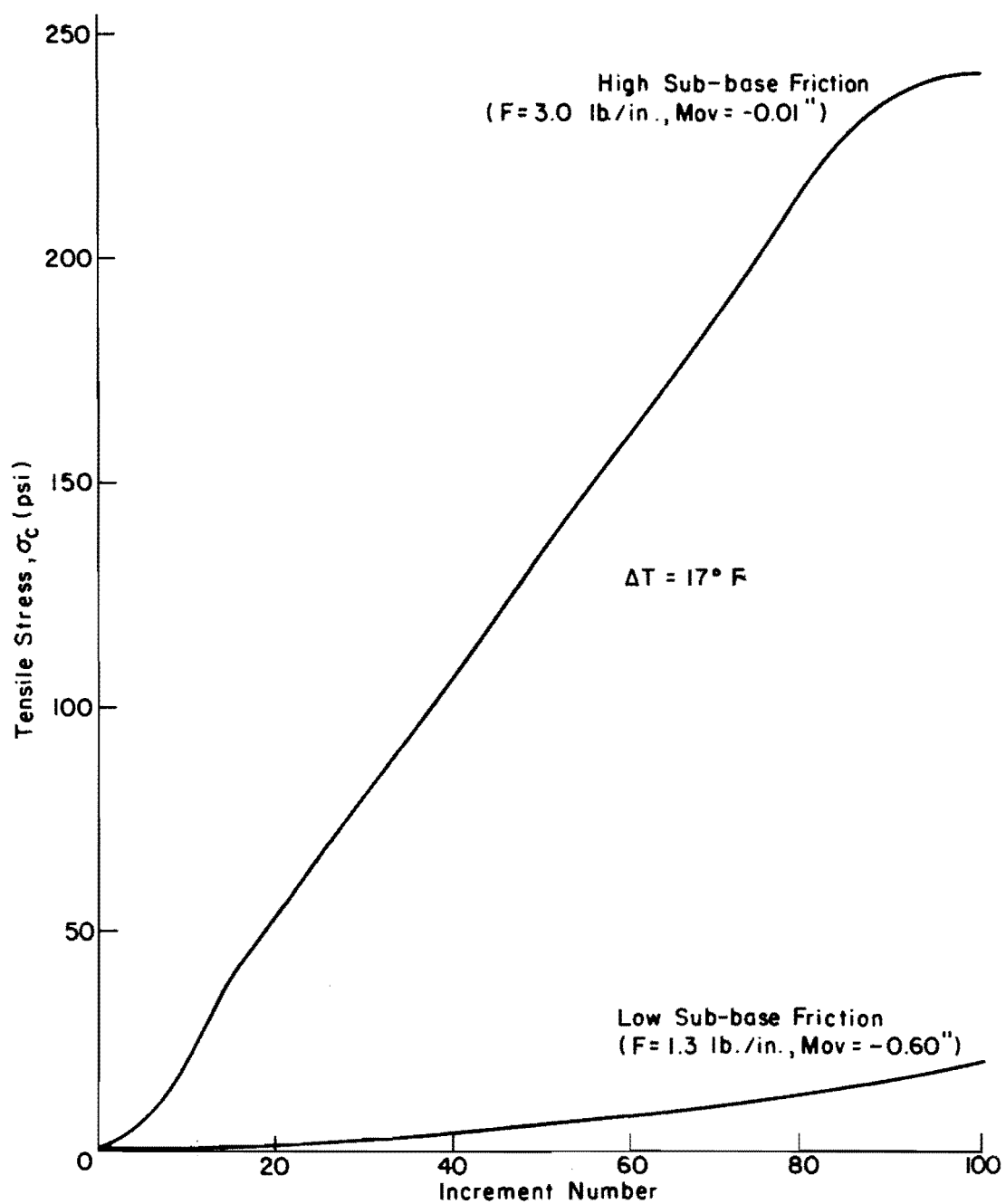


Fig. 6.2. Concrete tensile stresses for two sub-base frictions at seven days after placement.



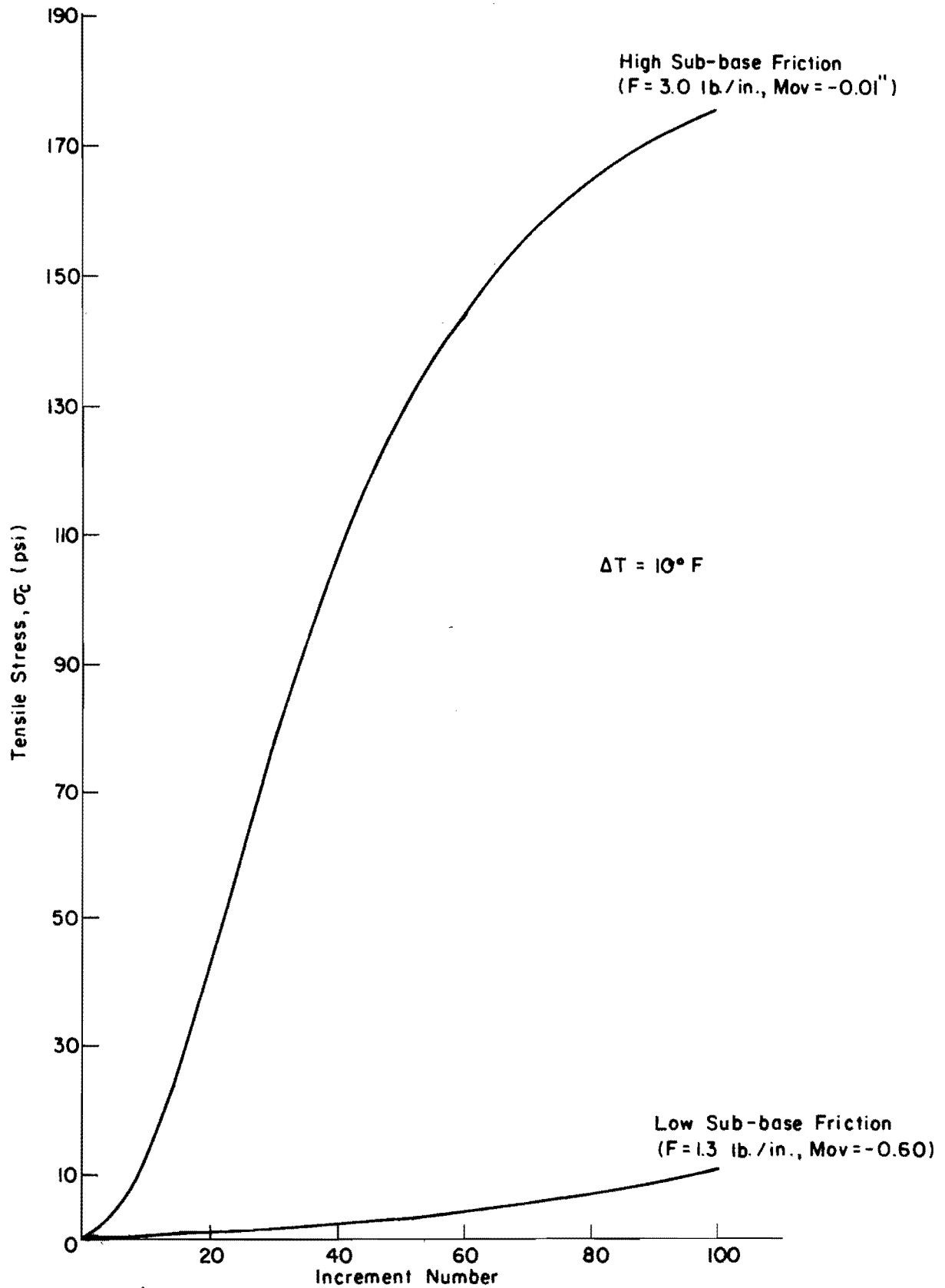


Fig. 6.3. Concrete tensile stresses for two sub-base frictions at 14 days concrete placement.

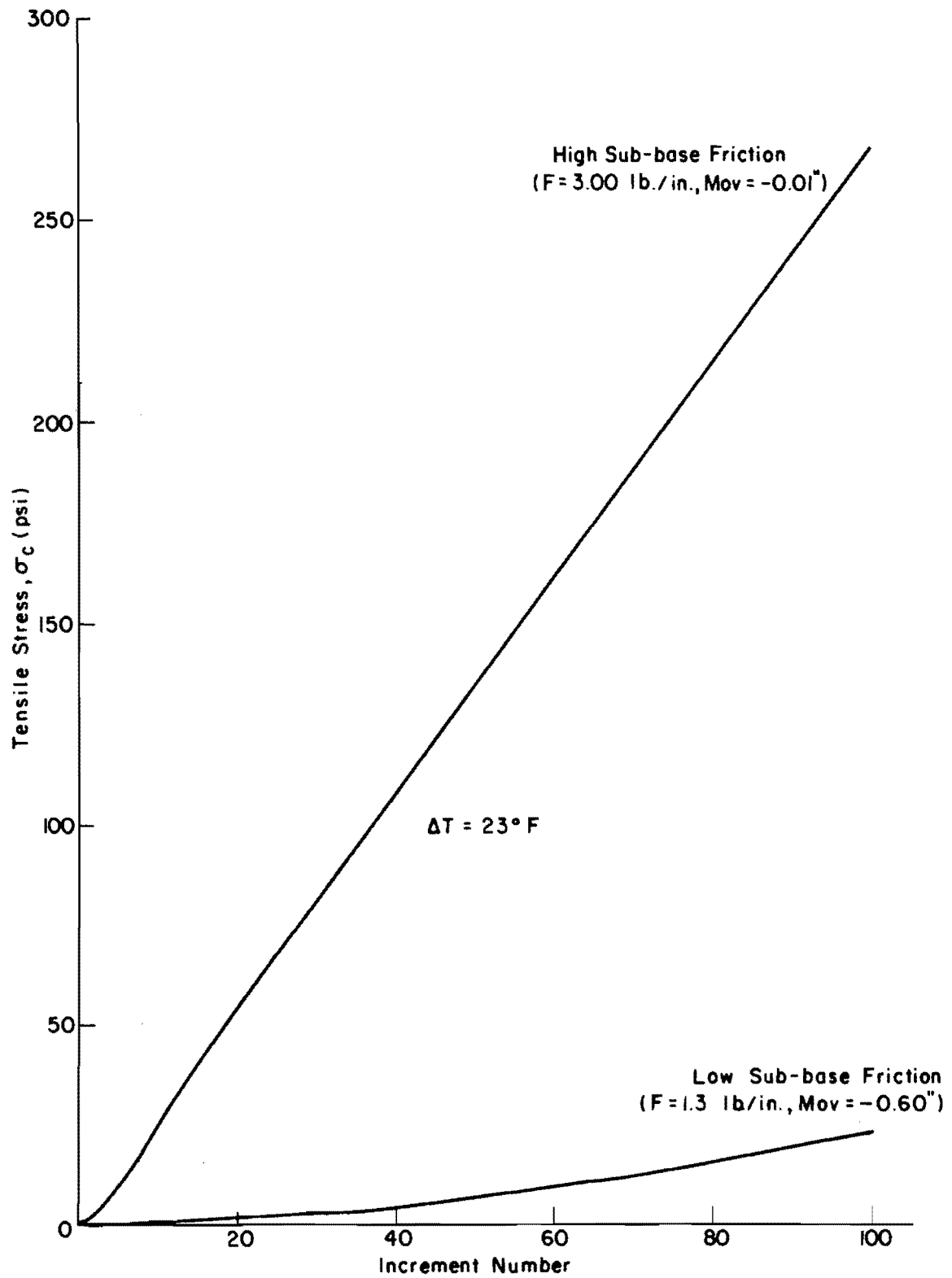


Fig. 6.4. Concrete tensile stress for two sub-base frictions after 28 days of concrete placement.

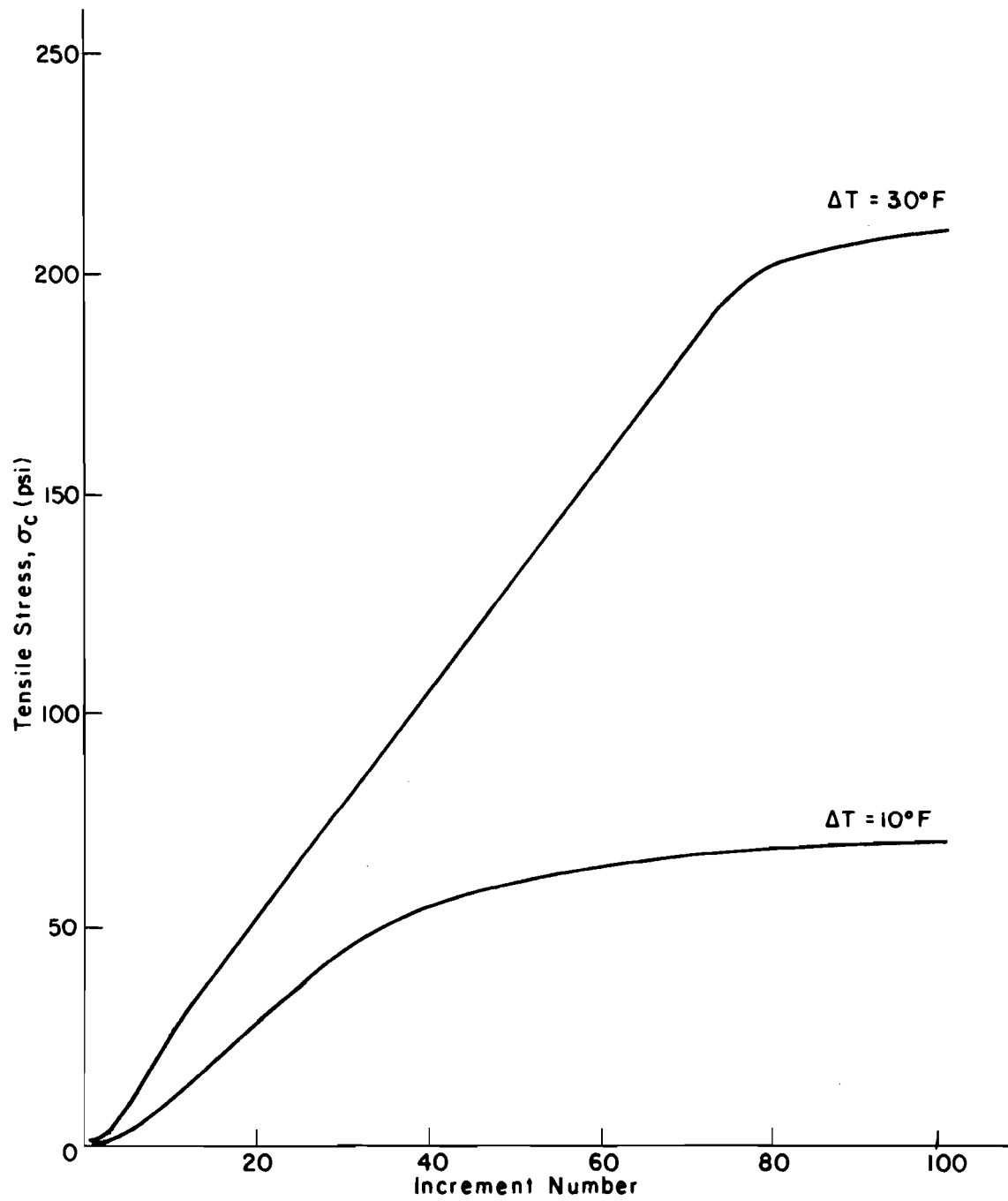


Fig. 6.5. Concrete tensile stresses for two drops in temperature at the first day after concrete placement.

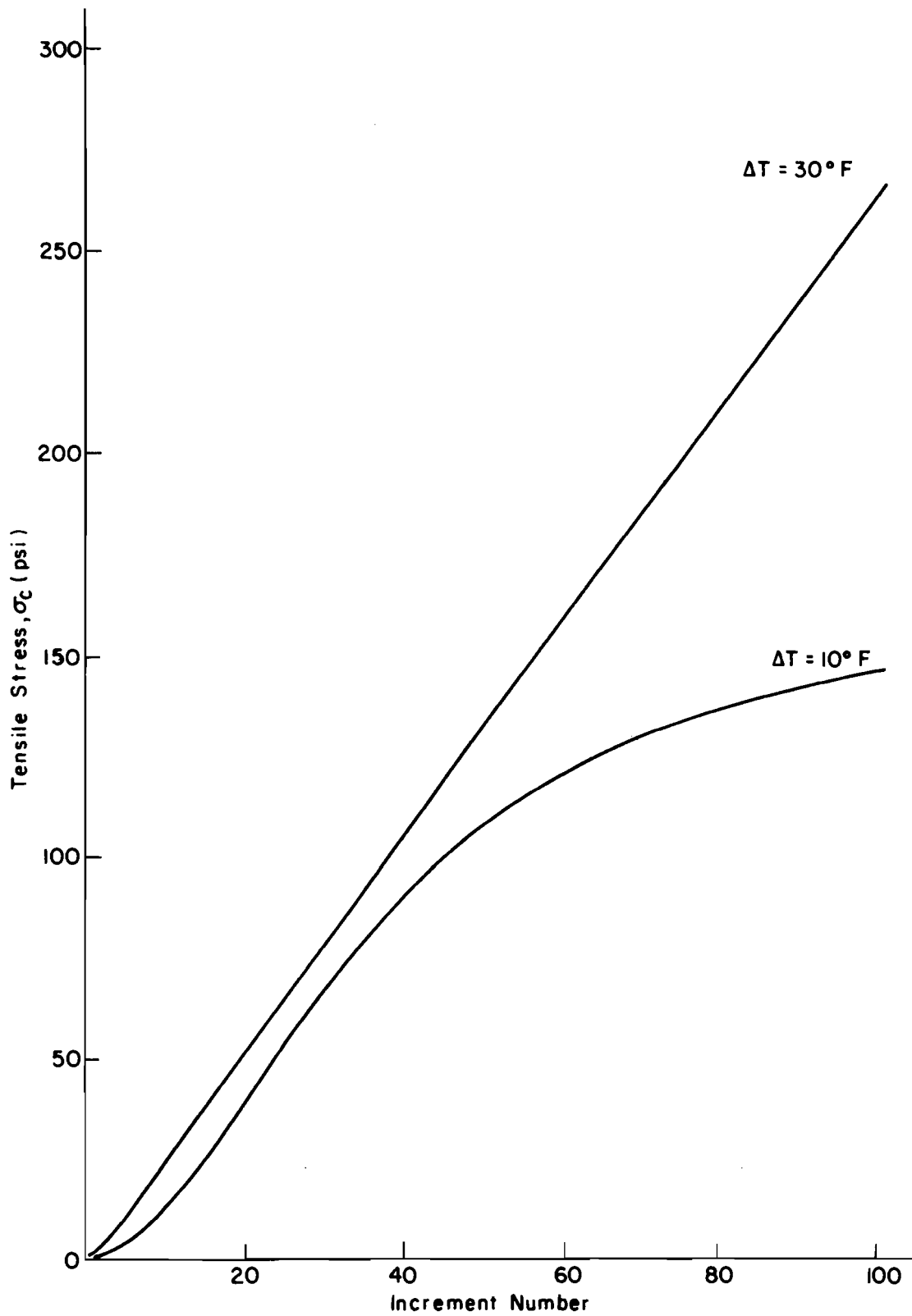


Fig. 6.6. Concrete tensile stresses for two drops in temperature after seven days of concrete placement.

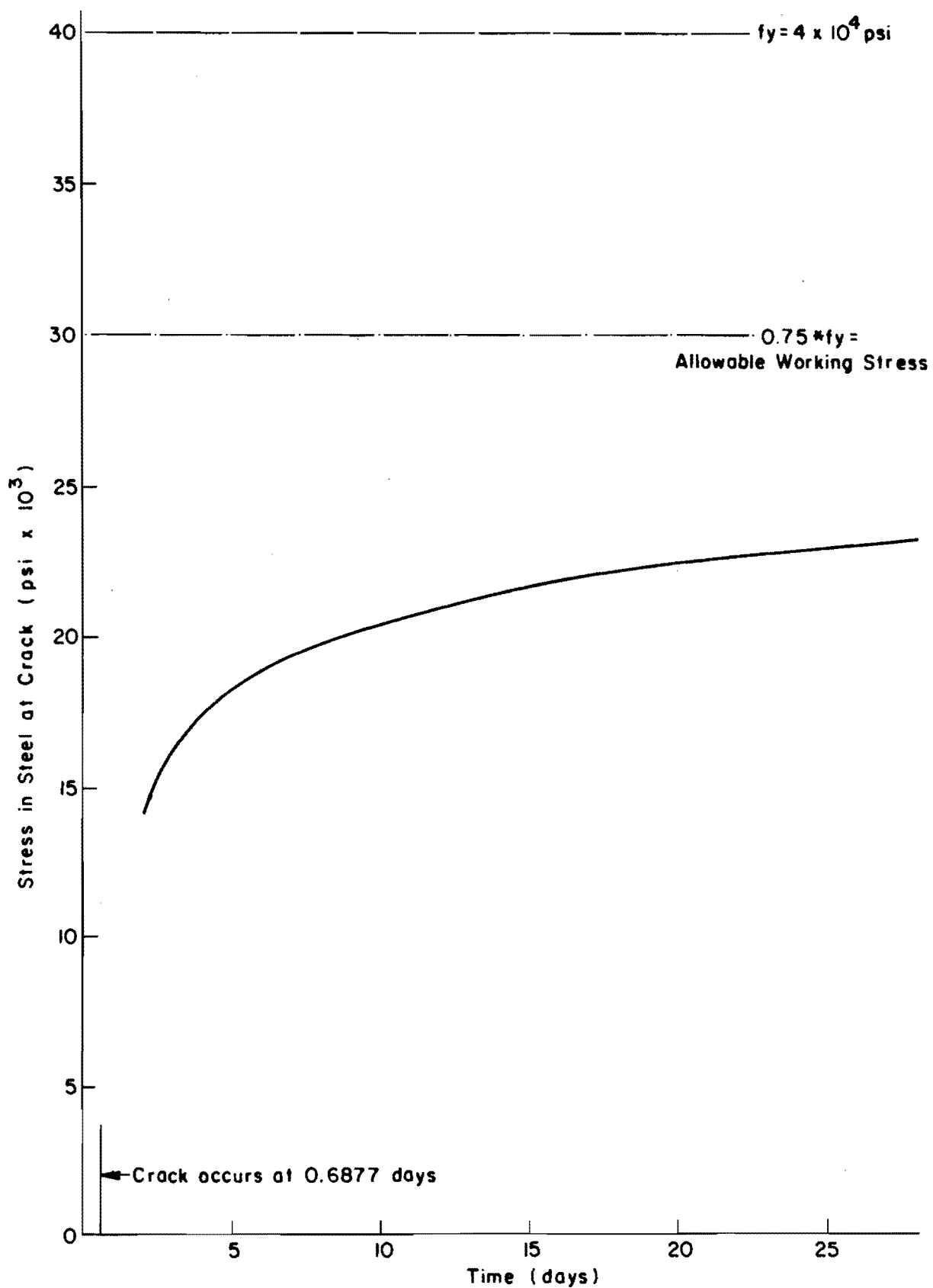


Fig. 6.7. Tensile stress of the steel at the crack.

pattern of the tensile stress of the steel at the crack emphasized the importance of checking the tensile stress of the steel at the crack against its allowable working stress on a daily basis.

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## CHAPTER 7. CONCLUSIONS, RECOMMENDATIONS AND IMPLEMENTATION GUIDELINES

Cracking in a jointed reinforced concrete pavement is a prime factor leading to the reduction in pavement performance depending on the crack width. Water percolation, spalling, loss of load carrying capacity, and pumping are some of the distress manifestations which vary with cracking in the slab. This study focused on developing a design analysis package that would consider the effects of drying shrinkage and drop in temperature to minimize the effect of transverse cracks in jointed concrete pavement.

### CONCLUSIONS

Based on this study the following conclusions are warranted:

- (1) The subgrade drag theory currently used for the design of longitudinal reinforcement in a jointed reinforced concrete pavement is inadequate for the range of subbase conditions currently in use throughout the U. S. The present method makes unrealistic static assumptions in computing the required steel, whereas the joint width and crack width function vary immediately with changes in temperature and shrinkage. Although the primary mode of failure for these pavements is at transverse cracks and joints there is no control in the present methods for crack width or joint width.
- (2) A computer program (JRCP-1) developed in this study more realistically models the complex interaction and movement characteristics between the concrete slab and the subbase layer at their interface. The crack width, longitudinal steel stress, and the concrete stress are predicted as a function of temperature and concrete drying shrinkage. The maximum crack width information developed in connection with NCHRP 1-15, "Design of Continuously Reinforced Concrete Pavements for Highways," may be used with this program to design jointed concrete pavements.
- (3) The program internally examines the occurrence of three cracks in the slab. The first crack (model 1) is assumed to occur near the center of the slab; the second crack and third crack (model 2) are assumed to occur between the middle of the slab and the free joints.
- (4) The program has the capability of providing the user with the following three options:



- (a) analysis of a given design, crack occurrence and crack width,
  - (b) steel reinforcement designed for a given slab geometry in environmental conditions, and
  - (c) the design of the required maximum length for a non-reinforced slab to eliminate the possibility of intermediate transverse cracking.
- (5) A limited sensitivity analysis in the program shows that subbase slab friction characteristics and the temperature conditions during curing have a large influence on the occurrence of crack, resulting crack width and the resulting steel stress at the crack.

### RECOMMENDATIONS

Based on the study the following recommendations are made:

- (1) The wheel load stresses should be superimposed on those predicted by temperature changes and drying shrinkage. There is evidence from studies of continuously reinforced concrete pavement that wheel load stresses may influence the formation of transverse cracks, especially during the early life of the pavement.
- (2) A range in temperature conditions should be selected on the basis of geographic areas in Texas to study variations in performance with respect to temperature and shrinkage cracking. These geographic areas should be the same as recommended for implementation of computer program CRCP-1.
- (3) The stochastic variations of cracking should be approximated in the program by using standard deviations of the more important inputs and a random generator to simulate this variation.

### IMPLEMENTATION GUIDELINES

The following steps are recommended for implementation of the computer program after recommendation (1) has been completed:

- (1) A user's manual should be developed for the SDHPT using the operating manual for program JRCP-1 in Appendix 1 as a guideline.
- (2) The temperature data developed in connection with the recommendation (2) should be used to develop a range of solutions, crack width, crack spacing, and steel stress for different material properties.
- (3) The information from the preceding number should be used to develop a design manual for CRCP that would reflect more variables than taken in to account at the present time; thus the performance level of CRCP would be improved.

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APPENDIX 1

OPERATING MANUAL FOR PROGRAM JRCP-1

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## APPENDIX 1. OPERATING MANUAL FOR PROGRAM JRCP-1

### Program Operation

The general procedures followed in the program are described in the attached flow chart. A problem number card at the beginning of each problem controls the start of the solution. Unless an error occurs because of unacceptable data, the program will work any number of problems in sequence, finally stopping when a blank problem number card is encountered.

The data deck starts with two cover cards used to identify the program and the particular run being made. The problems to be solved together in one run are stacked behind the cover cards in sequence as illustrated in Fig. A1.1. Each problem consists of one problem number card with alphanumeric description of the problem. This is followed by slab properties, steel properties, concrete properties, slab-base friction relationship, temperature data, minimum allowable number of iterations, and tolerance for relative closure.

### Guide for Data Input

The following pages provide a guide for Data Input. It should be expected that revisions of these forms and instructions will be developed in the future and may supersede the present versions.

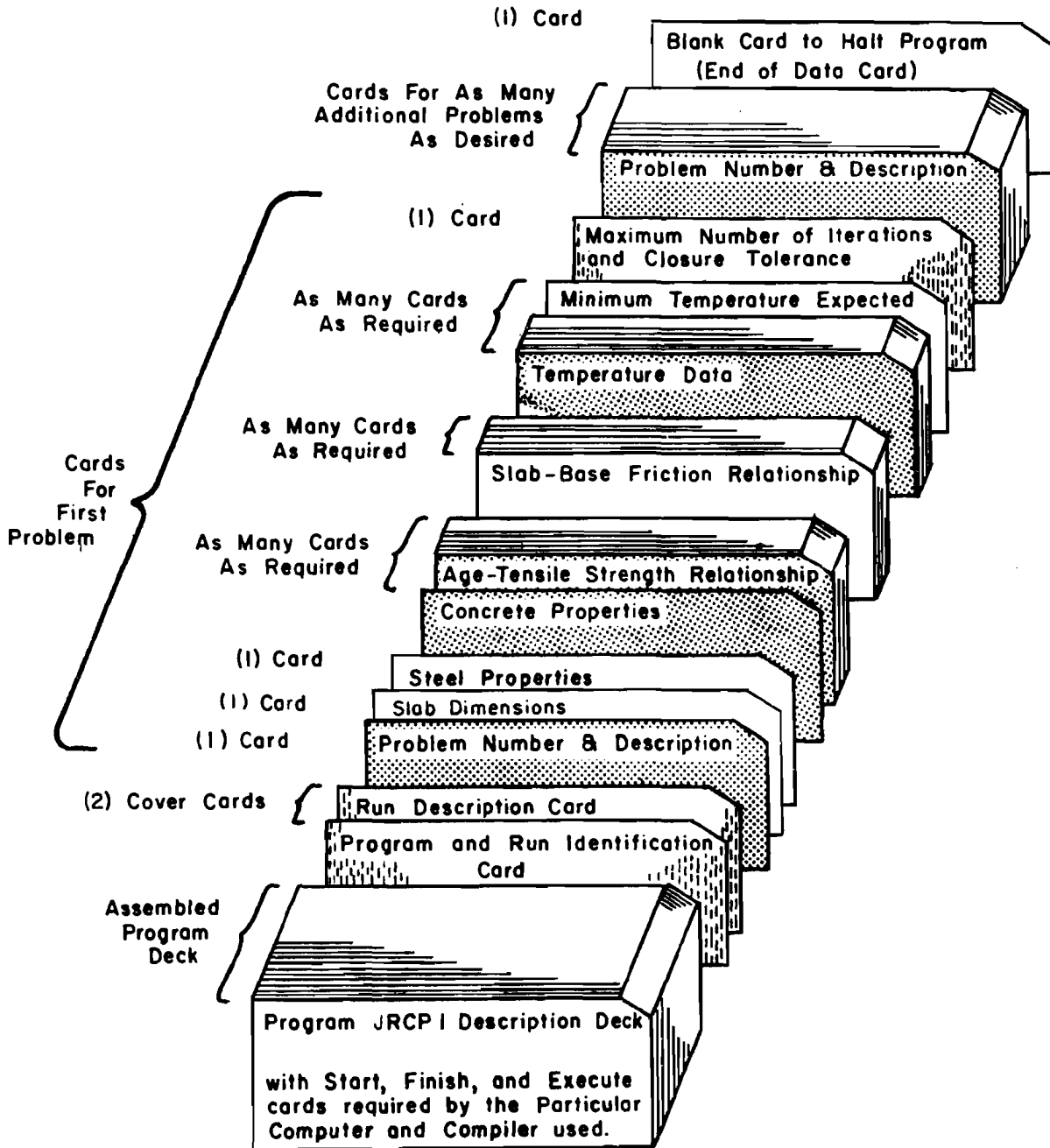


Fig A1.1. Assembly order for JRCP-1 program deck with data, ready to run.

JRCP-1 - GUIDE FOR DATA INPUT -- Card forms

IDENTIFICATION OF PROGRAM AND RUN (2 alphanumeric cards per run)

Description of Run
--------------------

80

--

80

IDENTIFICATION OF PROBLEM (one card each problem; program stops if PROB NUM is left blank)

PROB NUM

A5	Description of Problem (alphanumeric)
----	---------------------------------------

80

SLAB DIMENSIONS

FT SLAB LENGTH	FT SLAB WIDTH	NUMBER OF INCREMENTS	lb/in/in FRICTION FACTOR	IN CRWM	ISTDS	NRF
F8.4	F8.4	I5	F8.4	F8.4	I2	I2
8	16	21	29	37	41	43

slab length must be understood as transverse joint spacing

STEEL PROPERTIES (one card each problem)

ITYPER	PERCENT REINFORCEMENT	in <sup>2</sup> BAR DIAMETER	(PSI) YIELD STRESS	(PSI) ELASTIC MODULUS	/ <sup>o</sup> F THERMAL COEFFICIENT	TRANSVERSE WIRE SPACING*
I5	E10.3	E10.3	E10.3	E10.3	E10.3	E10.3
1 5	11 21	31	41	51	61	70

ISTDS = 0 for analysis of a given design (user needs to input percentage of steel and slab dimension)

ISTDS = 1 if steel design option is used (the program will design percentage of steel required for a given slab geometry)

\* Required only in the case of deformed wire fabric analysis.



JRCP-1 - GUIDE FOR DATA INPUT -- Card forms

- NRF = 0 if ISTD5 = 0 or 1
- NRF = 1 if non-reinforcement option is used (design optimum slab length for non-reinforced slab)
- ITYPER = 1 for deformed bar
- ITYPER = 2 for deformed wire fabric
- CRWM = Maximum allowable crack width, inches.

CONCRETE PROPERTIES

CONSTANTS (one card each problem)

(IN) SLAB THICKNESS	/°F THERMAL COEFFICIENT	(IN/IN) DRYING SHRINKAGE STRAIN	UNIT WEIGHT OF CONCRETE (pcf)	(PSI) 28-DAY COMPRESSIVE STRENGTH*	TENS. STRENGTH FLEX. STRENGTH
E10.3	E10.3	E10.3	E10.3	E10.3	E10.3
11	21	31	41	51	61
					70

AGE-TENSILE STRENGTH RELATIONSHIP

NTS	AGE(1)	TS(1)	AGE(2)	TS(2)									AGE(7)	TS(7)
	F5.1	F5.1	F5.1	F5.1									F5.1	F5.1
1	11	16	21	26	31	36	41	46	51	56	61	66	71	76
5														80

AGE(8)	TS(8)									AGE(NTS)	TS(NTS)		
F5.1	F5.1									F5.1	F5.1		
11	16	21	26	31	36	41	46	51	56	61	66	71	76
													80

- NTS = 0, if no tensile strength data is available (data are generated).
- NTS = Total number of points on Age-Strength relationship (maximum is 20).
- AGE(I) = Age of concrete in days.
- TS(I) = Tensile strength in psi.

\* Not required if Age-Tensile Strength data are provided.

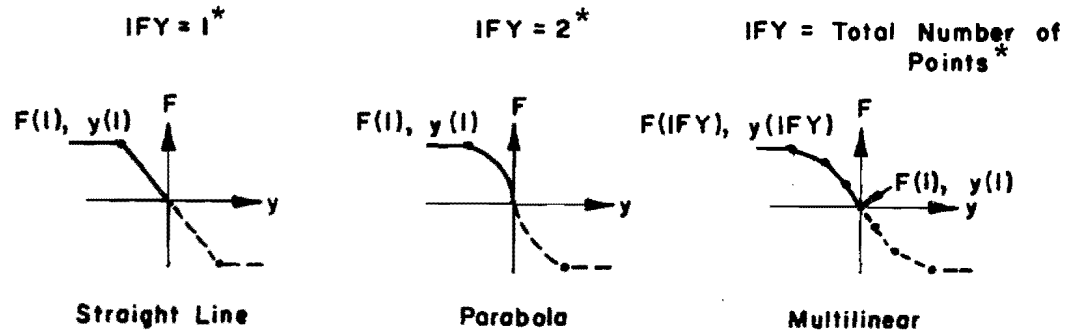
JRCP -1 - GUIDE FOR DATA INPUT -- Card forms

SLAB-BASE FRICTION RELATIONSHIP (F-y curve)

IFY		F(1)	y(1)	F(2)	y(2)								F(7)	y(7)		
15		F5.2	F5.2	F5.2	F5.2								F5.2	F5.2		
1	5	11	16	21	26	31	36	41	46	51	56	61	66	71	76	80

F(8)	y(8)							F(IFY)	y(IFY)					
F5.2	F5.2							F5.2	F5.2					
11	16	21	26	31	36	41	46	51	56	61	66	71	76	80



F(I) = Force per unit length (lb/in/in).

y(I) = Movement (inches).

\*Only the solid portion of the curve need to be defined; the dotted portion is generated by symmetry with respect to the origin.

JRCP-1 - GUIDE FOR DATA INPUT -- Card forms

TEMPERATURE DATA

Average curing temperature and minimum daily temperature (<sup>o</sup>F)

CURT	NTEMP	TD(1)	TD(2)	TD(3)											TD(13)	TD(14)
F5.1	I5	F5.1	F5.1	F5.1											F5.1	F5.1
1	6	11	16	21	26	31	36	41	46	51	56	61	66	71	76	80

TD(15)	TD(16)							TD(NTEMP)						
F5.1	F5.1							F5.1						
11	16	21	26	31	36	41	46	51	56	61	66	71	76	80

- CURT = Average curing temperature of concrete, °F.
- NTEMP = Number of days.
- TD(I) = Minimum daily temperature, °F.

Minimum temperature expected after concrete gains full strength

DTMAX

F5.1
11 15

ITERATIONS AND TOLERANCE CONTROL

MAXITE	TOL
I5	F5.1
1	6 10

- MAXITE = Maximum number of iterations.
- TOL = Relative closure tolerance in percent.

STOP PROGRAM	One blank card to end program
--------------	-------------------------------

## GENERAL PROGRAM NOTES

The data cards must be stacked in the proper order for the program to run.

All integer format and E format numbers must be right justified.

The problem number may be alphanumeric.

Sign convention adopted is as follows:

- (1) tension is positive,
- (2) friction forces in the positive x-direction are positive,
- (3) movements in the positive x-direction are positive, and
- (4) temperature drop at a given time is defined as the difference between the temperature at which concrete has set and the temperature at that time.

## SLAB DIMENSIONS

Only one card is required per problem. This card includes the commands to use the steel design option or the non-reinforcement option. The slab length must be always provided, even if the non-reinforcement option is used. The units are slab length, feet, slab width, feet, maximum allowable crack width, inches.

## STEEL PROPERTIES

Only one card is required per problem. Program JRCP-1 has the capability of analyzing the most commonly used types of longitudinal reinforcement, deformed bars and deformed wire fabric. The desirable type of reinforcement can be specified by ITYPER option. ITYPER = 1 is for deformed bars while ITYPER = 2 is for deformed wire fabric. The units to be used are pounds and inches. The unit of temperature used in the analysis should be degrees Fahrenheit in the thermal coefficient and temperature data.

## CONCRETE PROPERTIES

The input of concrete properties consists of two or more cards. The first card has slab thickness, thermal coefficient, final drying shrinkage, unit weight, and 28-day compressive strength. Units are pounds and inches except for unit weight of concrete, where pounds per cubic foot should be used. In case the thermal coefficient and/or final drying shrinkage of the concrete mix used are not available, Fig 3.3 contains recommended values obtained from the present state-of-the-art.

The second card contains the age-tensile strength relationship of the concrete. If these data are not provided, the recommendations given by the United States Bureau of Reclamation will be used to generate the age-tensile strength relationship. In this case, the 28-days compressive strength of concrete is required, and NTS should be zero.

## SLAB-BASE FRICTION RELATIONSHIP (F-y curve)

Various relationships can be input to define the F-y curve used in the computations. Regardless of the type of curve, symmetry is assumed with respect to the origin of the axes. This implies that only one portion of the curve is needed, while the remainder is generated by the program.

The three types of frictional resistance relationships are: straight line, parabola, and multilinear curves. The desired relationship is specified by the control IFY, where a value of one, two, or greater than two indicates that the F-y curve is a straight line, parabola, or multilinear relationship, respectively. In the case of a straight line or a parabola, only one point is required to define the curve. This point is where sliding occurs. If the multilinear curve is used, then the first point should be the origin  $F(1) = 0$  ,  $y(1) = 0$  , while the last point  $[F(IFY), y(IFY)]$  should be sliding. The force should be expressed in  $\text{lbs/in}^2$  and the movement in inches.

#### TEMPERATURE DATA

In the temperature data, the average curing temperature and the minimum daily temperature over a period of NTEMP days should be specified. NTEMP should be equal to the time when the tensile strength reaches its maximum value, as specified in the Age-Tensile Strength relationship. If no tensile strength data are available, then as discussed previously, strength values will be generated by the program, in which case NTEMP should be 28 days, and 28 minimum daily temperatures will be required.

One more piece of information is required for the analysis: minimum temperature expected after concrete gains full strength.

#### MAXIMUM NUMBER OF ITERATIONS AND CLOSURE TOLERANCE

The maximum number of iterations should be set to prevent excessive computation. Most jointed concrete pavement problems should close to a reasonable tolerance within 10 iterations; an allowed maximum of 20 is usually adequate.

The closure tolerance is Relative closure and should be expressed in percent. If it is unreasonably small, closure may be difficult to achieve. For many structural road problems, a value of one percent is satisfactory.

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APPENDIX 2

GLOSSARY OF NOTATION FOR COMPUTER PROGRAM JRCP-1



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APPENDIX 2. GLOSSARY OF NOTATION FOR COMPUTER PROGRAM JRCP-1

NOTATION FOR JRCP-1 PROGRAM

AAA	Counter for the number of iterations for friction closure
AGE	Age of concrete generated by program
AGEU	Age of concrete input by user
ALPHAC	Thermal coefficient of concrete
ALPHAS	Thermal coefficient of steel
ANTEMP	Last day on time temperature curve
BAD	Counter to indicate friction closure
BHIGH	Spacing of transverse wire in deformed wire fabric
BLOW	Half spacing of transverse wires
BONDL	Bond or development length
COMSTR	Compressive strength of concrete
CONSTR( )	Concrete stress
CRACKW1	Width of the first crack
CRACKW2	Width of the second crack
CURTEMP	Curing temperature
DELTAT	Drop in temperature at any time
DELTATM	Maximum drop in temperature
DIA	Diameter of individual bar
DELTAX	Increment length
DIF( )	Difference between two successive iterations
DT( )	Daily temperature
DIST	Distance between free edge and first crack
EC	Modulus of elasticity of concrete
ES	Modulus of elasticity of the steel
F( )	Friction force
FEXP( )	Flexural strength
FLESTRN	Flexural strength of concrete
FOUT	Value of flexural strength calculated by linear interpolation
FPC	Compressive strength
FU	Maximum friction force
FY	Yield stress of the steel
FRF	Friction factor for the AASHO steel equations
IFY	Number of points defining the friction movement curve
INDEX	Closure control
ITEB	Counter for the number of iterations on bond length
ITYPER	Option for the type of reinforcement
ISTDS	Option for steel design
L	Length of JRCP-1 Model
MA1	AAA-1
MAXITE	Maximum allowable number of iterations
N	Index for reading data

NPROB	Problem number (stops if blank)
NT	Total number of increments in the JRCP-1 Model
NTEMP	Number of daily temperatures
NTP1	NT+1
NRF	Option for non-reinforcement design
P	Percent longitudinal reinforcement
P2	Percent transverse reinforcement
PERCENT	Percentage of 28-day flexural strength
REFF	Upper bound on FU
SS( )	Steel strain
STRAIN( )	Concrete strain
STRESSS( )	Steel stress
STRNMUL	Transformation factor between tensile and flexural strength
STRSCO	Concrete stress at point of zero movement
STRSC1	Concrete stress for Model-1
STRSC2	Concrete stress for Model-2
THICK	Slab thickness
TIME	Time in days
TOL	Tolerance for closure criteria
UNWT	Unit weight of concrete
VDS	Volume to surface ratio
W	Slab width
XBAR	Slab length
Y( )	Concrete movement
YEXP( )	Movement on the frictional-resistance curve
YP( )	Movement for testing criteria
YPITE( )	Movement from the previous iteration
YST	Center to center spacing for transverse steel
Z	Drying shrinkage at any time
ZTOT	Total drying shrinkage

C-----Notation for subroutine DFBARF

A	Length of the fully bonded section in the JRCP Model
AA	Coefficient of the square term in quadratic equation
AAAAA	Summation of area under the steel stress diagram
ANA	Number of stations in the fully bonded section
A1,A2,A3	Magnitude of areas under the steel stress diagram
BB	Coefficient of the linear term in quadratic equation
BONDCON	Bond constant
BONDLC	Computed bond length
CC	Constant term in quadratic equation
C1,...,C9	Coefficients in the solution of equations
DELTA	Magnitude of delta for the solution of quadratic equation
DENO	Constant used for computing the slope of the steel curve
E	Distance in the fully bonded section of the JRCP Model
LOCMAX	Location of maximum concrete stress
NA	Number of increments
NAM1	NA - 1
NAP1	NA + 1
NAP2	NA + 2
RATIO	Ratio of modulus of elasticity of steel to that of concrete
ROOT1	Positive root of the quadratic equation
ROOT2	Negative root of the quadratic equation

SIGMASB	Stress in the steel between cracks
SIGMASC	Stress in the steel at the crack
SUM1	Summation for solution of equations
SUM2	Summation of the slopes to the steel stress distribution
U	Bond Stress

C-----Notation for subroutine DFBAR

AA	Coefficient of the square term in quadratic equation
B	Bond length
BB	Coefficient of the linear term in quadratic equation
CHECK	Check for solution of equations
CONGRES	Concrete stress between cracks
DD	Constant term in the quadratic equation
DEL	Value of delta in quadratic equation
R2, R6	Roots of quadratic equation
STRAREA	Area under the steel stress distribution
STRC	Stress in the concrete between cracks
STRSB	Stress in the steel between cracks
STRSC	Stress in the steel at the crack

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APPENDIX 3

COMPUTER PROGRAM

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APPENDIX 3. COMPUTER PROGRAM

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

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PROGRAM JRCP1(INPUT,OUTPUT)
DIMENSION AN1(40),AN2(18)
DIMENSION F(501),SUM(501),AGE(8),PERCENT(8)
COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW
COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
COMMON /BLOCK7/ Y(501),REFF(501),YP(501),H,CLOSER,YPITE(501)
COMMON /BLOCK8/ STX,STY,PSX,PSY,ITE
COMMON /BLOCK9/ NSTRN,VDS,AGEU(20),TENSION(20),STRNMUL
COMMON /BLOCK10/ DT(50),NTEMP,NTIFLAG,UPINC,DOWNINC
COMMON /BLOCK11/ Z,YP1,Y1(501),DELTA,DELTA,TEMP1,REFF1,YPITE1,W
COMMON /BLOCK12/ DT(50),NTEMP,NTIFLAG,UPINC,DOWNINC
COMMON /BLOCK13/ Z,YP1,Y1(501),DELTA,DELTA,TEMP1,REFF1,YPITE1,W
COMMON /BLOCK14/ BHIGH,BLOW,YSL,P2,YST
COMMON /BLOCK15/ STRSC1(501),STRSS1(501),INC,FRF,FY,L
DATA AGE/0.,1.,3.,5.,7.,14.,21.,28./
DATA PERCENT/0.,15.,38.,53.,63.,82.,94.,100./
REAL NEG1
INTEGER AAA
REAL L
      ITEST=5H
C
C PROGRAM AND PROBLEM IDENTIFICATION
C
5 READ 510, (AN1(N),N=1,40)
12 10 CONTINUE
12 READ 520, NPROB,(AN2(N),N=1,18)
22 IF (NPROB=ITEST) 20,450,20
24 20 CONTINUE
24 PRINT 530
30 PRINT 540, (AN1(N),N=1,40)
36 PRINT 550, NPROB,(AN2(N),N=1,18)
C
C READ SLAB DIMENSIONS AND DESIGN FLAGS
C
46 READ 555, XBAR,W,NT,FRF,CRWM,ISTOS,NRF
72 PRINT 580
76 PRINT 556
102 PRINT 580
106 PRINT 557,XBAR,W,NT,FRF,CRWM
124 XBAR=XBAR*12.
126 557 FORMAT(/,15X,22H SLAB LENGTH = ,E10.3,/,
1 15X,22H SLAB WIDTH = ,E10.3,/,
2 15X,22H NUMBER OF INCREMENTS= ,I5,/,
3 15X,22H FRICTION FACTOR = ,E10.3,/,
4 15X,22H MAX. CRACKWIDTH = ,E10.3,////)
126 IF (ISTOS.EQ.1)PRINT 551
133 IF (NRF.EQ.1)PRINT 553
141 IF (NRF.NE.1.AND.ISTOS.NE.1)PRINT 554
154 555 FORMAT(2F8.4,15,2F8.4,3I2)
154 556 FORMAT(10X,1H*,46X,1H*,/,
1 10X,48H* SLAB DIMENSIONS *,/,
2 10X,1H*,46X,1H*)
154 551 FORMAT(/,10X,* STEEL DESIGN OPTION *,/)

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JRCP1

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154 553 FORMAT(/,10X,* NON-REINFORCEMENT OPTION *,/)
154 554 FORMAT(/,10X,* SLAB ANALYSIS OPTION *,/)
C
C INPUT STEEL PROPERTIES
C
154 READ 560, ITPER,P,DIA,FY,ES,ALPHAS,BHIGH
176 PRINT 580
202 PRINT 570
206 PRINT 580
212 IF (ITYPER.EQ.1) PRINT 590
220 IF (ITYPER.EQ.2) PRINT 600
226 IF (ITYPER.LT.1.OR.ITYPER.GT.2) GO TO 540
236 PRINT 610, P,DIA,FY,ES,ALPHAS
253 P=P/100.
C
C INPUT CONCRETE PROPERTIES
C
255 READ 620, THICK,ALPHAC,ZTOT,UNWT,FPC,STRNMUL
274 PRINT 580
300 PRINT 630
304 PRINT 580
310 PRINT 640, THICK,ALPHAC,ZTOT,UNWT,FPC,STRNMUL
C
C INPUT AGE-TENSILE STRENGTH RELATIONSHIP
C
330 IF (STRNMUL.EQ.0.0) STRNMUL=1.0
C
C NSTRN DESIGNATES WHETHER AGE-STRENGTH RELATIONSHIP IS AVAILABLE
C
C NSTRN = 1 AGE-STRENGTH DATA IS PROVIDED
C
332 READ 660, NSTRN,(AGEU(I),TENSION(I),I=1,7)
350 IF (NSTRN.GT.7) READ 650, (AGEU(I),TENSION(I),I=8,NSTRN)
367 TENS=TENSION(NSTRN)
371 IF (NSTRN.EQ.0) GO TO 30
372 PRINT 670, ((AGEU(I),TENSION(I)),I=1,NSTRN)
406 GO TO 60
407 30 CONTINUE
407 PRINT 680
413 PRINT 690
417 DO 50 I=1,8
421 DUMDUM=FPC*PERCENT(I)/100.
424 IF (DUMDUM.EQ.0.) GO TO 40
425 DUMDUM=STRNMUL*3000./(3.+12000./DUMDUM)
431 40 CONTINUE
431 PRINT 700, AXE(I),DUMDUM
441 50 CONTINUE
443 TENS=STRNMUL*3000./(3.+12000./FPC)
450 60 CONTINUE
C
C INPUT SLAB-BASE FRICTION RELATIONSHIP ** (FORCE-DISPLACEMENT**)
C
C FORCE-DISPLACEMENT RELATIONSHIP
C
450 PRINT 710
454 READ 730, IFY,(FEXP(I),YEXP(I),I=1,7)

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JRCP1



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472      IF (IFY.GT.7) READ 720, (FEXP(I),YEXP(I),I=8,IFY)
511      IF (IFY.EQ.1) GO TO 70
513      IF (IFY.EQ.2) GO TO 80
515      IF (IFY.GT.2) GO TO 90
517  70  CONTINUE
517      FRICMUL=FEXP(1)/YEXP(1)
521      FU=FEXP(1)
522      GO TO 100
523  80  CONTINUE
523      FRICMUL=SQRT(ABS(1/YEXP(1)))*FEXP(1)
532      FU=FEXP(1)
533      GO TO 100
533  90  CONTINUE
533      IF (FEXP(1).NE.0.OR.YEXP(1).NE.0.) GO TO 450
541  100 CONTINUE
541      IF (IFY.EQ.2) PRINT 750, FEXP(1),YEXP(1)
553      IF (IFY.EQ.1) PRINT 740, FEXP(1),YEXP(1)
565      IF (IFY.GT.2) PRINT 760, ((FEXP(1),YEXP(1)),I=1,IFY)

C
C      INPUT MAXIMUM DAILY DROP IN TEMPERATURE
C
604      READ 770, CURTEMP,NTEMP,(DT(I),I=1,14)
616      IF (NTEMP.GT.14) READ 780, (OT(I),I=15,NTEMP)
633      PRINT 800
637      PRINT 790, CURTEMP
645      PRINT 810
651      DO 110 I=1,NTEMP
653          TEM7T=DT(I)
655          DT(I)=CURTEMP-DT(I)
657          IF (DT(I).LT.0) DT(I)=0.
662      PRINT 820, I,TEMPT,DT(I)
674  110 CONTINUE

C
C      INPUT MINIMUM TEMPERATURE AFTER
C      CONCRETE GAINS FULL STRENGTH
C
677      READ 830, DE3TATH
704      PRINT 840, DELTATH
712          DELTATH=CURTEMP-DELTATH
714      READ 850, MAXITE,TOL
724      PRINT 860
730      PRINT 870, MAXITE,TOL
C      *****
C      INITIALIZE PARAMETERS
C      *****
740      IFINISH=0
741      TOL=TOL/100.
743  120 CONTINUE
743      IF (IFINISH.EQ.0) GO TO 130
744      PRINT 530
750      PRINT 540, (AN1(N),N=1,40)
756      PRINT 550, NPROB,(AN2(N),N=1,18)
766      IF (IFINISH.EQ.1) PRINT 480
774  130 CONTINUE

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774      IF (ITYPER.EQ.2) ICLOSEP=1
777      ANTEMP=NTEMP
1001      IBABY=0
1002      IBXBAR=0
1003      IENDONE=0
1004      ITEB=0
1005      NTP1=NT*1
1007      IB=1
1010      VDS=THICK
1011      EP=1.E-9
1013      AAA=1
1014      BLOW=BHIGH/2.
140 CONTINUE
CALL DRIVER(NRF,ISTDS,ZTOT,F,SUM,CRWM)
IF(ISTDS.NE.1.0.NRF.EQ.1)GOTO 450

C
C      PREPARE FOR PRINTING RESULTS IF STEEL DESIGN OPTION CHOSEN
C
AB=3.1416*DIA*DIA/4.
P=P*100.
YSL=AB*100./(THICK*P)
PRINT 880,P,YSL
480  FORMAT (62X,9H MAXIMUM ,/, 2X,23H TIME TEMP DRYING ,
1      53H TENSILE CRACK CRACK CONCRETE STRESS IN ,/
2      1X,51H (DAYS) DROP SHRINKAGE STRGTH SPACING WIDTH ,
3      4X,22H STRESS THE STEEL ,/)
490  FORMAT ( 2X,F5.2,2X,F5.1,2X,E10.3,2X,F5.1,3X,F6.1,
1      1X,F10.3+2(2X,E10.3))
510  FORMAT ( 20A4)
520  FORMAT (A5,5X,17A4,A2)
530  FORMAT (5H1 ,76X,10H1-----TRIM)
540  FORMAT (1X,20A4)
550  FORMAT (///5H PROB,/,A5,5X,17A4,A2,/)
560  FORMAT (15,5X,6(E10.3))
570  FORMAT (10X,1H*,46X,1H*,/,
1      10X,48H* STEEL PROPERTIES *,/,
2      10X,1H*,46X,1H*)
580  FORMAT (10X,48(1H*))
590  FORMAT (///15X,39H TYPE OF LONGITUDINAL REINFORCEMENT IS ,/
1      26X,14H DEFORMED BARS)
600  FORMAT (///15X,39H TYPE OF LONGITUDINAL REINFORCEMENT IS ,/
1      23X,21H DEFORMED WIRE FABRIC)
610  FORMAT (///15X,24H PERCENT REINFORCEMENT =,E10.3,/,
1      15X,24H BAR DIAMETER =,E10.3,/,
2      15X,24H YIELD STRESS =,E10.3,/,
3      15X,24H ELASTIC MODULUS =,E10.3,/,
4      15X,24H THERMAL COEFFICIENT =,E10.3,///)
620  FORMAT (10X,6(E10.3))
630  FORMAT (10X,1H*,46X,1H*,/,
1      10X,48H* CONCRETE PROPERTIES *,/,
2      10X,1H*,46X,1H*)
640  FORMAT (///15X,22H SLAB THICKNESS =,E10.3,/,
1      15X,22H THERMAL COEFFICIENT =,E10.3,/,
2      15X,22H TOTAL SHRINKAGE =,E10.3,/,
3      15X,22H UNIT WEIGHT CONCRETE=,E10.3,/,
4      15X,22H COMPRESSIVE STRENGTH=,E10.3,/)

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```
1051 5      15X,22H (TENS/FLEX)RATIO      =,E10.3,///  
1051 650  FORMAT ((10X,14F5.0))  
1051 660  FORMAT (15,5X,14F5.0)  
1051 670  FORMAT (///,15X,40H TENSILE STRENGTH DATA AS INPUT BY USER ,///  
1      14X,16H AGE, TENSILE ,/  
2      13X,18H (DAYS) STRENGTH ,/  
3      (15X,F5.1,2X,F5.1))  
1051 680  FORMAT (14X,22H TENSILE STRENGTH DATA,/,15X,21(1H*))  
1051 690  FORMAT ( /,15X,43H NO TENSILE STRENGTH DATA IS INPUT BY USER ,/  
1      15X,49H THE FOLLOWING AGE-TENSILE STRENGTH RELATIONSHIP ,/  
2      15X,46H IS USED WHICH IS BASED ON THE RECOMMENDATION ,/  
3      15X,37H GIVEN BY U.S. BUREAU OF RECLAMATION ,///  
4      15X,15H AGE, TENSILE ,/  
5      14X,17H (DAYS) STRENGTH ,/  
1051 700  FORMAT (13X, 2(2X,F5.1))  
1051 710  FORMAT ( /,10X,48(1H*),/,10X,1H*,46X,1H*,///  
1      10X,1H*,5X,35H SLAB-BASE FRICTION CHARACTERISTICS,6X,1H*,/  
2      10X,1H*,14X,17H F-Y RELATIONSHIP,15X,1H*,/,10X,1H*,46X,1H*,///  
3      10X,48(1H*),///  
1051 720  FORMAT ((10X,14F5.2))  
1051 730  FORMAT (15,5X,14F5.2)  
1051 740  FORMAT (15X,41HTYPE OF FRICTION CURVE IS A STRAIGHT LINE,///  
1      15X,24H MAXIMUM FRICTION FORCE=,2X,F6.3,/  
2      15X,24H MOVEMENT AT SLIDING      =,2X,F6.3)  
1051 750  FORMAT (15X,36HTYPE OF FRICTION CURVE IS A PARABOLA,///  
1      15X,24H MAXIMUM FRICTION FORCE=,2X,F6.3,/  
2      15X,24H MOVEMENT AT SLIDING      =,2X,F6.3)  
1051 760  FORMAT (15X,45HTYPE OF FRICTION CURVE IS A MULTILINEAR CURVE,///  
1      15X,5H F(1),2X,5H Y(1),/, (15X,F6.3,2X,F6.3),///  
1051 770  FORMAT (F5.1,I5,14F5.1)  
1051 780  FORMAT ((10X,I4F5.1))  
1051 790  FORMAT ( 14X,20H CURING TEMPERATURE=,F5.1,///  
1051 800  FORMAT (///,10X,30(1H*),///  
1      10X,1H*,28X,1H*,/  
2      10X,30H* TEMPERATURE DATA      *,/,10X,1H*,28X,1H*,/  
3      10X,30(1H*),///  
1051 810  FORMAT (20X,7HMINIMUM,6X,7HDROP IN,/  
1      10X,3MDAY,5X,11HTEMPERATURE,2X,11HTEMPERATURE,/  
1051 820  FORMAT (10X,(13,8X,F5.1,8X,F5.1))  
1051 830  FORMAT (10X,F5.1)  
1051 840  FORMAT (/,14X,36H MINIMUM TEMPERATURE EXPECTED AFTER ,/  
1      14X,36H CONCRETE GAINS FULL STRENGTH      =,F5.0,  
2      20H DEGREES FARENHITE ,///  
1051 850  FORMAT (15,F5.1)  
1051 860  FORMAT (///,10X,48(1H*),/,10X,1H*,46X,1H*,/,10X,1H*,6X,  
1      33H ITERATION AND TOLERANCE CONTROL ,7X,1H*,/  
2      10X,1H*,46X,1H*,/,10X,48(1H*),///  
1051 870  FORMAT (10X,40H MAXIMUM ALLOWABLE NUMBER OF ITERATIONS=,I5 ,///  
1      10X,28H RELATIVE CLOSURE TOLERANCE=,F5.1, 8H PERCENT,///  
1051 880  FORMAT (1X,* LONGITUDINAL STEEL = *,E10.3,* PERCENT. ,///  
1      * SPACED = *,E10.3,* INCHES CENTER TO CENTER ,///  
1051 900  FORMAT (10X,15,2X,F5.1,2X,*(E10.3,2X,))  
1051 910  FORMAT (///,10X,37H FOR ALLOWABLE NUMBER OF ITERATIONS, ,/  
1      10X,36H THE SOLUTION DOES NOT CLOSE ON THE ,  
2      10X,24H STRESS STRENGTH CURVE. ,/  
3      10X,24H PROGRAM IS TERMINATED. )
```

JRCP1

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```
1051 940  FORMAT (///,10X,* ERROR IS DETECTED *,/  
1      10X,* FRICTION-MOVEMENT CURVE INPUT IS WRONG *,/  
2      10X,* F(1) AND Y(1) SHOULD BE ZEROS *,/  
3      10X,* PROGRAM IS TERMINATED *)  
1051 950  FORMAT (///,10X,* ERROR IS DETECTED *,/  
1      10X,*TYPE OF PERCENT REINFORCMENT OPTION IS NOT RIGHT,/  
2      10X,*ITPER=,I5)  
1051 960  FORMAT (///,10X,* PROGRAM IS TERMINATED , ITE = *,I5)  
1051 450  CONTINUE  
1051 ENO
```

JRCP1

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PROGRAM LENGTH INCLUDING I/O BUFFERS  
6410

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	12	20	-	24	30	-	407	40	-	431
60	-	450	70	-	517	80	-	523	90	-	533
100	-	541	120	-	743	130	-	774	140	-	1016
450	-	1051	480	-	1201	490	-	1231	510	-	1243
520	-	1245	530	-	1250	540	-	1254	550	-	1256
551	-	1151	553	-	1156	554	-	1163	555	-	1125
556	-	1131	557	-	1065	560	-	1263	570	-	1266
580	-	1306	590	-	1311	600	-	1324	610	-	1337
620	-	1400	630	-	1403	640	-	1423	650	-	1472
660	-	1475	670	-	1500	680	-	1530	690	-	1536
700	-	1603	710	-	1606	720	-	1635	730	-	1640
740	-	1643	750	-	1665	760	-	1707	770	-	1724
780	-	1727	790	-	1732	800	-	1740	810	-	1767
820	-	2004	830	-	2010	840	-	2013	850	-	2035
860	-	2037	870	-	2061	880	-	2077	900	-	2114
910	-	2121	940	-	2152	950	-	2202	960	-	2222

EXTERNALS AND TAGS

INPUTC	-	S00200	OUTPUTC	-	S00300	SQRT	-	S00400	ORIVER	-	S00500
END	-	S00600	QBENTRY	-	S00100						

BLOCK NAMES AND LENGTHS

BLOCK1	-	12C01	BLOCK2	-	1755C02	BLOCK3	-	6C03	BLOCK4	-	3724C04
BLOCK5	-	30C05	BLOCK6	-	10C06	BLOCK8	-	3726C07	BLOCK9	-	5C10
BLOCK10	-	53C11	BLOCK12	-	66C12	BLOCKA	-	775C13	BLOCKB	-	6C14
BLOCKC	-	1756C15									

VARIABLE ASSIGNMENTS

AAA	-	765C02	AB	-	4343	AGE	-	4300	AGEU	-	2C11
AL	-	0C04	ALPHAC	-	0C06	ALPHAS	-	1C06	ANTEMP	-	4337
ANI	-	2234	ANZ	-	2304	BHIGH	-	0C14	BLOW	-	1C14
CONSTR	-	1752C04	CRWM	-	4324	CURTEMP	-	4333	DELTATM	-	4335
DIA	-	10C01	DT	-	0C12	DUMDUM	-	4332	EP	-	5C06
ES	-	5C01	F	-	2326	FEXP	-	0C05	FPC	-	3C06
FRF	-	1753C15	FRICMUL	-	24C05	FU	-	26C05	FY	-	1754C13
I	-	4330	IB	-	4342	IBABY	-	4C03	IBXBAR	-	4340
ICLOSEB	-	2740C07	IENDONE	-	4341	IFINISH	-	4336	IFY	-	27C05
ISTDS	-	4325	ITEB	-	5C03	ITEST	-	4321	ITYPER	-	7C06
L	-	1755C15	MAXITE	-	1753C02	MODFLAG	-	5C14	N	-	4322
NEG1	-	4320	NPROB	-	4323	NRF	-	4326	NSTRN	-	0C11
NT	-	25C05	NTEMP	-	62C12	NTP1	-	6C01	P	-	2C01
PERCENT	-	4310	REFF	-	765C07	SS	-	0C02	STRAIN	-	765C04
STRESS	-	2737C04	STRNMUL	-	52C11	STRSC1	-	0C15	STRSS1	-	765C15
SUM	-	3313	TEMP1	-	4334	TENS	-	4331	TENSION	-	26C11
THICK	-	1C01	TOL	-	6C06	UNWT	-	11C01	VDS	-	1C11
W	-	774C13	WS	-	766C02	XBAR	-	0C03	Y	-	0C07
YEXP	-	12C05	YP	-	1752C07	YPITE	-	2741C07	YSL	-	2C14
Y1	-	2C13	ZTOT	-	4327						

START OF CONSTANTS

1052

JRCP1

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START OF TEMPORARIES  
2227

START OF INDIRECTS  
2234

START OF VARIABLES  
2234

SPACE REQUIRED TO COMPILE -- JRCP1  
40200

JRCP1

```

SUBROUTINE DRIVER (NRF,ISTDS,ZTOT,F,SUM,CRWM)
11 DIMENSION F(501),SUM(501)
11 COMMON/BLOCK1/RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,OIA,UNWT
11 COMMON/BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW
11 COMMON/BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
11 COMMON/BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
11 COMMON/BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
11 COMMON /BLOCK8/ Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
11 COMMON/BLOCKD/STRSC2(501),OIST
11 COMMON/BLOCKA/Z,YP1,Y1(501),DELTAX,DELTAT,TEMP1,REFF1,YPITE1,W
11 COMMON/BLOCKB/BHIGH,BLOW,YSL,P2,YST,MOOFLAG
11 COMMON/BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
11 COMMON /BLOCK12/ DT(501),NTEMP,NTIFLAG,UPINC,DOWNINC
11 REAL L
11 L=XBAR
12 IP=0
13 IFS=0
14 IF (NRF.NE.1) XOTO 5
16 P=0.
17 GOTO 10
17 5 IF (ISTDS.NE.1) GOTO 10
21 CALL STDS (FRW,FY,W)
23 10 CONTINUE
23 ITIME=0
24 20 CONTINUE
C
C MAIN LOOP ON TIME
C
24 ITIME=ITIME+1
26 TIME=FLOAT(ITIME)
27 IF (TIME.GT.28.0) GOTO 30
36 DELTAT=DT(ITIME)
37 IGB=0
40 CALL FORWARD (TENSTRN,ZTOT,Z)
42 IS=0
43 CALL MODEL1 (TIME,IS,INT)
46 CALL DIST1 (DIST,TENSTRN,IGB)
51 IF (NRF.EQ.1) XOTO 50
57 IF (IGB.EQ.1) XOTO 27
62 IF (DIST.NE.XBAR/2.) GO TO 20
65 INC=DIST/H
C
C CALCULATE FIRST CRACK WIDTH
C
67 DUM=DIST-(INC*H)
71 IF (DUM.EQ.0.) GOTO 123
72 YC=DUM*(Y1(INC+1)-Y1(INC))/H
77 GOTO 12
77 123 YC=Y1(INC)
101 12 CRACKW1=2.*ASS(YC)
104 IF (CRACKW1.GT.CRWM) GOTO 70
107 IF (CRACKW1.GT.0.00100) GOTO 45
112 IF (ISTDS.EQ.1) GOTO 38
113 45 CONTINUE

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DRIVER

```

113 PRINT 540, CRACKW1, TIME
123 IF (MODFLAG.EQ.1) RETURN
131 250 ISC=1
132 CALL MODEL2 (F,BONDL,Z,DELTAT,SUM,INDEX,STRMAX,ISC)
141 L=XBAR
143 DIFF=STRSC-0.75*FY
146 IF (DIFF.GT.0.1) GOTO 200
C
C SUB-LOOP ON TIME FOR CRACK 2
C
155 ITIME=ITIME+1
156 TIME=FLOAT(ITIME)
160 IF (TIME.GT.28.0) GOTO 220
163 DELTAT=DT(ITIME)
164 CALL FORWARD (TENSTRN,ZTOT,Z)
166 IS=1
167 CALL MODEL1 (TIME,IS,INT)
172 ISC=0
173 CALL MODEL2 (F,BONDL,Z,DELTAT,SUM,INDEX,STRMAX,ISC)
206 L=XBAR
210 H=L/NT
212 CALL STRSC0 (STRSCON)
214 IF (TENSTRN.GT.STRSCON) GOTO 250
223 TENSTRN=STRSCON
223 CALL DIST1 (DIST,TENSTRN,IGB)
C
C CALCULATE THE SECOND CRACK WIDTH
C
226 CRACKW2=ABS((STRSCON*DIST)/2.-2.*(Z*ALPHAC*DELTAT))
235 IF (CRACKW2.GT.CRWM) GOTO 260
244 ISC=1
245 CALL MODEL2 (F,BONDL,Z,DELTAT,SUM,INDEX,STRMAX,ISC)
254 L=XBAR
256 H=L/NT
260 DIFF=STRSC-0.75*FY
263 IF (DIFF.GT.0.1) GOTO 200
272 PRINT 300, TIME, CRACKW2, DIST
303 300 FORMAT (29H SECOND CRACK OCCURS AT TIME ,F8.4,16H WITH A WIDTH OF .
1 F8.4,/,36H AT A DISTANCE FROM THE FREE EDGE OF ,E10.3)
303 RETURN
304 30 IF (NRF.EQ.1) XOTO 35
314 IF (ISTDS.EQ.1) GO TO 38
316 PRINT 510
321 510 FORMAT (/,5X,34HNO CRACK OCCURS AT END OF 28 DAYS.)
321 RETURN
322 35 CONTINUE
322 PRINT 520,L
330 RETURN
331 200 IF (IFS.EQ.1) GOTO 70
337 4F (ISTDS.EQ.1) GOTO 270
340 PRINT 210,STRSC,TIME
210 210 FORMAT (20H STRESS IN THE STEEL,E10.3,25H IS GREATER THAN ITS WORK
1,20HING STRENGTH AT TIME,F8.4)
347 RETURN
350 220 CONTINUE

```

DRIVER

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
350 PRINT 230
354 230 FORMAT(46H AT THE END OF 28 DAYS NO SECOND CRACK OCCURS )
354 RETURN
355 260 CONTINUE
355 IF (ISTDS.EQ.1)GOTO 270
363 PRINT 280,CRACKW2,TIME
372 280 FORMAT(13H SECOND CRACK,F8.4,51H IS WIDER THAN MAXIMUM ALLOWABLE C
IRACKWIDTH AT TIME ,F8.4)
RETURN
372 50 CONTINUE
373 IF(DIST.LE.XBAR/2.)GOTO 51
402 IF(DIST.GT.0.75*XBAR)GOTO 52
406 GOTO 20
406 520 FORMAT(/,1X,*FOR THE GIVEN INPUT DATA, THE LENGTH OF THE NON-*
1 ,/, * REINFORCED SLAB IS *E10.3,* INCHES.*)
406 51 CONTINUE
C
C ADJUST LENGTH FOR NON-REINFORCED.
406 L=L-LX2.
411 GOTO 10
411 52 CONTINUE
411 L=L+L/2.
414 GOTO 10
414 60 CONTINUE
414 PRINT 530, CRACKW1,TIME,STRSC1(1NC)
426 530 FORMAT(/,1X,11H CRACKWIDTH,F8.4,
154H IS GREATER THAN MAXIMUM ALLOWABLE CRACKWIDTH AT TIME
2F8.4,/,26H WITH A CONCRETE STRESS OF ,F8.4)
RETURN
427 70 CONTINUE
427 IF(ISTDS.NE.1)GOTO 60
435 IP=IP+1
436 IF(IP.GT.4MAXITE)GOTO 14
C
C ADJUST STEEL PERCENTAGE FOR STEEL DESIGN OPTION
441 P=P/P/2.
443 GOTO 10
444 540 FORMAT(24H WIDTH OF FIRST CRACK IS ,F8.4,7H INCHES,8H AT TIME.
1 F8.4,7H DAYS. ,//)
444 38 IF(IFS.EQ.1)XOTO 18
446 P=P-P/2.
451 IF(P.EQ.0.)GOTO 39
451 IF(P.LE..00005)P=0.
454 GOTO 10
455 270 CONTINUE
455 SA=THICK*P
457 SFC=STRSC*SA
461 SA=SFC/(0.75*FY)
464 P=SA/THICK
466 IFS=1
467 GOTO 10
467 18 PRINT 915
473 915 FORMAT(3X,*FOR THE GIVEN SLAB LENGTH, THE PERCENT OF STEEL WAS *
1 *DICTATED BY THE STEEL *,/,* STRESSES AND NOT BY CRACKWIDTH. *,
2 //)
```

DRIVER

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
473 RETURN
474 27 CALL INTRSC(TENSTRN,IS,INT,YC,DIST,ZTOT,ISTDS)
507 IGB=0
510 GOTO 12
514 39 CONTINUE
514 PRINT 550,CRACKW1
522 550 FORMAT(/,3X,* NO STEEL IS NEEDED. WIDTH OF FIRST CRACK = *E10.3,
1 * INCHES. *,/)
522 GOTO 1000
526 14 IF(STRSC.LE.0.75*FY)GOTO 15
532 PRINT 920,STRSC,TIME
541 GOTO 1000
545 15 IF(CRACKW1.LE.CRW1)GOTO 45
550 P=P*100.
551 PRINT 910,CRACKW1,P
561 PRINT 920,STRSC,TIME
571 920 FORMAT(* FOR THE MAX NUMBER OF ITERATION THE STRESS IN THE STEEL *
1 ,/,* AT THE CRACK IS *E10.3,* PSI, AT TIME *F8.4,/)
571 910 FORMAT(3X,*SLAB LENGTH NEEDS TO BE REDUCED,CRACKW1 = *E10.3,
1 ,/, * INCHES WITH PERCENT STEEL = *E10.3)
571 1000 CONTINUE
571 END
```

DRIVER

SUBPROGRAM LENGTH  
1043

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

S	-	17	10	-	23	12	-	101	14	-	526
15	-	545	18	-	467	20	-	24	27	-	474
30	-	304	35	-	322	38	-	444	39	-	514
45	-	113	50	-	373	51	-	406	52	-	411
60	-	414	70	-	427	123	-	77	200	-	331
210	-	626	220	-	350	230	-	641	250	-	131
260	-	355	270	-	455	280	-	650	300	-	602
510	-	620	520	-	662	530	-	676	540	-	720
550	-	752	910	-	1002	915	-	733	920	-	765
1000	-	571									

EXTERNALS AND TAGS

STOS	-	S00100	FORWARD-	S00200	MODEL1 -	S00300	DIST1 -	S00400
OUTPTC	-	S00500	MODEL2 -	S00600	STRSCO -	S00700	INTRSCT-	S01000
END	-	S01100						

BLOCK NAMES AND LENGTHS

BLOCK1	-	12C01	BLOCK2 -	1755C02	BLOCK3 -	6C03	BLOCKS -	30C04
BLOCK6	-	10C05	BLOCK8 -	3726C06	BLOCKD -	766C07	BLOCKA -	775C10
BLOCKB	-	6C11	BLOCKC -	1756C12	BLOCK12-	66C13		

VARIABLE ASSIGNMENTS

ALPHAC	-	0C05	BOND1 -	1033	CRACKW1-	1031	CRACKW2-	1040	
DELTAT	-	770C10	D1FF -	1036	DIST	-	765C07	DT -	0C13
DUM	-	1027	FEXP -	0C04	FRF	-	1753C12	FY -	1754C12
H	-	2737C06	IFS -	1021	168	-	1023	INC -	1752C12
INDEX	-	1034	INT -	1026	IP	-	1020	IS -	1025
ISC	-	1032	ITIME -	1022	L	-	1755C12	MAXITE -	1753C02
MODFLAG-	SC11	NT	-	25C04	P	-	2C01	REFF -	765C06
SA	-	1041	SFC -	1042	SS	-	0C02	STRMAX -	1035
STRSC	-	1C03	STRSCON-	1037	STRSC1	-	0C12	STRSC2 -	0C07
STRSS1	-	765C12	TENSTRN-	1024	THICK	-	1C01	TIME -	4C05
W	-	774C10	WS -	766C02	XBAR	-	0C03	Y -	0C06
YC	-	1030	YEXP -	12C04	YP	-	1752C06	YPITE -	2741C06
Y1	-	2C10	Z -	0C10					

START OF CONSTANTS

572

START OF TEMPORARIES

1015

START OF INDIRECTS

1020

START OF VARIABLES

1020

SPACE REQUIRED TO COMPILE -- DRIVER  
35600

DRIVER

```

SUBROUTINE MODEL1(TIME,IS,INT)
6 COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
6 COMMON/BLOCKS/FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
6 COMMON/BLOCK2/ SS(S01),AAA,WS(S01),MAXITE,CRACKW
6 COMMON/BLOCKA/Z,YP1,Y1(S01),DELTAX,DELTAT,TEMP1,REFF1,YPITE1,W
6 COMMON/BLOCKC/ STRSC1(S01),STRSS1(S01),INC,FRF,FY,L
6 COMMON /BLOC2D/ STRSC2(S01),DIST
6 COMMON/BLOCKB/ Y(S01),REFF(S01),YP(S01),H,ICLOSEB,YPITE(S01)
6 REAL L
6 IF(INT.EQ.1)XOTO 40
C INITIALIZE L6OP PARAMETERS
10 INC=0
11 H=L/NT
13 DELTAX=0.0
C MAIN LOOP ON INCREMENT.
14 10 DELTAX=DELTAX-H
16 INC=INC+1
20 IF(DELTAX.GT.L)RETURN
23 IF(IS.NE.1)GOTO 40
25 IF(DELTAX.GT.DIST)RETURN
30 F0=0.0
31 CALL STRSCS(F0)
33 CALL FRIC1(F1)
35 REFF1=F1
37 CALL STRSCS(F1)
40 CALL FRIC1(F2)
42 F3=(F1+F2)/2.
20 CONTINUE
45 CALL BACFRC1(F3)
47 CALL STRSCS(F3)
51 CALL CLOSE1(INDEX,F3)
53 IF(INDEX.EQ.1)GOTO 30
57 CALL BINRYF1(F3)
61 GOTO 20
30 CONTINUE
64 IF(INT.EQ.1)RETURN
64 IF(P.EQ.0.)GOTO 10
66 STRSS1(INC)=F3*DELTAX/(P*THICK)-STRSC1(INC)/P
67 GOTO 10
75 END
75
    
```

MODEL1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
105

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10 - 14 20 - 45 30 - 64 40 - 30

EXTEPNALS AND TAGS

STRSCS - 500100 FRIC1 - 500200 BACFR1- 500300 CLOSE1 - 500400  
BINRYF1- 500500 END - 500600

BLOCK NAMES AND LENGTHS

BLOCK1 - 12C01 BLOCK5 - 30C02 BLOCK2 - 1755C03 BLOCKA - 775C04  
BLOCKC - 1756C05 BLOCKD - 766C06 BLOCK8 - 3726C07

VARIABLE ASSIGNMENTS

DELTA - 767C04 DIST - 765C06 FEXP - 0C02 F0 - 100  
F1 - 101 F2 - 102 F3 - 103 H - 2737C07  
INC - 1752C05 INDEX - 104 L - 1755C05 NT - 25C02  
P - 2C01 REFF - 765C07 REFF1 - 772C04 SS - 0C03  
STRSC1 - 0C05 STRSC2 - 0C06 STRSS1 - 765C05 THICK - 1C01  
WS - 766C03 Y - 0C07 YEXP - 12C02 YP - 1752C07  
YPITE - 2741C07 Y1 - 2C04

START OF CONSTANTS

76

START OF TEMPORARIES

77

START OF INDIRECTS

100

START OF VARIABLES

100

SPACE REQUIRED TO COMPILE -- MODEL1

33000

MODEL1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
6 SUBROUTINE DIST1(DIST,TENSTRN,IGB)
6 COMMON /BLOCK3/XBAR,STRSC,STRSB,STRC,IBABY,ITEB
6 COMMON /BLOC25/FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
6 COMMON /BLOCK8/Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
6 COMMON /BLOC2C/STRSC1(501),STRSS1(501),INC,FRF,FY,L
6 DO 10 J=1,NT
7 IF (ABS(TENSTRN).LE.ABS(STRSC1(J)))GOTO 20
13 10 CONTINUE
16 DIST=0.75*XBAR
17 RETURN
20 IF (J.EQ.1)GOTO 30
22 DUMDUM=(STRSC1(J)-STRSC1(J-1))/(ABS(H*J)-ABS(H*(J-1)))
35 DIST=ABS(H*(J-1))*(ABS(TENSTRN)-STRSC1(J-1))/DUMDUM
47 IF (DIST.GE.XBAR/2.)RETURN
52 30 IGB=1
53 RETURN
54 END
```

DIST1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH

67

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20 - 20 30 - 52

EXTERNALS AND TAGS

END - S00100

BLOCK NAMES AND LENGTHS

BLOCK3 - 6C01 BLOCK5 - 30C02 BLOCK8 - 3726C03 BLOCKC - 1756C04

VARIABLE ASSIGNMENTS

DUMDUM - 66 FEXP - 0C02 H - 2737C03 J - 65  
NT - 25C02 REFF - 765C03 STRSC1 - 0C04 STRSS1 - 765C04  
XBAR - 0C01 Y - 0C03 YEXP - 12C02 YP - 1752C03  
YPITE - 2741C03

START OF CONSTANTS

55

START OF TEMPORARIES

57

START OF INDIRECTS

65

START OF VARIABLES

65

SPACE REQUIRED TO COMPILE -- DIST1

32700

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

3      SUBROUTINE STRSCO(STRSCON)
3      COMMON /BLOCK8/Y(501),REFF(501),YP(501),M,ICLOSEB,YPITE(501)
3      COMMON /BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
3      COMMON /BLOC2D/STRSC2(501),DIST
3      REAL LONG,M,M1
3      DELTAX=0.0
4      50 CONTINUE
4      LONG=(0.50*DIST)-DELTAX
7      MIS=0
10     CALL STRSC12(MIS,STRSC01,STRSC02,LONG,J,I)
14     MIS=1
15     CALL STRSC12(MIS,STRSC01,STRSC02,LONG,J,I)
21     DIFF=STRSC01-STRSC02
23     IF(DIFF)20,30,40
26     20 DELTAX=DELTAX+M
30     GOTO 50
31     30 STRSCON=STRSC01
32     RETURN
33     40 M1=-((STRSC1(I)-STRSC1(I-1))/H)
37     B1=STRSC1(I-1)
41     IF(J.EQ.0)GOTO 45
42     M=(STRSC2(J+1)-STRSC2(J))/H
45     B=STRSC2(J)
46     STRSCON=(B-B1*M/M1)/(1-M/M1)
56     RETURN
56     45 M=STRSC2(J+1)/H
61     B=0.
62     GOTO 46
62     END

```

DIST1

STRSCO



RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
102

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS  
20 - 26 30 - 31 40 - 33 45 - 56  
46 - 46 50 - 4

EXTERNALS AND TAGS

STRSC12- S00100 END - S00200

BLOCK NAMES AND LENGTHS

BLDCKB - 3726C01 BLOCKC - 1756C02 BLOCKD - 766C03

VARIABLE ASSIGNMENTS

B - 101 B1 - 100 DELTAX - 71 DIFF - 77  
DIST - 765C03 H - 2737C01 I - 76 J - 75  
LONG - 66 M - 67 MIS - 72 M1 - 70  
REF - 765C01 STRSC01 - 73 STRSC02 - 74 STRSC1 - 0C02  
STRSC2 - 0C03 STRSS1 - 765C02 Y - 0C01 YP - 1752C01  
YPITE - 2741C01

START OF CONSTANTS

63

START OF TEMPORARIES

64

START OF INDIRECTS

66

START OF VARIABLES

66

SPACE REQUIRED TO COMPILE -- STRSCO

32600

STRSCO

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
11 SUBROUTINE STRSC12(MIS,STRSC01,STRSC02,LONG,J,I)
11 COMMON /BLOC25/FEAP(10),YEXP(10),FRICMUL,NT,FU,IFY
11 COMMON /BLOCKB/Y(501),REF(501),YP(501),M,ICLOESB,YPITE(501)
11 COMMON /BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
11 COMMON /BLOC20/STRSC2(501),DIST
11 REAL LONG
11 DO 100 J=1,NT
12 IF (ABS(LONG-J*M).LT.0.10)GOTO 110
17 100 CONTINUE
21 ILONG=LONG
22 IF (ILONG.FQ.0)GOTO 120
23 PRINT 80
26 PRINT 85,LONX,M
41 85 FORMAT(* IN STRSC12 *,* LONG = *,E10.3,* M = *,E10.3)
41 80 FORMAT(40# ERROR IS DETECTED DISTANCES ARE WRONG )
43 STOP 100
110 CONTINUE
43 IF (MIS.NE.1)XOTO 140
51 DUMDUM=(STRSC2(J)-STRSC2(J-1))/(ABS(H*J)-ABS(H*(J-1)))
65 STRSC02=STRSC2(J-1)+DUMDUM*(ABS(LONG)-ABS(H*(J-1)))
76 RETURN
140 CONTINUE
76 I=(NT+1)/2-J
101 DUMDUM=(STRSC1(I+1)-STRSC1(I))/(ABS(H*J)-ABS(H*(J-1)))
113 STRSC01=STRSC1(I)+DUMDUM*(ABS(H*J)-ABS(LONG))
121 RETURN
120 STRSC02=0.
123 J=0
123 I=(NT+1)/2
125 STRSC01=STRSC1(I)
127 RETURN
127 END
```

STRSC12

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
160

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS											
80	-	141	85	-	133	110	-	43	120	-	122
140	-	76									

EXTERNALS AND TAGS

OUTPTC - S00100 STOP - S00200 END - S00300

BLOCK NAMES AND LENGTHS

BLOCKS - 30C01 BLOCKB - 3726C02 BLOCKC - 1756C03 BLOCKD - 766C04

VARIABLE ASSIGNMENTS

DUMDUM	-	157	FEXP	-	0C01	H	-	2737C02	ILONG	-	156
NT	-	25C01	REFF	-	765C02	STRSC1	-	0C03	STRSC2	-	0C04
STRSS1	-	765C03	Y	-	0C02	YEXP	-	12C01	YP	-	1752C02
YPITE	-	2741C02									

START OF CONSTANTS

130

START OF TEMPORARIES

147

START OF INDIRECTS

156

START OF VARIABLES

156

SPACE REQUIRED TO COMPILE -- STRSC12  
33200

STRSC12

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

12 SUBROUTINE INTRSC1(TENSTRN,IS,INT,YC,DIST,ZTOT,ISTDS)
12 COMMON/BLOCK2/SS(501),AAA,WS(501),MAXITE,CRACKW
12 COMMON/BLOCK3/XBAR,STRSC,STRSB,STRC,IBABY,ITEB
12 COMMON/BLOCK9/STX,STY,PSX,PSY,ITE
12 COMMON/BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
12 COMMON/BLOCK6/ALPHAC,ALPHAS,EC,FRP,TIME,EP,TOL,ITYPER
12 COMMON/BLOCK5/FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
12 COMMON/BLOCKA/Z,YP1,Y1(501),DELTAX,DELTAT,TEMP1,REFF1,YPITE1,W
12 INC=NT/2
13 YITEMP=STRSC1(INC)
15 X1=TENSTRN
16 TIME=TIME-0.5
20 IDT=0
21 50 CALL DELTEM1(TIME,DELTAT)
23 CALL FORWARD(TENSTRN,Z,ZTOT)
31 DELTAX=XBAR/2.
33 INT=1
40 ITE=1
41 CALL MODEL1(TIME,IS,INT)
42 IF(IDT.EQ.1)XOTO 30
50 X2=TENSTRN
51 Y2=STRSC1(INT)
53 IF(TIME.LE.0.1)GOTO 80
55 IF(Y2-X2)20,30,10
60 10 TIME=TIME-0.1
62 GOTO 50
63 20 X2=TENSTRN
64 Y2=STRSC1(INC)
66 OIF=(Y2-X2)/X2
71 IF(ABS(OIF).JE.TOL)GOTO 30
74 ITE=ITE+1
75 IF(ITE.GT.MAXITE)GOTO 35
100 CALL GETME(X1,YITEMP,X2,Y2,FOUT)
103 TENSTRN=FOUT
110 CALL BACKTIM(TENSTRN,ZTOT,Z)
112 CALL DELTEM1(TIME,DELTAT)
114 CALL MODEL1(TIME,IS,INT)
121 GOTO 20
125 30 INT=0
126 DIST=XBAR/2.
127 YC=Y1(INC)
131 RETURN
132 80 TIME=0.33
134 IDT=1
135 IF(ISTDS.EQ.1)GOTO 50
137 PRINT 400
142 400 FORMAT(* SLAB GETS A CRACK RIGHT AFTER CONCRETE PLACEMENT *
146 1 /*. THE TIME IS ASSUMED TO BE 0.33 DAYS. */,/)
146 GOTO 50
146 35 CONTINUE
156 PRINT 355,ITE,MAXITE
156 355 FORMAT(* THE SOLUTION DID NOT CLOSE IN INTRSC1.*,I3,I3,/)
156 END

```

INTRSCT

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
221

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	60	20	-	63	30	-	125	35	-	146
50	-	21	80	-	132	355	-	202	400	-	165

EXTERNALS AND TAGS

DELTEM1-	S00100	FORWARD-	S00200	MODEL1 -	S00300	GETME -	S00400
BACKTIM-	S00500	OUTPTC -	S00600	END -	S00700		

BLOCK NAMES AND LENGTHS

BLOCK2 -	1755C01	BLOCK3 -	6C02	BLOCK9 -	5C03	BLOCKC -	1756C04
BLOCK6 -	10C05	BLOCK5 -	30C06	BLOCKA -	775C07		

VARIABLE ASSIGNMENTS

DELTAT -	770C07	DELTAX -	767C07	DIF -	217	FEXP -	0C06
FOUT -	220	IDT -	214	INC -	1752C04	ISTDS -	0
ITE -	4C03	MAXITE -	1753C01	NT -	25C06	SS -	0C01
STRSC1 -	0C04	STRSS1 -	765C04	TIME -	4C05	TOL -	6C05
WS -	766C01	XBAR -	0C02	X1 -	213	X2 -	215
YEXP -	12C06	Y1 -	2C07	YITEMP -	212	Y2 -	216
Z -	0C07						

START OF CONSTANTS

157

START OF TEMPORARIES

210

START OF INDIRECTS

212

START OF VARIABLES

212

SPACE REQUIRED TO COMPILE -- INTRSC

33400

INTRSC

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

6      SUBROUTINE STOS(FRF,FY,W)
6      COMMON/BLOCK1/RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNMT
6      COMMON/BLOCK3/XBAR,STRSC,STRSB,STRC,IBABY,ITEB
6      COMMON/BLOCK6/ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
6      COMMON/BLOCK8/BHIGH,BLOW,YSL,P2,YST,MOOFLAG
6      REAL L
6      L=XBAR/12.
6      FS=0.75*FY
10     P=L*FRF/(2.*FS)
11     AB=3.1416/4*DIA**2
14     P2=W*FRF*100.0/(2.*FS)
20     IF (ITYPER.EQ.1)GOTO 10
23     BHIGH=AB/(THICK*P2)
25     PRINT 500,P2,BHIGH
30     BLOW=BHIGH/2.
37     RETURN
41
42     10 YST=AB*100./(THICK*P2)
46     PRINT 510,P2,YST
55     RETURN
56     500 FORMAT(* FOR ITPER EQUAL TO 2, THE TRANSVERSE STEEL IS *,E10.3,
1      * PERCENT SPACED.*,/*,E10.3,* INCHES CENTER TO CENTER.*)
56     510 FORMAT(* FOR ITPER EQUAL TO 1, THE TRANSVERSE STEEL IS *,E10.3,
1      * PERCENT SPACED.*,E10.3,/* INCHES CENTER TO CENTER.*)
56     ENO

```

STDS

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
123

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10 - 42 500 - 66 510 - 103

EXTERNALS AND TAGS

OUTPTC - S00100 END - S00200

BLOCK NAMES AND LENGTHS

BLDCK1 - 12C01 BLOCK3 - 6C02 BLOCK6 - 10C03 BLOCKB - 6C04

VARIABLE ASSIGNMENTS

AB - 122 BHIGH - 0C04 BLOW - 1C04 DIA - 10C01  
FS - 121 ITYPER - 7C03 L - 120 P - 2C01  
P2 - 3C04 THICK - 1C01 XBAR - 0C02 YST - 4C04

START OF CONSTANTS

57

START OF TEMPORARIES

117

START OF INDIRECTS

120

START OF VARIABLES

120

SPACE REQUIRED TO COMPILE -- STDS

32700

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
3 SUBROUTINE STRSCS(FRIC1)
3 COMMON/BLOCK1/RATIO,THICK,P,FF,STRAIN,ES,NTPI,U,DIA,UNWT
3 COMMON/BLOCK6/ALPHAC,ALPHAS,EC,FRP,TIME,EP,TOL,ITYPER
3 COMMON/BLOCKA/Z,YPI,Y1(501),DELTAX,DELTAT,TEMPI,REFF1,YPITEL,W
3 COMMON/BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
3 DUMDUM=FRIC1*DELTAX/(THICK*(1+P*ES/EC))
12 STRSC1(INC)=DUMDUM*P*ES*(Z+DELTAT*(ALPHAC-ALPHAS))/(1+P*ES/EC)
26 Y1(INC)=STRSC1(INC)*DELTAX/EC-DELTAX*(ALPHAC*DELTAT+Z)
35 RETURN
35 END
```

STDS

STRSCS

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH

41

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

EXTERNALS AND TAGS

END - 500100

BLOCK NAMES AND LENGTHS

BLOCK1 - 12C01 BLOCK6 - 10C02 BLOCKA - 775C03 BLOCKC - 1756C04

VARIABLE ASSIGNMENTS

ALPHAC - 0C02 ALPHAS - 1C02 DELTAT - 770C03 DELTAX - 767C03

DUMDUM - 40 EC - 2C02 ES - 5C01 INC - 1752C04

P - 2C01 STRSC1 - 0C04 STRSS1 - 765C04 THICK - 1C01

Y1 - 2C03 Z - 0C03

START OF CONSTANTS

36

START OF TEMPORARIES

36

START OF INDIRECTS

40

START OF VARIABLES

40

SPACE REQUIRED TO COMPILE -- STRSCS

32600

STRSCS

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

3      SUBROUTINE FRIC1(FA)
3      COMMON/BLOCKS/FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
3      COMMON/BLOCKA/Z,YP1,Y1(501),DELTAX,DELTAT,TEMP1,REFF1,YPITE1,W
3      COMMON/BLOCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
5      IF(IFY.EQ.1)XOTO 10
5      IF(IFY.EQ.2)XOTO 40
7      GOTO 90
7      10 CONTINUE
7      SLOPE=FRICMUL
11     FA=Y1(INC)*SLOPE
13     IF(ABS(FA).LE.FU)RETURN
16     IF(FA.GT.0.0)FA=FU
21     IF(FA.LE.0.0)FA=-FU
24     RETURN
25     40 CONTINUE
25     IF(Y1(INC).GT.0.0)GOTO 50
30     FA=FRICMUL*SQRT(ABS(Y1(INC)))
35     GOTO 60
36     50 CONTINUE
36     FA=-FRICMUL*SQRT(Y1(INC))
44     60 CONTINUE
44     IF(ABS(FA).LE.FU)RETURN
50     IF(FA.GT.0.0)FA=FU
53     IF(FA.LT.0.0)FA=-FU
56     RETURN
57     90 CONTINUE
57     DO 100 J=1,INW
61     IF(ABS(Y1(INT)),LT.ABS(YEXP(J)))GOTO 110
67     100 CONTINUE
72     FA=FEXP(IFY)
73     GOTO 120
73     110 CONTINUE
73     DUMDUM=(FEXP(J)-FEXP(J-1))/(ABS(YEXP(J))-ABS(YEXP(J-1)))
102    FA=FEXP(J-1)+DUMDUM*(ABS(Y1(INC))-ABS(YEXP(J-1)))
112    120 CONTINUE
112    IF(Y1(INC).GT.0.0)FA=-FA
115    RETURN
116    END

```

FRIC1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
125

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	7	40	-	25	50	-	36	60	-	44
90	-	57	110	-	73	120	-	112			

EXTERNALS AND TAGS

SQRT - S00100 END - S00200

BLOCK NAMES AND LENGTHS

BLOCKS - 30C01 BLOCKA - 775C02 BLOCKC - 1756C03

VARIABLE ASSIGNMENTS

DUNDUM	-	124	FEXP	-	0C01	FRICMUL	-	24C01	FU	-	26C01
IFY	-	27C01	INC	-	1752C03	J	-	123	SLOPE	-	122
STRSC1	-	0C03	STRSS1	-	765C03	YEXP	-	12C01	Y1	-	2C02

START OF CONSTANTS

117

START OF TEMPORARIES

117

START OF INDIRECTS

122

START OF VARIABLES

122

SPACE REQUIRED TO COMPILE -- FRIC1

33100

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBROUTINE BACFR1(F3)

```

3      COMMON /BLOC25/FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
3      COMMON/BLOCKA/Z,YP1,Y1(S01),DELTA,DELTA,TEMPI,REFF1,YPITE1,W
3      IF (FRICMUL.EQ.0.0)RETURN
5      IF (IFY.EQ.1)XOTO 40
7      IF (IFY.EQ.2)XOTO 60
11     DO 10 J=1,IFY
12     IF (ABS(F3).LT.ABS(FEXP(J)))GOTO 20
16     10 CONTINUE
20     YP1=YEXP(IFY)
22     RETURN
22     20 CONTINUE
22     DUNDUM=(FEXP(J)-FEXP(J-1))/(ABS(YEXP(J))-ABS(YEXP(J-1)))
31     YP1=ABS(YEXP(J-1))*(ABS(F3)-FEXP(J-1))/DUNDUM
37     IF (F3.GT.0.0)YP1=-YP1
41     RETURN
42     40 CONTINUE
42     YP1=F3/FRICMUL
44     IF (ABS(F3).GE.FU)YP1=YEXP(1)
50     RETURN
51     60 CONTINUE
51     YP1=(F3/FRICMUL)**2
53     IF (ABS(F3).GE.FU)YP1=YEXP(1)
60     IF (F3.GT.0.0)YP1=-YP1
63     RETURN
64     END

```

FRIC1

BACFR1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
70

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS  
20 - 22 40 - 42 60 - 51

EXTERNALS AND TAGS  
END - S00100

BLOCK NAMES AND LENGTHS  
BLOCK5 - 30C01 BLOCKA - 775C02

VARIABLE ASSIGNMENTS  
DUMDUM - 67 FEXP - 0C01 FRICMUL- 24C01 FU - 26C01  
IFY - 27C01 J - 66 YEXP - 12C01 YP1 - 1C02  
Y1 - 2C02

START OF CONSTANTS  
65

START OF TEMPORARIES  
65

START OF INDIRECTS  
66

START OF VARIABLES  
66

SPACE REQUIRED TO COMPILE -- BACFR1  
32700

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

3	SUBROUTINE BINRYF1(F3)
3	COMMON/BLOCKA/Z,YP1,Y1(S01),DELTAX,DELTAT,TEMP1,REFF1,YPITE1,W
3	COMMON/BLOCKC/STRSC1(S01),STRSS1(S01),INC,FRF,FY,L
7	IF(YP1.GT.Y1(INC))GOTO 10
7	TEMP1=REFF1
10	REFF1=F3
11	F3=(3.*F3-TEMP1)/2.
14	RETURN
14	10 CONTINUE
14	F3=(REFF1+F3)/2.
17	RETURN
17	END

BACFR1

BINRYF1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
23

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS  
10 - 14

EXTERNALS AND TAGS  
ENO - S00100

BLOCK NAMES AND LENGTHS  
BLOCKA - 775C01 BLOCKC - 1756C02

VARIABLE ASSIGNMENTS  
INC - 1752C02 REFF1 - 772C01 STRSC1 - 0C02 STRSS1 - 765C02  
TEMP1 - 771C01 YP1 - 1C01 Y1 - 2C01

START OF CONSTANTS  
20

START OF TEMPORARIES  
22

START OF INDIRECTS  
23

START OF VARIABLES  
23

SPACE REQUIRED TO COMPILE -- BINRYF1  
32400

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

5      SUBROUTINE C30SE1(INDEX,F3)
5      COMMON/BLOCK2/SS(501),AAA,NS(501),MAXITE,CRACKW
5      COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FRC,TIME,EP,TOL,ITYPER
5      COMMON/BLOCK4/Z,YP1,Y1(501),DELTAX,DELTAT,TEMPI,REFF1,YPITE1,W
5      COMMON/BLDCKC/STRSC1(501),STRSS1(501),INC,FRF,FY,L
5      INTEGER AAA
5      INDEX=0
5      BAD=1.
7      IF(AAA.EQ.1)XOTO 50
11     IF(Y1(INC).EQ.0.0)GOTO 10
12     IF(ABS(Y1(INT)).LT.1.E-06)GOTO 10
16     DIF1=(Y1(INC)-YPITE1)/Y1(INC)
21     IF(ABS(DIF1).GT.TOL)BAD=BAD-1.
26     10 CONTINUE
26     IF(BAD.GT.1.)GOTO 50
32     INDEX=1
32     AAA=1
33     RETURN
34     50 CONTINUE
34     AAA=AAA+1
36     IF(AAA.GT.MAXITE)GOTO 70
41     MA1=AAA-1
41     YPITE1=Y1(INC)
43     110 FORMAT(* MA1 IS*,I5,*BAD IS*,F5.1,* AAA IS *,I5)
43     RETURN
44     70 CONTINUE
44     PRINT 120
50     PRINT 110,MA1,BAD,AAA
62     120 FORMAT(* IN SUBROUTINE CLOSE1 THE SOLUTION DID NOT CLOSE*)
62     END

```

BINRYF1

CLOSE1



RUNW VERSION FEB 74 16.51.06. 23 JUL 75

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
110

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS  
10 - 26 50 - 34 70 - 44 110 - 67  
120 - 76

EXTERNALS AND TAGS

OUTPTC - S00100 END - S00200

BLOCK NAMES AND LENGTHS

BLOCK2 - 1755C01 BLOCK6 - 10C02 BLOCKA - 775C03 BLOCKC - 1756C04

VARIABLE ASSIGNMENTS

AAA - 765C01 BAD - 105 DIF1 - 106 INC - 1752C04  
MAXITE - 1753C01 MA1 - 107 SS - 0C01 STRSC1 - 0C04  
STRSS1 - 765C04 TOL - 6C02 WS - 766C01 YPITE1 - 773C03  
Y1 - 2C03

START OF CONSTANTS

63

START OF TEMPORARIES

104

START OF INDIRECTS

105

START OF VARIABLES

105

SPACE REQUIRED TO COMPILE -- CLOSE1  
32700

CLOSE1

SUBROUTINE FORWARD (TENSTRN,ZTOT,Z)

```
C *****
C THIS SUBROUTINE CALCULATES THE TIME DEPENDENT VARIABLES FROM
C WHICH THE SLAB RESPONSES ARE COMPUTED. LINEAR INTERPOLATION
C IS USED TO GET FLEXURAL STRENGTH FROM AGE OF CONCRETE .
C *****
6 COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP],U,DIA,UNWT
6 COMMON /BLOC22/ SS(501),AAA,WS(501),MAXITE,CRACKW
6 COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
6 COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
6 COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
6 COMMON /BLOC26/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
6 COMMON /BLOCK8/ Y(501),REFF(501),YP(501),M,ICLOSEB,YPITE(501)
6 COMMON /BLOCK10/ NSTRN,VDS,AGEU(20),TENSION(20),STRNMUL
6 DIMENSION PERCENT(8),AGE(8)
6 DATA PERCENT/0.,15.,38.,53.,63.,82.,94.,100./
6 DATA AGE/0.,3.,5.,7.,14.,21.,28./
6 INTEGER AAA
C
6 IF (NSTRN.GT.0.) GO TO 30
10 DO 10 I=1,8
11 J=I
11 IF (TIME.3E.AGE(I)) GO TO 20
14 CONTINUE
16 PRINT 80, TIME
16 GO TO 70
20 CONTINUE
6 PERCOM=(PERCENT(J)-PERCENT(J-1))/(AGE(J)-AGE(J-1))
6 PERTOM=PERCENT(J-1)+PERCOM*(TIME-AGE(J-1))
6 COMSTR=PERCOM*FPC/100
6 FLESTRN=3000./(3.+12000./COMSTR)
6 TENSTRN=FLESTRN*STRNMUL
6 GO TO 60
30 CONTINUE
50 DO 40 I=1,NSTRN
50 J=I
52 IF (TIME.3E.AGEU(I)) GO TO 50
55 CONTINUE
60 PRINT 80, TIME
65 GO TO 70
70 CONTINUE
C
C COMPUTE SLOPE BY LINEAR INTERPOLATION
C
70 SLOPE=(TENSION(J)-TENSION(J-1))/(AGEU(J)-AGEU(J-1))
75 TENSTRN=TENSION(J-1)+SLOPE*(TIME-AGEU(J-1))
101 FLESTRN=TENSTRN/STRNMUL
102 COMSTR=(12000.*FLESTRN)/(3000.-3.*FLESTRN)
C
60 CONTINUE
C
106 EC=33.*(UNWT**1.5)*SQRT(COMSTR)
116 RATIO=ES/EC
117 U=9.5*SQRT(COMSTR)/DIA
124 IF (U.GT.800.) U=800.
```

FORWARD

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

131          SHRN=26.*EXP(0.36*VDS)
137          Z=(TIME/(SHRN+TIME))*ZTOT
143          RETURN
144 70 CONTINUE
144 80 FORMAT (//,10X,*ERROR IS DETECTED IN SUBROUTINE FORWARD*//,10X,
1 *TIME ENCOUNTERED IS GREATER THAN MAXIMUM AGE PROVIDED BY THE USE
2R*//, 10X,*TIME **E10.3*//,
3      10X,*PROGRAM IS TERMINATED*)
144          END

```

FORWARD

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBPROGRAM LENGTH
242

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS
20 - 27 30 - 50 50 - 70 60 - 106
70 - 144 80 - 161

EXTERNALS AND TAGS
OUTPTC - S00100 SQRT - S00200 RBAREX - S00300 EXP - S00400
END - S00500

BLCK NAMES AND LENGTHS
BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04
BLOCK5 - 30C05 BLOCK6 - 10C06 BLOCK8 - 3726C07 BLOCK10- 53C10

VARIABLE ASSIGNMENTS
AAA - 765C02 AGE - 223 AGEU - 2C10 AL - 0C04
COMSTR - 236 CONSTR - 1752C04 DIA - 10C01 EC - 2C06
ES - 5C01 FEXP - 0C05 FLESTRN- 237 FPC - 3C06
I - 233 J - 234 NSTRN - 0C10 PERCENT- 213
PERCOM - 235 RATIO - 0C01 REFF - 765C07 SHRN - 241
SLOPE - 240 SS - 0C02 STRAIN - 765C04 STRESS- 2737C04
STRNMUL- 52C10 TENSION- 26C10 TIME - 4C06 U - 7C01
UNWT - 11C01 VDS - 1C10 WS - 766C02 Y - 0C07
YEXP - 12C05 YP - 1752C07 YP1TE - 2741C07

START OF CONSTANTS
145

START OF TEMPORARIES
210

START OF INDIRECTS
213

START OF VARIABLES
213

SPACE REQUIRED TO COMPILE -- FORWARD
33500

```

FORWARD

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBROUTINE MODEL2 (F,BONDL,Z,DELTAT,SUM,INDEX,STRMAX,ISC)
13 DIMENSION F(501),SUM(501)
13 COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
13 COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW
13 COMMON /BLOCK23/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
13 COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
13 COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICNUL,NT,FU,IFY
13 COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
13 COMMON /BLOCK28/ Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
13 COMMON /BLOCK9/ STX,STY,PSX,PSY,ITE
13 COMMON /BLOCK214/ IFINISH
13 COMMON /BLOCKC/ STRSC1(501),STRSS1(501),INC,FRF,FY,L
13 COMMON /BLOCK2D/STRSC2(501),DIST
13 REAL NEG1
13 INTEGER AAA
13 REAL L
13 IF(ISC.EQ.1)GOTO 15
15 INC=2
16 GH=XBAR/NT
20 L=0.0
21 18 L=GH*L
23 H=L/NT
25 INC=INC+1
27 GOTO 16
27 15 CONTINUE
27 L=DIST/2.
31 H=L/NT
33 INC=NT/2
34 16 CONTINUE
34 DO 10 I=1,NTP1
36 Y(I)=REFF(I)*YP(I)+AL(I)*F(I)=0.
54 SS(I)=STRAIN(I)*CONSTR(I)+STRESSS(I)=0.
66 10 CONTINUE
70 IF (ITYPER.EQ.1) CALL DFBAR (BONDL,STRMAX,Z,DELTAT)
100 IF (ITYPER.EQ.2) CALL DFWIRE (BONDL,STRMAX,Z,DELTAT)
110 IF (BONDL.GE.L) GO TO 80
113 IF (L.GT.0.75*DIST)GOTO 88
117 STRAIN=STRMAX/EC
121 CALL STRGENE (BONDL)
122 CALL SIMPSPE (STRAIN,NTP1,H,SUM)
131 CALL CONMOV (SUM,Z,DELTAT)
137 CALL FRIC (F)
144 DO 20 J=1,NTP1
151 REF*(J)=F(J)
153 20 CONTINUE
156 IF (ITYPER.EQ.1) CALL DFBARF (F,BONDL,STRMAX,Z,DELTAT)
167 IF (ITYPER.EQ.2) CALL DFWIREF (F,BONDL,STRMAX,Z,DELTAT)
201 IF (BONDL.GE.3)GOTO 80
204 CALL SIMPSPE (STRAIN,NTP1,H,SUM)
207 CALL CONMOV (SUM,Z,DELTAT)
215 CALL FRIC (F)
222 DO 30 J=1,NTP1
227 F(J)=(REFF(J)*F(J))/2.
233 30 CONTINUE
235 CALL SIMPSPE (F,NTP1,H,SUM)

```

MODEL2

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

240 FF=SUM(NTP1)
246 40 CONTINUE
246 IF (AAA-LT.MAXITE) GO TO 50
251 PRINT 90, AAA
256 PRINT 100
262 PRINT 110, (I,AL(I),REFF(I),YP(I),Y(I),F(I),I=1,NTP1)
335 STOP
337 50 CONTINUE
337 CALL BAKFRIC (F)
344 IF (ITYPER.EQ.1) CALL DFBARF (F,BONDL,STRMAX,Z,DELTAT)
361 IF (ITYPER.EQ.2) CALL DFWIREF (F,BONDL,STRMAX,Z,DELTAT)
373 IF (BONDL.GE.3)GOTO 80
376 CALL SIMPSPE (STRAIN,NTP1,H,SUM)
401 201 FORMAT(10X,*BONDL IN MODEL2 =*,E10.3,/)
401 CALL CONMOV (SUM,Z,DELTAT)
407 CALL CLOSE (NTP1,INDEX,F)
415 IF (INDEX.EQ.1.AND.ICLOSEB.EQ.1) GO TO 70
430 CALL BINARF (F)
431 CALL SIMPSPE (F,NTP1,H,SUM)
437 FF=SUM(NTP1)
445 GO TO 40
446 70 CONTINUE
446 STRSC2(INC)=STRMAX
451 IF(ISC.EQ.1)RETURN
453 IF(L.LE.DIST/2.)GO TO 18
457 88 DELTA=L
C PRINT 161
461 161 FORMAT(10X,*STRSC2*,9X,* INC *,/)
C PRINT 160,(STRSC2(I),I=1,INC)
461 RETURN
461 80 CONTINUE
461 STRSC2(INC)=STRMAX
464 IF(ISC.EQ.1)RETURN
466 IF(L.LE.DIST/2.)GOTO 18
472 81 CONTINUE
472 PRINT 150
476 RETURN
477 150 FORMAT(///,10X,* BOND LENGTH IS GREATER THAN DIST,*)
160 FORMAT(10X,E10.3,SX,IS)
90 FORMAT (///,10X,*RESULTS FOR ITERATION *, IS,/)
100 FORMAT (/,12X,*I*,7X,*AL(I)*,7X,*REFF*,9X,*YP*,11X,*Y*,11X,*F*,/)
110 FORMAT (10X,IS,5(2X,E10.3))
130 FORMAT ( 10X,* STRMAX =*,E10.3)
140 FORMAT (///,15X,* FOR TIME OF *,E10.3,/,
1 10X,*SHRINKAGE=*,E10.3,/,
2 10X,*DELTAT =*,E10.3)
477 END

```

MODEL2

RUNW VERSION FEB 74 16.S1.06. 23 JUL 75

SUBPROGRAM LENGTH  
613

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

15	-	27	16	-	34	18	-	21	40	-	246
50	-	337	70	-	446	80	-	461	81	-	472
88	-	457	90	-	530	100	-	535	110	-	544
130	-	550	140	-	554	150	-	517	160	-	525
161	-	513	201	-	506						

EXTERNALS AND TAGS

DFBAR	-	S00100	DFWIRE	-	S00200	STRGENE	-	S00300	SIMPSP	-	S00400
CONMOV	-	S00500	FRIC	-	S00600	DFBARF	-	S00700	DFWIREF	-	S01000
OUTPTC	-	S01100	STOP	-	S01200	BAKFRIC	-	S01300	CLOSE	-	S01400
BINARYF	-	S01500	END	-	S01600						

BLOCK NAMES AND LENGTHS

BLOCK1	-	12C01	BLOCK2	-	1755C02	BLOCK3	-	6C03	BLOCK4	-	3724C04
BLOCK5	-	30C05	BLOCK6	-	10C06	BLOCK8	-	3726C07	BLOCK9	-	5C10
BLOCK14	-	1C11	BLOCKC	-	1756C12	BLOCKO	-	766C13			

VARIABLE ASSIGNMENTS

AAA	-	765C02	AL	-	0C04	CONSTR	-	1752C04	DELTAX	-	612
DIST	-	765C13	EC	-	2C06	FEXP	-	0C05	FF	-	3C01
GH	-	607	H	-	2737C07	I	-	610	ICLOSEB	-	2740C07
INC	-	1752C12	ISC	-	1	ITYPER	-	7C06	J	-	611
L	-	1755C12	MAXITE	-	1753C02	NEGT	-	606	NT	-	25C05
NTP1	-	6C01	REFF	-	765C07	SS	-	0C02	STRAIN	-	765C04
STRAIN	-	4C01	STRESSS	-	2737C04	STRMAX	-	0	STRSC1	-	0C12
STRSC2	-	0C13	STRSS1	-	765C12	WS	-	766C02	XBAR	-	0C03
Y	-	0C07	YEXP	-	12C05	YP	-	1752C07	YPITE	-	2741C07

START OF CONSTANTS  
500

START OF TEMPORARIES  
574

START OF INDIRECTS  
577

START OF VARIABLES  
606

SPACE REQUIRED TO COMPILE -- MODEL2.  
35100

MODEL2

RUNW VERSION FEB 74 16.S1.06. 23 JUL 75

SUBROUTINE C6NMOV (SUM,Z,DELTA)

```

C *****
C THIS SUBROUTINE COMPUTES THE MOVEMENT OF THE CONCRETE AT
C EVERY STATION . THE MOVEMENT IS COMPUTED FROM THE DEVELOPPED
C DIFFERENTIAL EQUATION .
C *****
DIMENSION SUM(50)
COMMON /BLOCK1/ RAT10,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
COMMON /BLOCK2/ SS(50),AAA,WS(50),MAXITE,CRACKW
COMMON /BLOC23/ XBAR,STRSC,STRSB,STRC,1BABY,1TEB
COMMON /BLOCK4/ AL(50),STRAIN(50),CONSTR(50),STRESSS(50)
COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU
COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL
COMMON /BLOC28/ Y(50),REFF(50),YP(50),H,ICLOSEB,YPITE(50)
INTEGER AAA
DO 10 I=1,NTP1
7   Y(I)=SUM(I)-AL(I)*(ALPHAC*DELTAT+Z)+Y(1)
15  IF (ABS(Y(I)).GT.1.) GO TO 20
22  10 CONTINUE
24  RETURN
24  20 CONTINUE
24  PRINT 50, (Y(I),I=1,NTP1)
37  50 FORMAT (/,10X,47H MOVEMENTS GREATER THAN 1 INCH ARE ENCOUNTERED ,
1* 10X,8(2X,E10.3))
37  END

```

CONMOV

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
57

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20 - 24 50 - 43

EXTERNALS AND TAGS

OUTPTC - S00100 END - 500200

BLOCK NAMES AND LENGTHS

BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLDCK4 - 3724C04  
BLOCK5 - 27C05 BLOCK6 - 7C06 BLOCK8 - 3726C07

VARIABLE ASSIGNMENTS

AAA - 765C02 AL - 0C04 ALPHAC - 0C06 CONSTR - 1752C04  
FEXP - 0C05 I - 56 NTP1 - 6C01 REFF - 765C07  
SS - 0C02 STRAIN - 765C04 STRESSS- 2737C04 WS - 766C02  
Y - 0C07 YEXP - 12C05 YP - 1752C07 YPITE - 2741C07

START OF CONSTANTS

40

START OF TEMPORARIES

54

START OF INDIRECTS

56

START OF VARIABLES

56

SPACE REQUIRED TO COMPILE -- CONMOV  
32700

CONMOV

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBROUTINE C3OSE (N,INDEX,F)
.....
C THIS SUBROUTINE IS USED WITH THE BINARY TECHNIQUE
C OF MOVEMENT CLOSURE
C .....
6 COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW
6 COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
6 COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
6 COMMON /BLDC28/ Y(501),REFF(501),YP(501),H,ICLOSER,YPITE(501)
6 DIMENSION DIW(501),F(501)
6 INTEGER AAA
6 INDEX=0
6 BAD=1.
10 IF (AAA.EQ.1) GO TO 50
12 DO 20 I=2,N
13 IF (Y(I).EQ.0.) GO TO 10
14 IF (ABS(Y(I)).LT.1.E-06) GO TO 10
20 DIF(I)=(Y(I)-YPITE(I))/Y(I)
23 IF (ABS(DIF(I)).GT.TOL) BAD=BAD+1.
31 CONTINUE
31 20 CONTINUE
34 IF (BAD.GT.1.) GO TO 50
37 INDEX=1
37 AAA=1
40 RETURN
41 CONTINUE
C
41 AAA=AAA+1
43 IF (AAA.GT.MAXITE) GO TO 70
46 MAI=AAA-1
46 DO 60 I=1,N
50 YPITE(I)=Y(I)
60 CONTINUE
54 RETURN
70 CONTINUE
54 PRINT 120
60 PRINT 110, MAI,BAD,AAA
72 PRINT 80
76 PRINT 130, ((I,Y(I),YPITE(I),DIF(I),SS(I),STRESSS(I),STRAIN(I),
1 CONSTR(I),F(I)),I=1,N)
154 80 FORMAT (//,28X,* Y YPITE DIF *,/)
154 110 FORMAT (//,10X,* SOLUTION DID NOT CLOSE FOR ITERATION*,I5,/,
1 10X,*THE NUMBER OF POINTS THAT DID NOT CLOSE ARE*,F10.0,/,
2 1M1,//,10X,* RESULTS FOR ITERATION *,I5,/)
154 120 FORMAT (//,10X,* BAD LUCK, SOLUTION DID NOT CLOSE *,//)
154 130 FORMAT ( 20X,I5,8(2X,E10.3))
154 END

```

CLOSE

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
1217

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	31	20	-	31	50	-	41	70	-	54
80	-	162	110	-	170	120	-	213	130	-	221

EXTERNALS AND TAGS

OUTPTC - S00100    END    -    S00200

BLDCK NAMES AND LENGTHS

BLOCK2 - 1755C01    BLOCK4 - 3724C02    BLOCK6 - 10C03    BLOCK8 - 3726C04

VARIABLE ASSIGNMENTS

AAA	-	765C01	AL	-	0C02	BAD	-	1214	CONSTR	-	1752C02
DIF	-	227	I	-	1215	MAXITE	-	1753C01	MAI	-	1216
REFF	-	765C04	SS	-	0C01	STRAIN	-	765C02	STRESS	-	2737C02
TDL	-	6C03	WS	-	766C01	Y	-	0C04	YP	-	1752C04
YPITE	-	2741C04									

START OF CONSTANTS

155

START OF TEMPDRARIES

224

START OF INDIRECTS

227

START OF VARIABLES

227

SPACE REQUIRED TO COMPILE -- CLOSE

33300

CLOSE

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

3      SUBROUTINE BAKFRIC (F)
3      DIMENSION F(501)
3      COMMON /BLOCK1/  RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
3      COMMON /BLOCK2/  SS(501),AAA,WS(501),MAXITE,CRACKW
3      COMMON /BLOCK3/  XBAR,STRSC,STRSB,STRC,IBABY,ITEB
3      COMMON /BLOCK4/  AL(501),STRAIN(501),CONSTR(501),STRESS(501)
3      COMMON /BLOCK5/  FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
3      COMMON /BLOCK6/  ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
3      COMMON /BLOCK7/  Y(501),REFF(501),YP(501),M,ICLOSEB,YPITE(501)
3      INTEGER AAA
3      IF (FRICMUL.EQ.0.0) RETURN
3      IF (IFY.EQ.1) GO TO 40
3      IF (IFY.EQ.2) GO TO 60
3      DO 30 I=1,NTP1
3      DO 10 J=1,IFY
3      IF (ABS(F(I)).LT.ABS(FEXP(J))) GO TO 20
10     CONTINUE
3      YP(I)=YEXP(IFY)
3      GO TO 30
20     CONTINUE
3      DUMDUM=(FEXP(J)-FEXP(J-1))/(ABS(YEXP(J))-ABS(YEXP(J-1)))
3      YP(I)=ABS(YEXP(J-1))*(ABS(F(I))-FEXP(J-1))/DUMDUM
3      IF (F(I).GT.0) YP(I)=-YP(I)
30     CONTINUE
3      RETURN
40     CONTINUE
3      DO 50 I=1,NTP1
3      YP(I)=F(I)/FRICMUL
3      IF (ABS(F(I)).GE.FU) YP(I)=YEXP(1)
50     CONTINUE
3      RETURN
60     CONTINUE
3      DO 70 I=1,NTP1
3      YP(I)=(F(I)/FRICMUL)**2
3      IF (ABS(F(I)).GE.FU) YP(I)=YEXP(1)
3      IF (F(I).GT.0) YP(I)=-YP(I)
70     CONTINUE
3      RETURN
3      END

```

BAKFRIC

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
121

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20	-	25	30	-	50	40	-	53	50	-	66
60	-	71	70	-	110						

EXTERNALS AND TAGS

END - 500100

BLOCK NAMES AND LENGTHS

BLOCK1 -	12C01	BLOCK2 -	1755C02	BLOCK3 -	6C03	BLOCK4 -	3724C04
BLOCK5 -	30C05	BLOCK6 -	10C06	BLOCK8 -	3726C07		

VARIABLE ASSIGNMENTS

AAA -	765C02	AL -	0C04	CONSTR -	1752C04	DUMDUM -	120
FEXP -	0C05	FRICMUL -	24C05	FU -	26C05	I -	116
IFY -	27C05	J -	117	NTP1 -	6C01	REFF -	765C07
SS -	0C02	STRAIN -	765C04	STRESSS -	2737C04	WS -	766C02
Y -	0C07	YEXP -	12C05	YP -	1752C07	YPITE -	2741C07

START OF CONSTANTS

114

START OF TEMPORARIES

114

START OF INDIRECTS

116

START OF VARIABLES

116

SPACE REQUIRED TO COMPILE -- BAKFRIC

33100

BAKFRIC

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

3      SUBROUTINE BINARYF (F)
3      DIMENSION F (501)
3      COMMON /BLOCK1/  RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
3      COMMON /BLOC22/  SS(501),AAA,WS(501),MAXITE,CRACKW
3      COMMON /BLOCK3/  XBAR,STRSC,STRSB,STRC,IBABY,ITEB
3      COMMON /BLOCK4/  AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
3      COMMON /BLOCK5/  FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
3      COMMON /BLOC26/  ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
3      COMMON /BLOCK8/  Y(501),REFF(501),YP(501),H,ICLOSER,YPITE(501)
3      COMMON /BLOC29/  STX,STY,PSX,PSY,ITE
3      DO 30 I=1,NTP1
5          IF (YP(I)+GT.Y(I)) GO TO 10
11             TEM7=REFF(I)
12             REFW(I)=F(I)
14             F(I)=(3*F(I)-TEMP)/2.
21             GO TO 20
10          CONTINUE
21             F(I)=(REFF(I)+F(I))/2.
25          CONTINUE
25          CONTINUE
30          RETURN
30          END

```

BINARYF

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
36

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10 - 21 20 - 25 30 - 25

EXTERNALS AND TAGS

END - S00100

BLOCK NAMES AND LENGTHS

BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04  
BLOCK5 - 30C05 BLOCK6 - 10C06 BLOCK8 - 3726C07 BLOCK9 - 5C10

VARIABLE ASSIGNMENTS

AL - 0C04 CONSTR - 1752C04 FEXP - 0C05 I - 34  
NTP1 - 6C01 REFF - 765C07 SS - 0C02 STRAIN - 765C04  
STRESS - 2737C04 TEMP - 35 WS - 766C02 Y - 0C07  
YEXP - 12C05 YP - 1752C07 YPITE - 2741C07

START OF CONSTANTS

31

START OF TEMPORARIES

33

START OF INDIRECTS

34

START OF VARIABLES

34

SPACE REQUIRED TO COMPILE -- BINARYF

32600

BINARYF

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBROUTINE DWBARF (F,BONDL,STRMAX,Z,DELTA)

C  
C \*\*\*\*\*  
C THIS SUBROUTINE SOLVES FOR THE STRESS IN THE STEEL AT THE CRAC  
C AND BETWEEN CRACKS. IT IS USED IN THE CASE OF DEFORMED BARS S  
C THE DEVELOPMENT LENGTH CRITERIA OR BOUNDARY CONDITION IS IMPOS  
C IN THE SOLUTION OF THE BASIC EQUATIONS.  
C \*\*\*\*\*  
C

10 DIMENSION F(S01),SUM(S01)

10 COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT

10 COMMON /BLOC22/ SS(S01),AAA,WS(S01),MAXITE,CRACKW

10 COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB

10 COMMON /BLOCK4/ AL(S01),STRAIN(S01),CONSTR(S01),STRESS(S01)

10 COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY

10 COMMON /BLOC26/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER

10 COMMON /BLOC28/ Y(S01),REFF(S01),YP(S01),H,CLOSEB,YPITE(S01)

10 COMMON /BLOC27/ SIGHASC,SIGHASB,NA,NAP1,E,A,S,DENO,NAP2

10 COMMON /BLOC214/ IFINISH

10 INTEGER AAA

10 REAL L

10 ICL6SEB=0

11 A=A3(NTP1)-BONDL

13 IF (A.LE.0.) GO TO 30

14 NA=A/N+1\*EP

21 E=A-AL(NA)

23 IF (NA.GT.NT) GO TO S0

26 NAP1=NA+1

27 NAP2=NA+2

30 NAM1=NA-1

31 DENG=THICK\*(P+1./RATIO)

35 SLOTE(I) = - F(I) / DENO

36 SUM1=0.

37 SUM2=0.

40 DO 10 I=1,NAM1

44 SUM1=SUM1+(2\*NA-(2.\*I+1))\*(-F(I))/DENO

54 SUM2=SUM2+(-F(I))/DENO

60 CONTINUE

C  
C DEFINE CONSTANTS

62 S=-W(NAP1)/OENO

64 BONDCON=DIA/(4.\*U)

67 ANA=NA

70 C1=1.+1./RATIO/P

74 C2=EC\*(Z+DELTA\*(ALPHAC-ALPHAS))/P

101 C3=FF/(P\*THICK)

103 C4=C2-C3

105 C5=H\*SUM2\*S

110 C6=H\*H\*SUM1/2.

113 C7=(ANA-1.)\*H

115 C8=H\*SUM2\*E+S\*E\*E/2.

121 C9=-C4/C1+C5

C  
C DEFINE QUADRATIC EQUATION CONSTANTS

C

DFBARF



RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

124      AA=BONDCON*(1.-1./(C1*C1))/2.
130      BB=(C7+E)/C1-BONCON*C9/C1
135      CC=KALPHAS*AL(NTP1)*DELTAT*ES-C4*(C7+E)/C1+C6+C8-BONDCON*C9*C9/2.
C
152      DELTA=BB*BB-4.*AA*CC
156      IF (DELTA<LT,0.) GO TO 60
C
157      ROOT1=(-BB-SQRT(DELTA))/(2.*AA)
165      ROOT2=(-BB+SQRT(DELTA))/(2.*AA)
173      IF (ROOT2.GT,0.) GO TO 40
201      SIGMASC=ROOT1
202      SIGMASB=(SIGMASC-C4)/C1
205      BONDLC=(SIGMASC-(SIGMASB+C5))*BONDCON
211      201 FORMAT(10X,*BONDLC = *E10.3,/,10X,*SIGMASC = *E10.3,/,
1          10X,*SIGMASB = *E10.3,/,10X,*C5 = *E10.3,/,
2          10X,*SDNDCON = *E10.3,/)
211      DUM=(BONDLC-BOND1)/BONDLC
213      IF (ABS(DUM).LE.TOL) ICLOSEB=1
220      IF (ICLOSEB.EQ,1) ITEB=0
223      ITES=ITEB+1
225      IF (ITES.XT,MAXITE) GO TO 20
230      BOND1=BONDLC
230      202 FORMAT(10X,*BOND1 IN DFBARF =*E10.3,/)
C
C      COMPUTE AREAS FOR SUMMATION CHECK
C
230      A1=H*((2.*ANA-2.)*SIGMASB+H*SUM1)/2.
237      A2=SIGMASB*E+H*SUM2*E+5*E*E/2.
245      A3=(SIGMASB+C5*SIGMASC)*BOND1/2.
252      A4=A1+A2+A3
C
255      DUM2=ALPHAS*AL(NTP1)*DELTAT*ES
260      IF (ABS(A4-DUM2).GT,1.E-5) GO TO 70
265      CALL POIRES (F,BOND1,STRMAX,LOCMAX,Z,DELTAT)
270      RETURN
271      20 CONTINUE
271      PRINT 90, ITEB
277      GO TO 80
303      30 CONTINUE
303      PRINT 100, A
311      GO TO 80
315      40 CONTINUE
315      PRINT 110, DELTA,ROOT1,ROOT2
327      GO TO 80
333      50 CONTINUE
333      PRINT 120, NA,NT
343      GO TO 80
347      60 CONTINUE
347      PRINT 130, DELTA
355      70 CONTINUE
355      PRINT 140, DUM2,A4
365      80 CONTINUE
365      90 FORMAT (/,10X,* SOLUTION DID NOT CLOSE BY ITERATING ON BOND *,
1          *LENGTH IN SUBROUTINE DFBARF*,/,10X,*PROGRAM IS TERMINATED*,
2          /,10X,* ITEB=*,[5])
365      100 FORMAT (/,10X,*ERROR IS DETECTED IN DFBARF*,/,

```

DFBARF

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

365      110 FORMAT (/,10X,*DELTA=*E10.3,/,
1          10X,*ROOT1=*E10.3,/,
2          10X,*ROOT2=*E10.3,/,
3          10X,* ERROR IS DETECTED IN SUBROUTINE DFBARF,ROOT2 IS POS.*/)
365      120 FORMAT (/,20X,* ERROR IS DETECTED *,/,
1          10X,* NA = *,[5],10X,* NT = *,[5])
365      130 FORMAT (/,10X,*ERROR IS DETECTED*,/,
1          10X,* DELTA IS NEGATIVE AND=*E10.3)
365      140 FORMAT (/,10X,* ERROR IS DETECTED IN SUBROUTINE DFBARF*,/,
1          10X,* DUM2 IS NOT EQUAL TO A4*,/,
2          10X,* DUM2=*E10.3,5X,* A4=*E10.3)
365      END

```

DFBARF

SUBPROGRAM LENGTH  
1613

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20	-	271	30	-	303	40	-	315	50	-	333
60	-	347	70	-	355	80	-	365	90	-	423
100	-	443	110	-	456	120	-	511	130	-	525
140	-	541	201	-	373	202	-	414			

EXTERNALS AND TAGS

SQRT	-	S00100	POIRES	-	S00200	OUTPTC	-	S00300	ENO	-	S00400
------	---	--------	--------	---	--------	--------	---	--------	-----	---	--------

BLOCK NAMES AND LENGTHS

BLOCK1	-	12C01	BLOCK2	-	1755C02	BLOCK3	-	6C03	BLOCK4	-	3724C04
BLOCK5	-	30C05	BLOCK6	-	10C06	BLOCK8	-	3726C07	BLOCK7	-	11C10
BLOCK14	-	1C11									

VARIABLE ASSIGNMENTS

A	-	5C10	AA	-	1575	AAA	-	765C02	AAAA	-	1610
AL	-	0C04	ALPHAC	-	0C06	ALPHAS	-	1C06	ANA	-	1563
A1	-	1605	A2	-	1606	A3	-	1607	BB	-	1576
BONOCON	-	1562	BONDLC	-	1603	CC	-	1577	CONSTR	-	1752C04
C1	-	1564	C2	-	1565	C3	-	1566	C4	-	1567
C5	-	1570	C6	-	1571	C7	-	1572	C8	-	1573
C9	-	1574	DELTA	-	1600	OENO	-	7C10	OIA	-	10C01
DUM	-	1604	DUMZ	-	1611	E	-	4C10	EC	-	2C06
EP	-	5C06	ES	-	5C01	FEXP	-	0C05	FF	-	3C01
H	-	2737C07	I	-	1561	ICLOSEB	-	2740C07	ITEB	-	5C03
L	-	1555	LOCMA	-	1612	MAXITE	-	1753C02	NA	-	2C10
NAM1	-	1556	NAP1	-	3C10	NAP2	-	10C10	NT	-	25C05
NTP1	-	6C01	P	-	2C01	RATIO	-	0C01	REFF	-	765C07
ROOT1	-	1601	ROOT2	-	1602	S	-	6C10	SIGMASB	-	1C10
SIGMASC	-	0C10	SS	-	0C02	STRAIN	-	765C04	STRESSS	-	2737C04
SUM	-	570	SUM1	-	1557	SUM2	-	1560	THICK	-	1C01
TOL	-	6C06	U	-	7C01	WS	-	766C02	Y	-	1C01
YEXP	-	12C05	YP	-	1752C07	YPITE	-	2741C07			

START OF CONSTANTS

366

START OF TEMPORARIES

562

START OF INOIRECTS

570

START OF VARIABLES

570

SPACE REQUIRED TO COMPILE -- OFBARF

34600

OFBARF

SUBROUTINE OWBAR (BOND,STRMAX,Z,DELTAT)

C THIS SUBROUTINE COMPUTES THE STRESSES AND STRAINS IN THE CONCRETE  
C STEEL DUE TO A TEMPERATURE DROP AND/OR SHRINKAGE .  
C THE EQUATIONS ARE WRITTEN FOR A FRICTIONLESS SYSTEM  
C

COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT  
COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW  
COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB  
COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESS(501)  
COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY  
COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER  
COMMON /BLOC7C/ STRSC1(501),STRSS1(501),INC,PRF,FY,L  
COMMON /BLOC28/ Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)  
COMMON /BLOC20/ STRSC2(501),DIST  
INTEGER AAA  
REAL L,L2  
L2=L\*2.

IF (Z.LT.0.OR.OELTAT.LT.0.) GO TO 40

COMPUTE CONSTANTS

C1=(RATIO\*P)/(1.-RATIO\*P)  
C2=(ES\*Z)/(1.-RATIO\*P)  
C3=(1.-C1)\*OIA/(4.\*U)  
C4=C2\*DIA/(4.\*U)  
AA=C3-C1\*C3  
BB=L2\*C1-C1\*C4+C2\*C3+C4  
DD=-ES\*L2\*DELTAT\*ALPHAS-L2\*C2-C2\*C4  
DELTA=BB\*BB-4.\*AA\*DD  
IF (DELTA.LT.0.) GO TO 90

C STRSC= STRESS IN THE STEEL AT THE CRACK  
C STRSB= STRESS IN THE STEEL BETWEEN CRACKS  
C STRC= STRESS IN CONCRETE  
C

STRSC=(-BB\*(DELTA\*\*0.5))/(2.\*AA)  
STRSB=C1\*STRSC-C2  
STRT=STRSB/RATIO\*EC\*Z  
B=(STRSC-STRSB)\*OIA/(4.\*U)  
IF (B.LE.0.) GO TO 30  
CHE=(L2-2.\*B)\*STRSB+(STRSC+STRSB)\*B  
CMETK=CHE-ES\*L2\*DELTAT\*ALPHAS  
IF (ABS(CHECK).GT.1.E-2) GO TO 70

C \* CHECKING THE SOLUTION BY SOLVING FOR CONCRETE STRESS FIRST

C11=OIA/(4.\*U\*P)  
C12=2.\*L2\*RATIO/2.  
C13=2.\*L2\*ES\*Z/2.  
C14=2.\*ALPHAS\*L2\*ES\*DELTAT/2.  
DEL=C12\*C12+4.\*C11\*(C13-C14)  
CONCRE=(C12\*SQRT(DEL))/(2.\*C11)  
R2=(-BB-SQRT(DELTA))/(2.\*AA)  
R4=C1\*R2-C2  
R6=R4/RATIO\*EC\*Z

OFBAR

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
167      IF (R6.GT.0) GO TO 50
171      IF (R2.GT.0) GO TO 50
173  10  CONTINUE
173      IF (ABS(STRC-CONCRE).GT.1.E-7) GO TO 80
C
C      * END OF ASOVE CHECK
C
201  20  CONTINUE
C
C      COMPUTE AREA UNDER STEEL STRAIN DIAGRAM FOR THE ASSUMED
C      FRICTIONLESS SYSTEM
C
201      DUM1=L-B
203      STRAREA=DUM1*STRSB/ES+(STRSB*STRSC)*B/(2.*ES)
214      IF (ABS(STRAREA-ALPHAS*DELTAT*L).GT.1.E-7) GO TO 100
223      STRMAX=STRC
C
224      STRAINC=STRC/EC
225      BONDL=B
226      RETURN
226  30  CONTINUE
226      PRINT 140, B
234      GO TO 110
237  40  CONTINUE
237      PRINT 150, Z,DELTAT
247      GO TO 110
252  50  CONTINUE
252      PRINT 160, R2,R4,R6
264      GO TO 110
267  70  CONTINUE
267      PRINT 120, P,DELTAT,Z,XBAR,STRSC,STRSB,STRC,EC,B
315      PRINT 180, CHECK
323      GO TO 110
326  80  CONTINUE
326      PRINT 120, P,DELTAT,Z,XBAR,STRSC,STRSB,STRC,EC,B
354      PRINT 190
360      GO TO 110
363  90  CONTINUE
363      PRINT 200
C
367  100 CONTINUE
367      PRINT 210
373      PRINT 220, STRAREA
401  110 CONTINUE
401  120 FORMAT (//,10X,* PERCENT REINFORCEMENT      ==*.E10.3,/,
1      10X,* TEMPERATURE DROP                    ==*.E10.3,/,
2      10X,*SHRINKAGE                             ==*.E10.3,/,
3      10X,* CRACK SPACING                       ==*.E10.3,/,
4      10X,* STEEL STRESS AT CRACK                ==*.E10.3,/,
5      10X,* STEEL STRESS BETWEEN CRACKS         ==*.E10.3,/,
6      10X,* CONCRETE STRESS                     ==*.E10.3,/,
7      10X,*CONCRETE MODULUS                     ==*.E10.3,/,
8      10X,* DEVELOPMENT LENGTH                   ==*.E10.3,/)
401  140 FORMAT(//,10X,*ERROR IS DETECTED IN SUBROUTINE DFBAR*,/,
1      10X,*BOND LENGTH IS NEGATIVE AND==*.E10.3,/,
2      10X,*PROGRAM IS TERMINATED*)
```

DFBAR

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
401  150 FORMAT (//,10X,* ERROR IS DETECTED IN SUBROUTINE TEMPSHR *,
1      10X,*      Z = *.E10.3,/,
2      10X,* DELTAT = *.E10.3)
401  160 FORMAT (//,10X,*ERROR IS DETECTED IN SUBROUTINE TEMPSHR *
1      10X,* STEEL STRESS AT CRACK              ==*.E10.3,/,
2      10X,* STEEL STRESS BETWEEN CRACK        ==*.E10.3,/,
3      10X,* CONCRETE STRESS                   ==*.E10.3)
401  180 FORMAT (//, 10X,* ROOTS DO NOT SATISFY EQUATION 1 *,/, 10X,
1      1 * CHECK= *. E10.3)
401  190 FORMAT (//,10X,* SOLUTION ONE DOES NOT MATCH SOLUTION TWO *)
401  200 FORMAT (//,30X,*DELTA IS NEGATIVE*)
401  210 FORMAT (//,10X,*SOMETHING IS WRONG, THE AREA UNDER STEEL STRAIN DI
1      AGRAM IS NOT EQUAL TO ALPHAS X DELTAT X XBAR / 2*,/)
401  220 FORMAT (//,10X,* AREA UNDER STEEL STRAIN DIAGRAM FOR FRICTIONLESS
1      ISLAB = *.E10.3,/)
401      END
```

DFBAR

SUBPROGRAM LENGTH  
713

FUNCTION ASSIGNMENTS

STATEMENT	ASSIGNMENTS								
10	- 173	20	-	201	30	-	226	40	- 237
50	- 252	70	-	267	80	-	326	90	- 363
100	- 367	110	-	401	120	-	413	140	- 506
150	- 530	160	-	551	180	-	603	190	- 614
200	- 623	210	-	627	220	-	644		

EXTERNALS AND TAGS  
RBAREX - S00100 SQRT - S00200 OUTPTC - S00300 END - S00400

BLOCK NAMES AND LENGTHS

BLOCK1 -	12C01	BLOCK2 -	175C02	BLOCK3 -	6C03	BLOCK4 -	3724C04
BLOCK5 -	30C05	BLOCK6 -	10C06	BLOCKC -	1756C07	BLOCKB -	3726C10
BLOCKD -	766C11						

VARIABLE ASSIGNMENTS

AA -	671	AAA -	765C02	AL -	0C04	ALPHA5 -	1C06
B -	675	BB -	672	CHE -	676	CHECK -	677
CONCRES -	705	CONSTR -	1752C04	C1 -	665	C11 -	700
C12 -	701	C13 -	702	C14 -	703	C2 -	666
C3 -	667	C4 -	670	00 -	673	DEL -	704
DELTA -	674	DIA -	10C01	DUM1 -	711	EC -	2C06
ES -	5C01	FEXP -	0C05	L -	1755C07	L2 -	664
P -	2C01	RATIO -	0C01	REFF -	765C10	R2 -	706
R4 -	707	R6 -	710	S5 -	0C02	STRAIN -	765C04
STRAIN -	4C01	STRAREA -	712	STRC -	3C03	STRESS5 -	2737C04
STRSR -	2C03	STRSC -	1C03	STRSC1 -	0C07	STRSC2 -	0C11
STRSS1 -	765C07	U -	7C01	WS -	766C02	XBAR -	0C03
Y -	0C10	YEXP -	12C05	YP -	1752C10	YPLTE -	2741C10

START OF CONSTANTS  
402

START OF TEMPORARIES  
654

START OF INDIRECTS  
664

START OF VARIABLES  
664

SPACE REQUIRED TO COMPILE -- OFBAR  
34700

DFBAR

```

SUBROUTINE GETME (X1,Y1,X2,Y2,FOUT)
*****
THIS SUBROUTINE SOLVES FOR THE POINT OF INTERSECTION OF TWO ST
LINES , WHERE ONE OF THE LINES IS Y=X .
THIS VERSION OF THE PROGRAM JOINS THE NEW POINT TO THE POINT
ON THE OTHER SIDE OF THE Y=X LINE .
*****
PSX AND PSY ARE STORED VALUES
BELOW THE EQUALITY LINE
STX AND STY ARE STORED VALUES
ABOVE THE EQUALITY LINE
COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRAKWX
COMMON /BLOCK9/ STX,STY,PSX,PSY,ITE
IF (ITE.EQ.2) GO TO 10
IF (X2-Y2) 40,40,20
10 CONTINUE
DUMX2=PSX=X1
DUMY2=PSY=Y1
GO TO 30
20 CONTINUE
DUMX2=PSX
DUMY2=PSY
30 CONTINUE
DUMX1=STX=X2
DUMY1=STY=Y2
GO TO 50
40 CONTINUE
DUMX1=STX
DUMY1=STY
DUMX2=PSX=X2
DUMY2=PSY=Y2
50 CONTINUE
FOUT=(DUMX2*DUMY1-DUMX1*DUMY2)/((DUMX2-DUMX1)-(DUMY2-DUMY1))
RETURN
END
    
```

GETME

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
55

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	14	20	-	20	30	-	23	40	-	27
50	-	35									

EXTERNALS AND TAGS

END - S00100

BLOCK NAMES AND LENGTHS

BLOCK2 - 1755C01 BLOCK9 - 5C02

VARIABLE ASSIGNMENTS

DUMX1	-	53	DUMX2	-	51	DUMY1	-	54	DUMY2	-	52
ITE	-	4C02	PSX	-	2C02	PSY	-	3C02	SS	-	0C01
STX	-	0C02	STY	-	1C02	WS	-	766C01			

START OF CONSTANTS

46

START OF TEMPORARIES

46

START OF INDIRECTS

51

START OF VARIABLES

51

SPACE REQUIRED TO COMPILE -- GETME

32600

GETME

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBROUTINE FRIC (F)
DIMENSION F(501)
COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
COMMON /BLOCK2/ SS(501),AAA,WS(501),MAXITE,CRACKW
COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
COMMON /BLOCK6/ ALPHAC,ALPHAS,EC,FPC,TINE,EP,TOL,ITYPER
COMMON /BLOCK8/ Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
INTEGER AAA

C
      BEYOND=0.
      IF (IFY.EQ.1) GO TO 10
      IF (IFY.EQ.2) GO TO 40
      IF (IFY.GT.2) GO TO 90
11 10 CONTINUE
      SLOTE=FRICMUL
C
      COMPUTE FRICTION FORCES FROM STRAIT LINE GRAPH
C
      DO 30 I=1,NTP1
13         F(I)=Y(I)*SLOPE
14         IF (ABS(F(I)).LE.FU) GO TO 20
17         IF (F(I).GT.0.0) F(I)=FU
23         IF (F(I).LT.0.0) F(I)=-FU
27
33 20 CONTINUE
33 30 CONTINUE
36         GO TO 140
36 40 CONTINUE
C
      COMPUTE FRICTION FORCES FROM PARABOLA
C
      DO 80 I=1,NTP1
36
C
      IF (Y(I).XT.0.) GO TO 50
      F(I)=FRICMUL*SQRT(ABS(Y(I)))
52         GO TO 60
52 50 CONTINUE
52         F(I)=-FRICMUL*SQRT(Y(I))
61 60 CONTINUE
61         IF (ABS(F(I)).LE.FU) GO TO 70
66         IF (F(I).GT.0.0) F(I)=FU
71         IF (F(I).LT.0.0) F(I)=-FU
75 70 CONTINUE
75 80 CONTINUE
100        GO TO 140
100 90 CONTINUE
C
      COMPUTE FRICTION FORCES FROM INPUT POINT CURVE
      DO 130 I=1,NTP1
102        DO 100 J=1,IWY
103        IF (ABS(Y(I)).LT.ABS(YEXP(J))) GO TO 110
110 100 CONTINUE
113        BEYOND=BEYOND+1.
115        F(I)=FEXP(IFY)
116        GO TO 120

```

FRIC

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

117 110 CONTINUE
117      DUMDUM=(FEXP(J)-FEXP(J-1))/(ABS(YEXP(J))-ABS(YEXP(J-1)))
126      F(I)=FEXP(J-1)+DUMDUM*(ABS(Y(I))-ABS(YEXP(J-1)))
137 120 CONTINUE
137      IF (Y(I).GT.0.0) F(I)=-F(I)
143 130 CONTINUE
C
C      COMPUTE THE TOTAL FRICTION FORCE
C
146 140 CONTINUE
146      IF (BEYOND.GT.0.) PRINT 199, BEYOND
156      FF=0
157      DO 150 I=1,NT+2
161          FF=FF+(F(I)+4.*F(I+1)+F(I+2))*H/3.
170 150 CONTINUE
173      IF (LONG7R.NE.100) RETURN
175      PRINT 200, FW
203      RETURN
204 190 FORMAT (//,10X,*IN COMPUTING THE FRICTION FORCES FROM MOVEMENTS*,/
1, 10X,F5.0,* POINTS EXCEEDED THE MAX MOV ON F-Y CURVE*)
204 200 FORMAT (/,10X,* TOTAL FRICTION FORCE FROM FRIC =*,E10.3)
204      END

```

FRIC

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBPROGRAM LENGTH
245

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS
10 - 11 20 - 33 30 - 33 40 - 36
50 - 52 60 - 61 70 - 75 80 - 75
90 - 100 110 - 117 120 - 137 130 - 143
140 - 146 190 - 212 200 - 227

EXTERNALS AND TAGS
SORT - S00100 OUTPTC - S00200 END - S00300

BLOCK NAMES AND LENGTHS
BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04
BLOCK5 - 30C05 BLOCK6 - 10C06 BLDCK8 - 3726C07

VARIABLE ASSIGNMENTS
AAA - 765C02 AL - 0C04 BEYOND - 237 CONSTR - 1752C04
DUMDUM - 243 FEXP - 0C05 FF - 3C01 FRICMUL - 24C05
FU - 26C05 H - 2737C07 I - 241 IFY - 27C05
J - 242 LONGPR - 244 NT - 25C05 NTP1 - 6C01
REFF - 765C07 SLOPE - 240 SS - 0C02 STRAIN - 765C04
STRESSS - 2737C04 WS - 766C02 Y - 0C07 YEXP - 12C05
YP - 1752C07 YPITE - 2741C07

START OF CONSTANTS
205

START OF TEMPORARIES
234

START OF INDIRECTS
237

START OF VARIABLES
237

SPACE REQUIRED TO COMPILE -- FRIC
33500

```

FRIC



RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
1374

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

10	-	27	40	-	210	50	-	211	60	-	223
70	-	237	80	-	255	130	-	264	140	-	277
150	-	313									

EXTERNALS AND TAGS

POIRES - 500100    OUTPTC - 500200    END - 500300

BLOCK NAMES AND LENGTHS

BLOCK1 -	12C01	BLOCK2 -	1755C02	BLOCK3 -	6C03	BLOCK4 -	3724C04
BLOCK5 -	30C05	BLOCK6 -	10C06	BLOCK7 -	11C07	BLOCK8 -	3726C10

VARIABLE ASSIGNMENTS

A	-	5C07	AAA	-	765C02	AL	-	0C04	ALPHAC	-	0C06
ALPHAS	-	1C06	ANA	-	1365	A1	-	1367	A2	-	1370
A3	-	1371	CONSTR	-	1752C04	C1	-	1361	C2	-	1362
C3	-	1363	DENO	-	7C07	DUM1	-	1364	DUM2	-	1366
DUM3	-	1372	E	-	4C07	EC	-	2C06	EP	-	5C06
ES	-	5C01	FEXP	-	0C05	FF	-	3C01	H	-	2737C10
I	-	1360	L	-	1353	LOCMAX	-	1373	NA	-	2C07
NAM1	-	1354	NAM2	-	1355	NAP1	-	3C07	NAP2	-	10C07
NT	-	25C05	NTP1	-	6C01	P	-	2C01	RATIO	-	0C01
REFF	-	765C10	S	-	6C07	SIGMASB	-	1C07	SIGMASC	-	0C07
SS	-	0C02	STRAIN	-	765C04	STRESSS	-	2737C04	SUM	-	366
SUM1	-	1356	SUM2	-	1357	THICK	-	1C01	WS	-	766C02
Y	-	0C10	YEXP	-	12C05	YP	-	1752C10	YP1TE	-	2741C10

START OF CONSTANTS

256

START OF TEMPORARIES

361

START OF INDIRECTS

366

START OF VARIABLES

366

SPACE REQUIRED TO COMPILE -- DFWIREF

34100

DFWIREF

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

* C SUBROUTINE DFWIRE (BOND,STRMAX,Z,DELTA)
* C *****
* C THIS SUBROUTINE SOLVES FOR THE STRESS IN THE STEEL AND
* C CONCRETE FOR DEFORMED WIRE FABRIC -NO FRICTION FORCES
* C ARE CONSIDERED IN THE SOLUTION
* C *****
* C COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
* C COMMON /BLOC22/ SS(501),AAA,WS(501),MAXITE,CRACKW
* C COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
* C COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESSS(501)
* C COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
* C COMMON /BLOC26/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
* C COMMON /BLOC2D/ STRSC(501),DIST
* C COMMON /BLOC27/ SIGMASC,SIGMASB,NA,NAP1,E,A,S,DENO,NAP2
* C COMMON /BLOC28/ Y(501),REFF(501),YP(501),H,ICLOSEB,YP1TE(501)
* C REAL L
* C
* C DEFINE CONSTANTS
* C
* C C1=EC*Z*EC*DELTA*(ALPHAC-ALPHAS)
* C C2=ALPHAS*L*DELTA*ES
* C C3=BOND/(2.*RATIO)*P*L
* C
* C SOLVE FOR STRESSES
* C STRC=(C1*P*L+C2*P/RATIO)/C3
* C STRSB=(-C1*BOND/2.*P*C2)/C3
* C STRSC=(C2/RATIO+C1*(L-BOND/2.)*P*C2)/C3
* C STRMAX=STRC
* C
* C CHECK EQUILISRIUM - EQUATION 1
* C
* C DUM1=STRC*P*STRSB
* C DUM2=P*STRSC
* C IF (ABS(DUM1-DUM2).GT.1.E-5) GO TO 10
* C
* C RETURN
* C
* C CONTINUE
* C PRINT 20, STRC,STRSB,STRSC,DUM1,DUM2
* C
* C 20 FORMAT (//,10X,* ERROR IS DETECTED *,/,
* C 1 10X,* EQUILIBRIUM IS NOT SATISFIED *,/,
* C 2 10X,* STRC = *E10.3,5X,* STRSB = *E10.3,5X,* STRSC =
* C 3 E10.3,/,10X,* DUM1 = *E10.3,5X,* DUM2 = *E10.3)
* C
* C END

```

DFWIRE



RUNW VERSION FEB 74 16.51.06. 23 JUL 75

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENXTH  
144

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS  
IO - 55 20 - 101

EXTERNALS AND TAGS  
OUTPTC - 500100 END - 500200

BLOCK NAMES AND LENGTHS  
BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04  
BLOCK5 - 30C05 BLOCK6 - 10C06 BLOCKD - 766C07 BLOCK7 - 11C10  
BLOCK8 - 3726C11

VARIABLE ASSIGNMENTS  
AL - 0C04 ALPHAC - 0C06 ALPHAS - 1C06 CONSTR - 1752C04  
C1 - 136 C2 - 137 C3 - 140 DUM1 - 141  
DUM2 - 142 EC - 2C06 ES - 5C01 FEXP - 0C05  
L - 135 P - 2C01 RATIO - 0C01 REFF - 765C11  
SRAINC - 143 SS - 0C02 STRAIN - 765C04 STRC - 3C03  
STRESS5 - 2737C04 STRSB - 2C03 STRSC - 1C03 STRSC2 - 0C07  
WS - 766C02 Y - 0C11 YEXP - 12C05 YP - 1752C11  
YPITE - 274IC11

START OF CONSTANTS  
74

START OF TEMPORARIES  
133

START OF INDIRECTS  
135

START OF VARIABLES  
135

SPACE REQUIRED TO COMPILE -- DFWIRE  
33100

```

SUBROUTINE POIRES (F,BONDL,STRMAX,LOCMAX,Z,DELTAT)
DIMENSION F(501),SUM(501)
COMMON /BLOCK1/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
COMMON /BLOC22/ SS(501),AAA,MS(501),MAXITE,CRACKW
COMMON /BLOCK3/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
COMMON /BLOCK4/ AL(501),STRAIN(501),CONSTR(501),STRESS5(501)
COMMON /BLOCK5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
COMMON /BLOC26/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
COMMON /BLOC7/ SIGMASC,SIGMASB,NA,NAP1,E,A,S,DENO,NAP2
COMMON /BLOC28/ Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
INTEGER AAA
REAL L
C
II=NAP2
SUM3=0.
SUM4=0.
STRESS5(1)=SIGMASB
SS(1)=STRESS5(1)/ES
STRAIN(1)=SS(1)*Z*DELTAT*(ALPHAC-ALPHAS)
CONSTR(1)=STRAIN(1)*EC
LOCMAX=1
STRMAX=CONSTR(1)
C
DO 20 I=2,NA
STRESS5(I)=STRESS5(I-1)*H*(-F(I)/DENO)
SS(I)=STRESS5(I)/ES
STRAIN(I)=SS(I)*Z*DELTAT*(ALPHAC-ALPHAS)
CONSTR(I)=STRAIN(I)*EC
IF (CONSTR(I).LT.STRMAX) GO TO 10
STRMAX=CONSTR(I)
LOCMAX=I
10 CONTINUE
SUM3=SUM3+(SS(I)+SS(I-1))*H/2.
SUM4=SUM4+(STRESS5(I)+STRESS5(I-1))*H/2.
20 CONTINUE
ADDI=STRESS5(NA)*S*E
ADDIAR=(STRESS5(NA)+ADDI)*E/2.
SUM3=SUM3+(ADDIAR)/ES
SUM4=SUM4+ADDIAR
SLO7E2=(SIGMASC-ADDI)/BONDL
ADDIC=ADDI/ES*Z*DELTAT*(ALPHAC-ALPHAS)
SLO7ECC=-ADDI/BONDL
STRESS5(NAP1)=ADDI*(AL(NAP1)-A)*SLOPE2
SS(NAP1)=STRESS5(NAP1)/ES
STRAIN(NAP1)=ADDIC-F(NAP1)*H/(THICK*EC)-(STRESS5(NAP1)+ADDI)*P/EC
CONSTR(NAP1)=STRAIN(NAP1)*EC
IF (CONSTR(NAP1).LT.STRMAX) GO TO 30
STRMAX=CONSTR(NAP1)
LOCMAX=NAP1
30 CONTINUE
SUM4=SUM4+(STRESS5(NAP1)+ADDI)*(AL(NAP1)-A)/2.
SUM3=SUM3+(STRESS5(NAP1)+ADDI)*(AL(NAP1)-A)/(2.*ES)
IF (NA.EQ.NT) I1=NAP1
DO 50 I=I1,NTP1
STRESS5(I)=ADDI*(AL(I)-A)*SLOPE2

```

DFWIRE

POIRES

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
205          SS(I)=STRESSS(I)/ES
210          STRAIN(I)=STRAIN(I-1)-F(I)*H/(THICK*EC)-(STRESSS(I)-STRESSS(I-1))*
1            P/EC
224          CONSTR(I)=STRAIN(I)*EC
227          IF (CONSTR(I).LT,STRMAX) GO TO 40
231          STRMAX=CONSTR(I)
232          LOCMAX=I
233 40        CONTINUE
233          SUM3=SUM3+(SS(I)+SS(I-1))*H/2.
241          SUM4=SUM4+(STRESSS(I)+STRESSS(I-1))*H/2.
247 50        CONTINUE
251          RETURN
252          END
```

POIRES

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
SUBPROGRAM LENGTH
1267

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS
10 - 54 30 - 150 40 - 233

EXTERNALS AND TAGS
END - 500100

BLOCK NAMES AND LENGTHS
BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04
BLOCK5 - 30C05 BLOCK6 - 10C06 BLOCK7 - 11C07 BLOCK8 - 3726C10

VARIABLE ASSIGNMENTS
A - 5C07 AAA - 765C02 ADDI - 1262 ADDIAR - 1263
ADDIC - 1265 AL - 0C04 ALPHAC - 0C06 ALPHAS - 1C06
CONSTR - 1752C04 DENO - 7C07 E - 4C07 EC - 2C06
ES - 5C01 FEXP - 0C05 H - 2737C10 I - 1261
II - 1256 L - 1255 NA - 2C07 NAP1 - 3C07
NAP2 - 10C07 NT - 25C05 NTP1 - 6C01 P - 2C01
REFF - 765C10 S - 6C07 SIGMASB - 1C07 SIGMASC - 0C07
SLOPECC - 1266 SLOPE2 - 1264 SS - 0C02 STRAIN - 765C04
STRESSS - 2737C04 SUM - 270 SUM3 - 1257 SUM4 - 1260
THICK - 1C01 WS - 766C02 Y - 0C10 YEXP - 12C05
YP - 1752C10 YPITE - 2741C10

START OF CONSTANTS
253

START OF TEMPORARIES
255

START OF INDIRECTS
264

START OF VARIABLES
270

SPACE REQUIRED TO COMPILE -- POIRES
34000
```

POIRES

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

7      SUBROUTINE SIMPSPE (Y,N,H,SUM)
      DIMENSION Y(N),SUM(N)
      C
      C      THIS SUBROUTINE COMPUTES THE AREA UNDER A DISTRIBUTION USING
      C      SIMPSONS RULE WITH A SPECIAL MODIFICATION
      C
7      DO 10 I=1,N
10     SUM(I)=0.
14     CONTINUE
15     SUM(1)=0.
16     A1=(Y(1)+Y(2))*H/2.
20     AOLD=A1
20     SUM(2)=AOLD
21     NM1=N-1
      C
23     DO 20 I=2,NM1
24     AS=(Y(I-1)+4.*Y(I)+Y(I+1))*H/3
33     A=AS-AOLD
35     SUM(I+1)=SUM(I)+A
40     AOLD=A
41     CONTINUE
44     RETURN
44     END

```

SIMPSPE

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```

SUBPROGRAM LENGTH
57

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

EXTERNALS AND TAGS
END - S00100

BLOCK NAMES AND LENGTHS

VARIABLE ASSIGNMENTS
A - 56 AOLD - 53 AS - 55 A1 - 52
I - 51 NM1 - 54

START OF CONSTANTS
45

START OF TEMPORARIES
47

START OF INDIRECTS
51

START OF VARIABLES
51

SPACE REQUIRED TO COMPILE -- SIMPSPE
32500

```

SIMPSPE

```

SUBROUTINE STRGENE (BONDL)
*****
C      THIS SUBROUTINE GENERATES THE STRAIN IN THE CONCRETE AT
C      EVERY STATION IN THE FRICTIONLESS SLAB .
C      RESULTS OF SUBROUTINE TEMPSHR ARE USED -( NO FRICTION )
C      *****
3      COMMON /BLOCK1/  RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
3      COMMON /BLOC22/  S5(501),AAA,WS(501),MAXITE,CRACKW
3      COMMON /BLOCK3/  XBAR,STRSC,STRSB,STRC,IBABY,ITEB
3      COMMON /BLOCK4/  AL(501),STRAIN(501),CONSTR(501),STRESS5(501)
3      COMMON /BLOCK5/  FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
3      COMMON /BLOC26/  ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
3      COMMON /BLOC28/  Y(501),REFF(501),YP(501),H,ICLOSEB,YPITE(501)
3      COMMON /BLOC2C/  STRSC1(501),STRSS1(501),INC,FRF,FY,L
3      INTEGER AAA
3      REAL L
C
3      A=L-BONOL
5      HH=-H
7      DO 20 I=1,NTP1
C
10         STRAIN(I)=STRAIN
12         AL(I)=HH+H
15         HH=AL(I)
16         IF (AL(I).LE.A) GO TO I0
20         STRAIN(I)=STRAIN-STRAIN*(AL(I)-A)/BONDL
24 10 CONTINUE
24         CONSTR(I)=STRAIN(I)*EC
27 20 CONTINUE
31 RETURN
32 END
    
```

STRGENE

```

SUBPROGRAM LENGTH
37
FUNCTION ASSIGNMENTS
STATEMENT ASSIGNMENTS
10 - 24
EXTERNALS AND TAGS
END - S00100
BLOCK NAMES AND LENGTHS
BLOCK1 - 12C01 BLOCK2 - 1755C02 BLOCK3 - 6C03 BLOCK4 - 3724C04
BLOCK5 - 30C05 BLOCK6 - 10C06 BLOCK8 - 3726C07 BLOCKC - 1756C10
VARIABLE ASSIGNMENTS
A - 34 AAA - 765C02 AL - 0C04 CONSTR - 1752C04
EC - 2C06 FEXP - 0C05 H - 2737C07 HH - 35
I - 36 L - 1755C10 NTP1 - 6C01 REFF - 765C07
SS - 0C02 STRAIN - 765C04 STRAINC - 4C01 STRESS5 - 2737C04
STRSC1 - 0C10 STRSS1 - 765C10 WS - 766C02 Y - 0C07
YEXP - 12C05 YP - 1752C07 YPITE - 2741C07
START OF CONSTANTS
33
START OF TEMPORARIES
33
START OF INDIRECTS
34
START OF VARIABLES
34
SPACE REQUIRED TO COMPILE -- STRGENE
32700
    
```

STRGENE

```

SUBROUTINE BACKTIM (TENSTRN,ZTOT,Z)
*****
C THIS SUBROUTINE CALCULATES THE TIME DEPENDENT VARIABLES FROM
C THE COMPUTED STRENGTH ON THE LINE OF EQUALITY OF STRESS -
C STRENGTH CURVE .
*****
6 DIMENSION PERCENT(8),AGE(8)
6 COMMON /BLOC21/ RATIO,THICK,P,FF,STRAIN,ES,NTP1,U,DIA,UNWT
6 COMMON /BLOC2/ SS(S01),AAA,WS(S01),MAXITE,CRACKW
6 COMMON /BLOC23/ XBAR,STRSC,STRSB,STRC,IBABY,ITEB
6 COMMON /BLOC4/ AL(S01),STRAIN(S01),CONSTR(S01),STRESS(S01)
6 COMMON /BLOC5/ FEXP(10),YEXP(10),FRICMUL,NT,FU,IFY
6 COMMON /BLOC6/ ALPHAC,ALPHAS,EC,FPC,TIME,EP,TOL,ITYPER
6 COMMON /BLOC28/ Y(S01),REFF(S01),YP(S01),H,CLOSEB,YPITE(S01)
6 COMMON /BLOC10/ NSTRN,VDS,AGEU(20),TENSION(20),STRNMUL
6 DATA AGE/0.,3.,5.,7.,14.,21.,28./
6 DATA PERCENT/0.,15.,38.,53.,63.,82.,94.,100./
6 INTEGER AAA
C
C
6 IF (NSTRN.GT.0.) GO TO 30
10 FLESTRN=TENSTRN/STRNMUL
11 COMSTR=(1200.*FLESTRN)/(3000.-3.*FLESTRN)
15 PERTOM=(COMSTR/FPC)*100.
20 EC=33.*(UNWT*1.5)*SQRT(COMSTR)
27 RATIO=ES/EC
30 U=9.5*SQRT(COMSTR)/DIA
35 IF (U.GT.800.) U=800.
42 DO 10 I=1,8
44 J=1
44 IF (PERCOM.LE.PERCENT(I)) GO TO 20
47 CONTINUE
51 PRINT 80, PERCOM
57 GO TO 70
62 20 CONTINUE
62 TIME=(PERCENT(J)-PERCENT(J-1))/(AGE(J)-AGE(J-1))
67 TIME=AGE(J-1)+(PERCOM-PERCENT(J-1))/TIME
73 GO TO 60
73 30 CONTINUE
C
C COMPUTE THE TIME CORRESPONDING
C TO TENSILE STRENGTH
C
73 DO 40 I=1,NSTRN
75 J=1
75 IF (TENSTRN.LE.TENSION(I)) GO TO 50
100 CONTINUE
103 PRINT 90, TENSTRN
110 GO TO 70
113 50 CONTINUE
C
C COMPUTE SLOPE BY LINEAR INTERPOLATION
C
113 TIME=(TENSION(J)-TENSION(J-1))/(AGEU(J)-AGEU(J-1))
120 TIME=AGEU(J-1)+(TENSTRN-TENSION(J-1))/TIME

```

```

C
124 60 CONTINUE
C
124 SHRN=26.*EXP(0.36*VOS)
132 Z=(TIME/(SHRN+TIME))*ZTOT
136 RETURN
137 70 CONTINUE
137 80 FORMAT (//,10X,*ERROR IS DETECTED IN SUBROUTINE BACKTIM.*,/,
1 10X,*THE COMPUTED PERCENT COMPRESSION IS GREATER THAN 1
2E MAXIMUM PERCENT AVAILABLE*.,/,
3 10X,*PERCOM =*E10.3,/,
4 10X,*PROGRAM IS TERMINATED*)
137 90 FORMAT (//,10X,*ERROR IS DETECTED IN SUBROUTINE BACKTIM.*,/,
1 10X,*THE COMPUTED TENSILE STRENGTH IS GREATER THAN THE
2AXIMUM STRENGTH PROVIDED BY THE USER*.,/,
3 10X,*TENSTRN=*E10.3,/,
4 10X,*PROGRAM IS TERMINATED*)
137 END

```

BACKTIM

BACKTIM

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENGTH  
302

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20	-	62	30	-	73	50	-	113	60	-	124
70	-	137	80	-	154	90	-	213			

EXTERNALS AND TAGS

SQRT	-	S00100	RBAREX	-	S00200	OUTPTC	-	S00300	EXP	-	S00400
END	-	S00500									

BLOCK NAMES AND LENGTHS

BLOCK1	-	12C01	BLOCK2	-	1755C02	BLOCK3	-	6C03	BLOCK4	-	3724C04
BLOCK5	-	30C05	BLOCK6	-	10C06	BLOCK8	-	3726C07	BLOCK10	-	53C10

VARIABLE ASSIGNMENTS

AAA	-	765C02	AGE	-	264	AGEU	-	2C10	AL	-	0C04
COMSTR	-	275	CONSTR	-	1752C04	DIA	-	10C01	EC	-	2C06
ES	-	5C01	FEXP	-	0C05	FLESTRN	-	274	FPC	-	3C06
I	-	277	J	-	300	NSTRN	-	0C10	PERCENT	-	254
PERCOM	-	276	RATIO	-	0C01	REFF	-	765C07	SHRN	-	301
SS	-	0C02	STRAIN	-	765C04	STRESSS	-	2737C04	STRNMUL	-	52C10
TENSION	-	26C10	TIME	-	4C06	U	-	7C01	UNWT	-	11C01
VDS	-	1C10	WS	-	766C02	Y	-	0C07	YEXP	-	12C05
YP	-	1752C07	YPITE	-	2741C07						

START OF CONSTANTS

140

START OF TEMPORARIES

251

START OF INDIRECTS

254

START OF VARIABLES

254

SPACE REQUIRED TO COMPILE -- BACKTIM

33500

BACKTIM

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBROUTINE DELTEM1 (TIME,DELTAT)

C  
C  
C  
C

THIS SUBROUTINE RETURNS THE TEMPERATURE DROP AT NON-  
INTEGER TIMES.

```

5 COMMON /BLOCK12/ DT(50),NTEMP,NTIFLAG,UPINC,ODWNINC
5 DO 10 ITIME=1,NTEMP
6 REA3TI=FLOAT(ITIME)
10 IF (REALTI.GT.TIME) GO TO 20
13 CONTINUE
15 PRINT 130, TIME,REALTI
24 STOP 66
26 20 CONTINUE
26 DTIME=TIME-(REALTI-1)
33 IF (DTIME.LEQ.0.1)GOTO 40
34 DELTAT=DT(ITIME)*DTIME
35 RETURN
36 40 DELTAT=DT(ITIME)
40 RETURN
40 130 FORMAT(* ERROR IN DELTEM1 TIME = *,E10.3,*REALTI = *,E10.3)
40 END

```

DELTEM1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBPROGRAM LENXTH  
56

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS

20 - 26 40 - 36 130 - 44

EXTERNALS AND TAGS

OUTPTC - S00100 STOP - S00200 END - S00300

BLOCK NAMES AND LENGTHS

BLOCK12- 66C01

VARIABLE ASSIGNMENTS

DT - 0C01 DTIME - 55 ITIME - 53 NTEMP - 62C01

REALTI - 54

START OF CONSTANTS

41

START OF TEMPORARIES

52

START OF INDIRECTS

53

START OF VARIABLES

53

SPACE REQUIRED TO COMPILE -- DELTEM1

32500

DELTEM1

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

SUBROUTINE DELTEMP (TIME,DELTAT)

```

C *****
C THIS SUBROUTINE CONTAINS THE INCREMENTAL TECHNIQUE
C FOR TEMPERATURE TIME DATA. A SINE WAVE IS FIT
C THROUGH EACH DAY. THE ROUTINE HAS THREE OPTIONS.
C
C DELTEMP INCREMENTS UP BY UPINC IF NTIFLAG = 1
C INCREMENTS DOWN BY DOWNINC IF NTIFLAG = -1
C IT GIVES THE TEMPERATURE DROP AT TIME IF NTIFLAG = 0
C *****
COMMON /BLOCK12/ DT(50),NTEMP,NTIFLAG,UPINC,DOWNINC
PI=3.14159265359
DO 10 ITIME=1,NTEMP
  REALTI=FLOAT(ITIME)
  IF (REALTI.GT.TIME) GO TO 20
10 CONTINUE
  PRINT 130, DELTAT,TIME
  STOP 66
20 CONTINUE
  IF (TIME.GT.REALTI-.75.A.TIME,LT.REALTI-.25) GO TO 30
  DELTAT=0.
  GO TO 40
30 CONTINUE
  DELTAT=DT(ITIME)*SIN((TIME-REALTI+.75)*2.*PI)
40 CONTINUE
  IF (NTIFLAG) 100,80,50
50 CONTINUE
  DELTAT=DELTAT+UPINC
  IF (TIME,LT.REALTI-.5) GO TO 90
  IF (DELTAT.GE.DT(ITIME)+UPINC-1.E-7) GO TO 90
  IF (DELTAT.LE.DT(ITIME)) GO TO 120
60 CONTINUE
  DELTAT=DT(ITIME)
70 CONTINUE
  TIME=REALTI-.5
80 CONTINUE
  RETURN
90 CONTINUE
  REALTI=REALTI+1.
  ITIME=ITIME+1
  DELTAT=DELTAT+UPINC
  IF (ITIME.GT.NTEMP) GO TO 70
  IF (DELTAT.GE.DT(ITIME)) GO TO 60
  GO TO 120
100 CONTINUE
  DELTAT=DELTAT-DOWNINC
  IF (DELTAT) 110,110,120
110 CONTINUE
  DELTAT=0.
  * IF (TIME,LE.REALTI-.5) TIME=REALTI-.75
  IF (TIME.GT.REALTI-.5) TIME=REALTI+.25
  RETURN
120 CONTINUE
  TPLUS=ABS(ASIN(DELTAT/DT(ITIME))/(2.*PI)-.25)
  IF (TIME,LE.REALTI-.5) TPLUS=-TPLUS

```

DELTEMP

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
156          TIME=REALTI+TPLUS=.5
161          RETURN
161 130      FORMAT (* END OF TEMPERATURE ARRAY ENCOUNTERED*,/,* DELTAT =*,F6.3
161          1,* TIME =*,F6.3)
161          END
```

RUNW VERSION FEB 74 16.51.06. 23 JUL 75

```
SUBPROGRAM LENGTH
213

FUNCTION ASSIGNMENTS

STATEMENT ASSIGNMENTS
20  -      30  30  -      46  40  -      57  50  -      61
60  -      76  70  -      100 80  -      102 90  -      103
100 -      116 110 -      121 120 -      136 130 -      174

EXTERNALS AND TAGS
OUTPTC - S00100  STOP - S00200  SIN - S00300  ASIN - S00400
END - S00500

BLOCK NAMES AND LENGTHS
BLOCK12- 66C01

VARIABLE ASSIGNMENTS
DOWNINC- 65C01 DT - 0C01 TIME - 210  NTEMP - 62C01
NTIFLAG- 63C01 PI - 207  REALTI - 211  TPLUS - 212
UPINC - 64C01

START OF CONSTANTS
162

START OF TEMPORARIES
204

START OF INDIRECTS
207

START OF VARIABLES
207

SPACE REQUIRED TO COMPILE -- DELTEMP
33200
```

DELTEMP

DELTEMP



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APPENDIX 4

SAMPLE PROBLEMS

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APPENDIX 4. SAMPLE PROBLEMS

TYPE OF PROGRAM-MODEL

```
*****  
*  
* SLAB DIMENSIONS *  
*  
*****
```

```
SLAB LENGTH      = 6.000E+01  
SLAB WIDTH       = 2.400E+01  
NUMBER OF INCREMENTS = 100  
FRICTION FACIOR  = 2.000E+00  
MAX. CRACKWIDTH  = 3.000E-02
```

NON-REINFORCEMENT OPTION

```
*****  
*  
* STEEL PROPERTIES *  
*  
*****
```

TYPE OF LONGITUDINAL REINFORCEMENT IS  
DEFORMED BARS

```
PERCENT REINFORCEMENT = 0.  
BAR DIAMETER          = 6.250E-01  
YIELD STRESS          = 6.000E+04  
ELASTIC MODULUS       = 2.900E+07  
THERMAL COEFFICIENT   = 5.000E-06
```

```
*****  
*  
* CONCRETE PROPERTIES *  
*  
*****
```

```
SLAB THICKNESS      = 1.000E+01  
THERMAL COEFFICIENT = 6.000E-06  
TOTAL SHRINKAGE     = 4.000E-04  
UNIT WEIGHT CONCRETE = 1.440E+02  
COMPRESSIVE STRENGTH = 4.000E+03  
(TENS/FLEX)RATIO    = 6.666E-01
```

TENSILE STRENGTH DATA

\*\*\*\*\*

NO TENSILE STRENGTH DATA IS INPUT BY USER  
 THE FOLLOWING AGE-TENSILE STRENGTH RELATIONSHIP  
 IS USED WHICH IS BASED ON THE RECOMMENDATION  
 GIVEN BY U.S. BUREAU OF RECLAMATION

AGE, TENSILE  
 (DAYS) STRENGTH

0.0	0.0
1.0	86.9
3.0	183.6
5.0	230.9
7.0	257.6
14.0	300.3
21.0	323.0
28.0	333.3

\*\*\*\*\*  
 \*  
 \* SLAB-BASE FRICTION CHARACTERISTICS \*  
 \* F-Y RELATIONSHIP \*  
 \*  
 \*\*\*\*\*

TYPE OF FRICTION CURVE IS A STRAIGHT LINE

MAXIMUM FRICTION FORCE= 3.000  
 MOVEMENT AT SLIDING = 0.010

\*\*\*\*\*  
 \*  
 \* TEMPERATURE DATA \*  
 \*  
 \*\*\*\*\*

CURING TEMPERATURE= 75.0

DAY	MINIMUM TEMPERATURE	DROP IN TEMPERATURE
1	55.0	20.0
2	55.0	20.0
3	55.0	20.0
4	55.0	20.0
5	55.0	20.0
6	55.0	20.0
7	55.0	20.0
8	55.0	20.0
9	55.0	20.0
10	55.0	20.0
11	55.0	20.0
12	55.0	20.0
13	55.0	20.0
14	55.0	20.0
15	55.0	20.0

16	55.0	20.0
17	55.0	20.0
18	55.0	20.0
19	55.0	20.0
20	55.0	20.0
21	55.0	20.0
22	55.0	20.0
23	55.0	20.0
24	55.0	20.0
25	55.0	20.0
26	55.0	20.0
27	55.0	20.0
28	55.0	20.0

MINIMUM TEMPERATURE EXPECTED AFTER  
 CONCRETE GAINS FULL STRENGTH = 0 DEGREES FARENHITE

```

*****
*                                     *
*           ITERATION AND TOLERANCE CONTROL           *
*                                     *
*****

```

MAXIMUM ALLOWABLE NUMBER OF ITERATIONS= 20  
 RELATIVE CLOSURE TOLERANCE= 1.0 PERCENT

FOR THE GIVEN INPUT DATA, THE LENGTH OF THE NON-  
 REINFORCED SLAB IS 1.000E+02 INCHES.

## T OF PROGRAM-MODEL1

```
*****
*
*          SLAB DIMENSIONS          *
*
*****
```

```
SLAB LENGTH      = 6.000E+01
SLAB WIDTH       = 2.400E+01
NUMBER OF INCREMENTS= 100
FRICTION FACTOR  = 2.000E+00
MAX. CRACKWIDTH  = 3.000E-02
```

## STEEL DESIGN OPTION

```
*****
*
*          STEEL PROPERTIES          *
*
*****
```

TYPE OF LONGITUDINAL REINFORCEMENT IS  
DEFORMED BARS

```
PERCENT REINFORCEMENT = 0.
BAR DIAMETER          = 6.250E-01
YIELD STRESS          = 6.000E+04
ELASTIC MODULUS       = 2.900E+07
THERMAL COEFFICIENT   = 5.000E-06
```

```
*****
*
*          CONCRETE PROPERTIES          *
*
*****
```

```
SLAB THICKNESS      = 1.000E+01
THERMAL COEFFICIENT = 6.000E-06
TOTAL SHRINKAGE     = 4.000E-04
UNIT WEIGHT CONCRETE= 1.440E+02
COMPRESSIVE STRENGTH= 4.000E+03
(TENS/FLEX)RATIO    = 6.666E-01
```

TENSILE STRENGTH DATA

\*\*\*\*\*

NO TENSILE STRENGTH DATA IS INPUT BY USER  
 THE FOLLOWING AGE-TENSILE STRENGTH RELATIONSHIP  
 IS USED WHICH IS BASED ON THE RECOMMENDATION  
 GIVEN BY U.S. BUREAU OF RECLAMATION

AGE, TENSILE  
 (DAYS) STRENGTH

0.0	0.0
1.0	86.9
3.0	183.6
5.0	230.9
7.0	257.6
14.0	300.3
21.0	323.0
28.0	333.3

\*\*\*\*\*  
 \*  
 \* SLAB-BASE FRICTION CHARACTERISTICS \*  
 \* F-Y RELATIONSHIP \*  
 \*  
 \*\*\*\*\*

TYPE OF FRICTION CURVE IS A STRAIGHT LINE

MAXIMUM FRICTION FORCE= 3.000  
 MOVEMENT AT SLIDING = -0.010

\*\*\*\*\*  
 \*  
 \* TEMPERATURE DATA \*  
 \*  
 \*\*\*\*\*

CURING TEMPERATURE= 75.0

DAY	MINIMUM TEMPERATURE	DROP IN TEMPERATURE
1	55.0	20.0
2	55.0	20.0
3	55.0	20.0
4	55.0	20.0
5	55.0	20.0
6	55.0	20.0
7	55.0	20.0
8	55.0	20.0
9	55.0	20.0
10	55.0	20.0
11	55.0	20.0
12	55.0	20.0
13	55.0	20.0
14	55.0	20.0
15	55.0	20.0



16	55.0	20.0
17	55.0	20.0
18	55.0	20.0
19	55.0	20.0
20	55.0	20.0
21	55.0	20.0
22	55.0	20.0
23	55.0	20.0
24	55.0	20.0
25	55.0	20.0
26	55.0	20.0
27	55.0	20.0
28	55.0	20.0

MINIMUM TEMPERATURE EXPECTED AFTER  
CONCRETE GAINS FULL STRENGTH = 0 DEGREES FARENHITE

```
*****
*                               *
*           ITERATION AND TOLERANCE CONTROL           *
*                               *
*****
```

MAXIMUM ALLOWABLE NUMBER OF ITERATIONS= 20

RELATIVE CLOSURE TOLERANCE= 1.0 PERCENT

FOR ITYPER EQUAL TO 1, THE TRANSVERSE STEEL IS 5.333E-02 PERCENT SPACED. 5.752E+0  
INCHES CENTER TO CENTER.

WIDTH OF FIRST CRACK IS .0084 INCHES AT TIME .4791 DAYS.

WIDTH OF FIRST CRACK IS .0087 INCHES AT TIME .4860 DAYS.

WIDTH OF FIRST CRACK IS .0089 INCHES AT TIME .4927 DAYS.

WIDTH OF FIRST CRACK IS .0093 INCHES AT TIME .5048 DAYS.

WIDTH OF FIRST CRACK IS .0095 INCHES AT TIME .5000 DAYS.

WIDTH OF FIRST CRACK IS .0103 INCHES AT TIME .5176 DAYS.

AT THE END OF 28 DAYS NO SECOND CRACK OCCURS

LONGITUDINAL STEEL = 7.173E-01 PERCENT.

SPACED = 4.277E+00 INCHES CENTER TO CENTER

## T OF PROGRAM-MODEL1

```

*****
*
*           SLAB DIMENSIONS           *
*
*****

```

```

SLAB LENGTH      = 6.000E+01
SLAB WIDTH       = 2.400E+01
NUMBER OF INCREMENTS = 100
FRICTION FACTOR  = 2.000E+00
MAX. CRACKWIDTH  = 3.000E-02

```

## SLAB ANALYSIS OPTION

```

*****
*
*           STEEL PROPERTIES         *
*
*****

```

TYPE OF LONGITUDINAL REINFORCEMENT IS  
DEFORMED BARS

```

PERCENT REINFORCEMENT = 2.000E-01
BAR DIAMETER          = 6.250E-01
YIELD STRESS          = 6.000E+04
ELASTIC MODULUS       = 2.900E+07
THERMAL COEFFICIENT   = 5.000E-06

```

```

*****
*
*           CONCRETE PROPERTIES     *
*
*****

```

```

SLAB THICKNESS      = 1.000E+01
THERMAL COEFFICIENT = 6.000E-06
TOTAL SHRINKAGE     = 4.000E-04
UNIT WEIGHT CONCRETE = 1.440E+02
COMPRESSIVE STRENGTH = 4.000E+03
(TENS/FLEX)RATIO    = 6.666E-01

```

## TENSILE STRENGTH DATA

\*\*\*\*\*

NO TENSILE STRENGTH DATA IS INPUT BY USER  
 THE FOLLOWING AGE-TENSILE STRENGTH RELATIONSHIP  
 IS USED WHICH IS BASED ON THE RECOMMENDATION  
 GIVEN BY U.S. BUREAU OF RECLAMATION

AGE, TENSILE  
 (DAYS) STRENGTH

0.0	0.0
1.0	86.9
3.0	183.6
5.0	230.9
7.0	257.6
14.0	300.3
21.0	323.0
28.0	333.3

\*\*\*\*\*  
 \*  
 \* SLAB-BASE FRICTION CHARACTERISTICS \*  
 \* F-Y RELATIONSHIP \*  
 \*  
 \*\*\*\*\*

TYPE OF FRICTION CURVE IS A STRAIGHT LINE

MAXIMUM FRICTION FORCE= 3.000  
 MOVEMENT AT SLIDING = -.010

\*\*\*\*\*  
 \*  
 \* TEMPERATURE DATA \*  
 \*  
 \*\*\*\*\*

CURING TEMPERATURE= 75.0

DAY	MINIMUM TEMPERATURE	DROP IN TEMPERATURE
1	55.0	20.0
2	55.0	20.0
3	55.0	20.0
4	55.0	20.0
5	55.0	20.0
6	55.0	20.0
7	55.0	20.0
8	55.0	20.0
9	55.0	20.0
10	55.0	20.0
11	55.0	20.0
12	55.0	20.0
13	55.0	20.0
14	55.0	20.0
15	55.0	20.0

16	55.0	20.0
17	55.0	20.0
18	55.0	20.0
19	55.0	20.0
20	55.0	20.0
21	55.0	20.0
22	55.0	20.0
23	55.0	20.0
24	55.0	20.0
25	55.0	20.0
26	55.0	20.0
27	55.0	20.0
28	55.0	20.0

MINIMUM TEMPERATURE EXPECTED AFTER  
 CONCRETE GAINS FULL STRENGTH = 0 DEGREES FARENHITE

```

*****
*                               *
*   ITERATION AND TOLERANCE CONTROL   *
*                               *
*****

```

MAXIMUM ALLOWABLE NUMBER OF ITERATIONS= 20

RELATIVE CLOSURE TOLERANCE= 1.0 PERCENT

WIDTH OF FIRST CRACK IS .0087 INCHES AT TIME .4245 DAYS.

STRESS IN THE STEEL 4.883E+04 IS GREATER THAN ITS WORKING STRENGTH AT TIME  
 3.000

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## THE AUTHORS

Felipe Vallejo-Rivero was born in Huauchinango, Puebla, Mexico, on January 20, 1950, the son of Rosa Lilia Rivero de Vallejo and Felipe Vallejo Perez. After completing high school at "Colegio Humboldt de Puebla," Puebla, Puebla, Mexico, in 1967, he entered Instituto Tecnológico y de Estudios Superiores de Monterrey, Monterrey, Nuevo Leon, Mexico. He received the degree of Civil Engineer from the Instituto Tecnológico y de Estudios Superiores de Monterrey, Monterrey, Nuevo Leon, Mexico. Felipe Vallejo-Rivero worked as resident Engineer and work-coordinator for a private contractor firm in highway construction in the State of Puebla, Mexico.

He was awarded with a scholarship from the Asociación Mexicana de Caminos through a special agreement between that agency and the Transportation Department of The University of Texas at Austin.

He attended the Intensive English Program for Foreign Students at The University of Texas at Austin.

Felipe Vallejo-Rivero is presently concerned with graduate studies in The Graduate School of Civil Engineering in The University of Texas at Austin, and also assists in the research of rigid pavement performance at the Center for Highway Research at The University of Texas at Austin.

B. Frank McCullough is an Associate Professor of Civil Engineering at The University of Texas at Austin. He has strong interests in pavements and pavement design and has developed design methods for continuously reinforced concrete pavement currently used by the State Department of Highways and Public Transportation, U. S. Steel Corporation, and others. He has also developed overlay design methods now being used by the FAA, U. S. Air Force, and FHWA. During nine years with the State Department of Highways and Public Transportation he was active in a variety of research and design activities. He worked for two years with Materials Research and



Development, Inc., Oakland, California, and for the past eight years for The University of Texas at Austin. He participates in many national committees and is the author of over 100 publications that have appeared nationally.