## EFFECT OF RAIN ON FREEWAY CAPACITY

by
E. Roy Jones
and
Merrell E. Goolsby

Research Report Number 24-23

Freeway Surveillance and Control
Research Study Number 2-8-61-24

Sponsored by
The Texas Highway Department
in cooperation with the
U.S. Department of Transportation

Federal Highway Administration
Bureau of Public Roads

August 1969
TEXAS TRANSPORTATION INSTITUTE
Texas A\&M University
College Station, Texas


#### Abstract

Capacity of a freeway is dependent upon physical factors of the roadway, traffic factors, and environmental factors. The effect on capacity of physical and traffic factors has been extensively investigated. However, little study has been devoted to the effect on capacity of environmental factors. This investigation determined the effect of rain, one of the most common environmental disturbances, on freeway capacity.

Rainfall records and extensive traffic flow data of the Gulf Freeway Surveillance and Control Center were used to define the effect of rain on capacity. Rain was found to reduce freeway capacity to between $81 \%$ and $86 \%$ of dry weather capacity with. $95 \%$ confidence.


SUMMARY

Capacity, the ability of a roadway to accommodate traffic, is one of the primary parameters Highway and Traffic Engineers must consider in the design and operation of traffic facilities. Freeway capacity is dependent upon physical features of the roadway, traffic factors, and environmental factors. The investigation described in this report quantifies the effect on freeway capacity of rain, one of the most common environmental disturbances.

The study was conducted on the Gulf Freeway in Houston utilizing extensive traffic flow data from the Data Acquisition and Control Computer System of the Gulf Freeway Surveillance and Control Center. Rainfall records from the U.S. Weather Bureau were merged with traffic data to determine the effect of rain.

Two bottlenecks of the inbound freeway were selected for analysis. Flow and density data for five-minute periods for a single peak period are adequate for fitting a mathematical traffic flow model relating flow, density, and speed. Maximum flow rate from the fitted curve is considered to be the capacity for that peak period. It was found that the capacity of the freeway during rain was between $81 \%$ and $86 \%$ of dry weather capacity with $95 \%$ confidence.

## IMPLEMENTATION STATEMENT

The quantitative measurement of the capacity-reducing effect of rain has several possible applications in a freeway control system. Since freeway control systems are based, in some fashion, on the capacitydemand relationship of the freeway, refinements in the determination of capacity will be reflected in greater effectiveness and reliability of control.

An automatic freeway control system should be able to. sense a .. change or impending change in the environment and through appropriate strategy, immediately react to the change. This form of control is preferable to that form which relies solely on measuring the effect of the environmental conditions on the traffic flow. The disadvantage in sensing the environment indirectly in this manner by sensing its effect are:
(1) The cause of the change in flow is not known and inappropriate corrective action may be taken to restore equilibrium.
(2) Some loss of efficiency will already have been suffered due to the delay in waiting for a measurable change in traffic operation.
(3) The need to take corrective action rather than providing precautionary measures in advance means that a larger margin must be used to avoid a breakdown in operation.

Flexibility in control strategies to compensate for the effect of rain on capacity can be designed into simple control systems which are based on historical traffic data as well as the more complex systems using real-time traffic inputs and digital computers. The use of digital computer
easily utifize real-cime inputs of environmental conalcions, cnence control modifications based on these inputs. Such a system might have instrumented rain detectors to transmit the presence of rain in the control area, at which time immediate control modifications based on predicted capacity reductions would be made in the controller.

Drew, et. al. ${ }^{1}$ considered freeway control systems using a multilevel approach. An application of these findings could be applied at the highest level of control, called the "self-organizing function." It is at this level that self-learning by the computer can occur. Given adequate inputs of environmental conditions and bottleneck flow rates the computer can re-evaluate, update and actually "learn" the capacities of the bottlenecks under each environmental category. The values could be applied to modify control when environmental changes occur.

## TABLE OF CONTENTS

ABSTRACT ..... ii
SUMMARY ..... iii
IMPLEMENTATION STATEMENT ..... Iv
INTRODUCTION ..... 1
STUDY OUTLINE ..... 3
ANALYSIS AND RESULTS ..... 5
DISCUSSION OF RESULTS ..... 23
CONCLUSIONS ..... 29
REFERENCES ..... 30

The opinions, findings, and conclusions expressed in this report are those of the authors and not necessarily those of the Bureau of Public Roads.

## INTRODUCTION

Capacity of a section of freeway is dependent upon a number of variables which fall into three classifications: (1) physical factors, such as roadway width, clearance, and grade; (2) traffic factors, such as distribution of vehicle types or driver characteristics; (3) environmental factors, such as lighting conditions, rain, fog, and ice. From these classifications it can be seen that capacity is not a fixed value dependent upon physical constraints alone, but varies with temporal changes in traffic and environmental factors. Only the physical factors contributing to capacity remain constant.

The effect on capacity of the physical and traffic factors has been extensively investigated. ${ }^{2}$ Moskowitz and Newman reported in 1963 that the effects of weather and lighting conditions were not treated at all in their research on freeway capacity and that this represented a deficiency in knowledge at that time. ${ }^{3}$ A survey of technical literature indicates little has been done to fill this void in knowledge.

The advent of freeway control as an operational reality has emphasized the need for a clear, quantitative determination of freeway capacity under all conditions. Although no unified approach to the design of freeway control systems has been generally accepted, the basic control techniques are not likely to change appreciably. The fundamental purpose of freeway control is to limit the traffic demand on the facility to some percentage of the capacity. If the demand exceeds the capacity, even for a short period of time, a breakdown in flow occurs, congestion sets in,
and the rate of flow reduces to a value lower than that which the facility could support under free flow conditions. Thus the success of a control system depends to some extent on its ability to respond to changes in the environment which affect its capacity.

The objective of this investigation is to determine the effect on capacity of rain, which is one of the most frequently experienced environmental disturbances.

The facility chosen for this capacity study was the Gulf Freeway in Houston, since it is the only facility in existence capable of the extensive data collection desired. The Gulf Freeway Surveillance and Control system is a product of six years of research. It now serves as both a research facility and as an operational freeway control system. This research was conducted by Texas Transportation Institute for the Texas Highway Department in cooperation with the Bureau of Public Roads, U. S. Department of Transportation.

Central control equipment includes a digital computer (Process Control and Data Acquisition System) and ancillary equipment. The computer is used for real-time control of the freeway during peak periods of the day, and to collect and store records of traffic flow and density. These records are collected by minute for each of four closed subsystems of detection on the inbound roadway during the morning peak period, 6:30-8:30 AM.

Measures of flow and density for a single peak period are adequate data for fitting a mathematical traffic flow model relating flow, density and speed. Statistical methods were used to fit and test the acceptability of the model. The model yields a maximum flow value which is defined, for the purpose of this report, as the capacity for that day. Identifying the peak of the curve relating flow rate and density to capacity is valid only if demand was sufficient to exceed capacity. This condition would be satisfied if the data points used to obtain each curve of best fit included points at or near the peak with densities higher than "cricital" or optimum
density. This requirement was satisfied by the data used.
Rainfall records were obtained from the Weather Bureau Station at William P. Hobby airport, located four miles southeast of the control center and from the station in downtown Houston, four miles northwest of the control center. These data were used to estimate the likelihood of precipitation during peak periods to determine the degree of application of results of this study. In addition, logs kept in the control center were used to verify weather conditions for each day.

The relationship of rainfall intensity to cap ity could not be identified because of the limitations created by varying rainfall rates both in time and space. Only an extensive long term study could hope to reveal this relationship. For this reason, days were simply classed as dry or rain. Where no clear-cut classification was possible, the data were not utilized. Further, the statistical tests applied to the data tended to discount those days where consistent weather conditions did not prevail through the entire peak period.

## ANALYSIS AND RESULTS

Processing of the data consisted of two main steps. The first was the processing of traffic data for a particular section of freeway with the objective of estimating the capacity of that section on each morning of operation. The second stage was the linking of this capacity to the weather condition prevailing during the collection of data to determine if there was any significant effect of rain on capacity.

## Basic Traffic Data

The collected data consisted of one minute vehicle detector counts taken in a 3.5 -mile section of the inbound freeway. The location of these detectors and the subdivision of the freeway into four subsystems numbered 2 to 5 are illustrated in Figure 1.

These one-minute counts were converted into flow rates and average densities for five-minute periods. The average densities were determined in units of vehicles per mile for all three lanes in each subsystem. The average 5 -minute rates of flow were expressed as vehicles per hour. An. example of the 5 -minute average densities and flow rates is shown in Table 1.

The validity of equating maximum flow rates with capacity depended upon the use of traffic data containing densities high enough to force the flow rate downward. To increase this likelihood, the traffic operations at two potential bottlenecks were selected for study. The first bottleneck, known as the "Griggs overpass" is located in subsystem 3, and the second,


FIG. I. LOCATION OF VEHICLE DETECTORS. ON INBOUND GULF FREEWAY

| 5 MIN | VPH | DEN | VPH | DEN | VPH | VPH | DEN | VPH | DEN | VPH | VPH | DATE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PERIOD | AT | IN | AT | IN | AT | AT | IN | AT | IN | AT | AT |  |
| ENOING | 225 | SS2 | WOOURG | SS3 | OVERPS | BAYOU | SS4 | TELEPH | SS5 | MERGE | CUMBLE |  |
| 5 | 2184 | 18 | 2916 | 55 | 2256 | 1920 | 30 | 1296 | 19 | 1320 | 516 | 62568 |
| 10 | 2304 | 22 | 3792 | 71 | 3792 | 3048 | 47 | 3576 | 56 | 3636 | 3216 | 62568 |
| 15 | 2412 | 28 | 4320 | 83 | 4548 | 3888 | 56 | 3828 | 66 | 4032 | 3168 | 62568 |
| 20 | 2844 | 27 | 4692 | 95 | 4668 | 4080 | 62 | 4272 | 78 | 4380 | 3552 | 62568 |
| 25 | 3612 | 46 | 5340 | 107 | 5220 | 4452 | 68 | 4728 | 95 | 4896 | 4116 | 62568 |
| 30 | 3600 | 49 | 5760 | 149 | 5844 | 5232 | 82 | 5544 | 118 | 5736 | 4392 | 62568 |
| 35 | 3852 | 54 | 5076 | 151 | 5388 | 4824 | 82 | 5352 | 119 | 5760 | 4704 | 62568 |
| 40 | 4200 | 62 | 5424 | 151 | 5688 | 5124 | 89 | 5304 | 112 | 5496 | 4656 | 62568 |
| 45 | 3816 | 70 | 5040 | 150 | 5664 | 5112 | 102 | 5472 | 131 | 5712 | 4920 | 62568 |
| 50 | 4152 | 71 | 5208 | 154 | 5736 | 5316 | 99 | 5640 | 138 | 5916 | 5004 | 62568 |
| 55 | 4452 | 78 | 5040 | 143 | 5808 | 5280 | 94 | 5760 | 160 | 6240 | 5364 | 62568 |
| 60 | 4488 | 94 | 4956 | 171 | 5496 | 5124 | 94 | 5376 | 158 | 5904 | 5376 | 62568 |
| 65 | 3780 | 101 | 4644 | 178 | 5700 | 5352 | 102 | 5460 | 171 | 5916 | 5124 | 62568 |
| 70 | 3516 | 104 | 4704 | 157 | 5472 | 5100 | 123 | 5184 | 186 | 5556 | 5232 | 62568 |
| 75 | 3816 | 102 | 4620 | 165 | 5220 | 4884 | 146 | 5208 | 192 | 5604 | 4992 | 62568 |
| 80 | 3588 | 115 | 4440 | 176 | 4980 | 4536 | 165 | 4776 | 176 | 5124 | 4992 | 62568 |
| 85 | 3264 | 110 | 4548 | 202 | 4812 | 4488 | 162 | 5076 | 177 | 5472 | 4668 | 62568 |
| 90 | 3948 | 112 | 3972 | 206 | 5208 | 4788 | 155 | 5208 | 189 | 5508 | 4764 | 62568 |
| 95 | 3228 | ¢9 | 4908 | 188 | 5316 | 4812 | 161 | 4896 | 183 | 5256 | 4800 | 62568 |
| 100 | 3804 | 91 | 4644 | 187 | 5184 | 4692 | 159 | 5280 | 178 | 5640 | 4932 | 62568 |
| 105 | 3180 | 84 | 4104 | 177 | 5196 | 4704 | 138 | 5208 | 175 | 5568 | 4656 | 62568 |
| 110 | 3480 | 70 | 4716 | 158 | 5160 | 4680 | 135 | 4944 | 192 | 5280 | 4464 | 62568 |
| 115 | 3324 | 42 | 5028 | 172 | 5136 | 4476 | 151 | 5052 | 181 | 5328 | 4392 | 62568 |
| 120 | 3732 | 46 | 4416 | 167 | 5256 | 4620 | 128 | 5472 | 182 | 5736 | 4740 | 62568 |
| 125 | 3264 | 35 | 5004 | 152 | 5316 | 4620 | 118 | 5316 | 178 | 5556 | 4392 | 62568 |
| 130 | 3324 | 3 C | 4728 | 141 | 5304 | 4608 | 102 | 5028 | 197 | 5244 | 4080 | 62568 |
| 135 | 3264 | 28 | 4488 | 99 | 4884 | 4404 | 110 | 4920 | 171 | 5016 | 4320 | 62568 |
| 140 | 168 | 1 | 960 | 15 | 2064 | 1728 | 39 | 3576 | 109 | 3732 | 4536 | 62568 |

TABLE 1. FLOW RATES AND DENSITIES ON THE INBOUND GULF FREEWAY, JUNE 25, 1968.
known as the "Telephone merge" is situated in subsystem 5 in the vicinity of Telephone Road.

## Model

For each of the two subsystems a pair of values representing flow rate, $q$, and density, $k$, was available for each five minutes of operation. The first and last two pairs of points were discarded to avoid errors due to starting and stopping of the system counting, leaving 24 to 30 pairs of $q$ and $k$ values in each subsystem on each day of records. The space-mean-speed, $u$, corresponding to each pair of values was then calculated as:

$$
\begin{equation*}
\mathrm{u}=\mathrm{q} / \mathrm{k} \tag{1}
\end{equation*}
$$

The model chosen for this analysis is the generalized macroscopic traffic flow model. ${ }^{4}$ Detailed development of the model is provided in the cited reference. This model is stated as:

$$
\begin{align*}
q=k \cdot u_{f}\left\{1-\left(k / k_{j}\right)^{(n+1) / 2}\right\} & n>-1  \tag{2}\\
u=u_{f}\left\{1-\left(k / k_{j}\right)^{(n+1) / 2}\right\} & n>-1 \tag{3}
\end{align*}
$$

For a value of the exponent, $n$, this model relates the flow rate $q$, or speed, $u$, to density, $k$. The two parameters, $u_{f}$, and $k_{j}$, are known as the "free-speed" and "jam density" respectively. The value of the exponent parameter is restricted to be greater than -1 .

The model was used in the following manner. $A$ value of $n$ was
selected as an initial value and a least-squares regression analysis was performed with equation (3) to give the value of $u_{f}$ and $k_{j}$ for the best fit to a particular day's data. The residual mean square of the fitted curve to the data was calculated. A second value of $n$ was then selected and the regression analysis repeated. If this value of $n$ resulted in $a$ closer fit, as indicated by a smaller residual mean square value, that value of $n$ was chosen as preferable to the first value. This process was repeated using a Fibonacci Search Technique ${ }^{4}$ until the optimum value of $n$ was determined.

Substituting the values of $n, u_{f}$, and $k_{j}$ thus determined in equation (3) provides the optimum flow-density model for the particular freeway subsystem and day. The maximum value of $q$ in equation (2) was determined and reported as the capacity. The ratio of the highest observed 5-minute flow rate to the capacity was determined to provide a subjective comparison of the model capacity to the maximum observed flow rate.

Acceptability of Model
The model error was statistically tested to provide an indication of how closely the optimum model fitted the data. Under the hypothesis that the model error was zero, the probability of the occurrance of the data was determined and reported as the acceptance level. This probability value is in effect, the significance level, or level of confidence, at which the model would be accepted. The variance of speed for a fixed density used in this determination was determined on a very large sample of data from which a few very divergent results were excluded. This resulted in a rigorous test with 231 degrees of freedom. The level at which the model was
selected as acceptable was chosen as $10 \%$, but the sensitivity of the final conclusions to this choice was investigated.

## Example of Traffic Model Output

Tables 2 and 3 show the result of fitting models to the data for the morning of June 25 , 1968, in subsystem 3 and 5 respectively. The variable names used in these computer print-outs are:
$E N=$ The $n$ value used in the model equation.
RSMS = Residual mean square, a measure of how closely the model fitted the data. A smaller value indicated a closer fit, with the optimum model having the smallest value.

DJ = Jam Density
$\mathrm{UF}=$ Free Speed. (This is theoretically infinite when $n=-1$.)

QM = Maximum Flow Rate, or the crest of the model curve. This is the capacity.

A-Level = Acceptance level as described above. A measure of the acceptability of the model.

Ratio = Ratio of max observed 5-minute flow rate to QM .

In the case of subsystem number 3 (Table 2), the equation of the optimum model would be:

$$
\begin{array}{ll} 
& q=k \cdot 89.02\left\{1-(k / 319 \cdot 96)^{0.7}\right\} \\
\text { or } \quad & u=89.02\left\{1-(k / 319 \cdot 96)^{0.7}\right\}
\end{array}
$$



TABLE 2. TRAFFIC MODEL FIT FOR SUB-SYSTEM 3, JUNE 25, 1968.

DATE $=02568$ SUB-SYSTEM NUMEER 5

|  | EN= | -1.00 | RSMS $=$ | 4.611 | OJ= | 468.11 | UF = | ******* | QM $=$ | 5057.47 | $\triangle-L E V E L=$ | 0. 277208 | RAT $10=$ | 1.103 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | EN= | -0.80 | RSMS $=$ | 4.117 | $0 \mathrm{~J}=$ | 432.54 | UF = | 373.48 | QM $=$ | 5662.07 | A-LEVEL $=$ | 0.143890 | RATIO= | 1.102 |
|  | EN= | -0.60 | RSMS $=$ | 3.671 | DJ= | 404.73 | UF = | 2197.25 | $C M=$ | 5672.64 | $A-L E V E L=$ | 0.241876 | RATIO= | 1.100 |
|  | EN= | -0.40 | RSMS $=$ | 3.265 | DJ $=$ | 382.40 | UF = | 154.53 | OM $=$ | 5687.05 | A-LEVEL $=$ | 0.368291 | RATIO= | 1.097 |
|  | EN= | -0.20 | RSMS = | 2.913 | DJ $=$ | 364.07 | UF = | 127.18 | $C M=$ | 57 C 4.25 | A-LEVEL $=$ | 0.507629 | RATIO= | 1.094 |
|  | EN= | 0.00 | RSMS $=$ | 2.603 | DJ= | 348.77 | UF = | 110.77 | $Q M=$ | 5723.42 | A-LEVEL $=$ | 0.646675 | RATIO = | 1.090 1.086 |
|  | EN= | 0.20 | RSMS $=$ | 2.334 | D J = | 335.89 | UF= | 99.84 | $C M=$ | 5744.03 | A-LEVEL $=$ | 0.763665 | RATIO= | 1.086 1.082 |
|  | EN= | 0.40 | RSMS $=$ | 2.108 | D $\mathbf{J}=$ | 324.69 | UF = | 92.03 | OM $=$ | 5765.71 | A-LEVEL | 0.850779 | RATIO= | 1.082 1.078 |
|  | EN= | 0.00 | RSMS $=$ | 1.924 | OJ= | 315.06 | UF = | 85.18 | OM $=$ | 5788.08 | A-LEVEL $=$ | 0.908493 0.928657 | RATIO $=$ | 1.078 1.074 |
|  | EN= | 0.80 | RSMS $=$ | 1.779 | OJ $=$ | 306.64 | UF $=$ UF $=$ | 81.63 77.99 | QM $\quad$ M $=$ | 5810.91 5834.05 | A-LEVEL $=$ | 0.948726 | RATIO= | 1.074 1.070 |
|  | EN= | 1.00 | RSMS $=$ | 1.673 | $\mathrm{DJ}=$ | 299.22 | UF = | 77.99 | GM $=$ | 5834.05 |  |  |  |  |
|  | EN= | 1.00 | RSMS $=$ | 1.673 | $\mathrm{DJ}=$ | 299.22 | UF= | 77.99 | QM $=$ | 5834.05 | A-LEVEL $=$ | 0.948726 | RATIO= | 1.070 |
|  | EN= | 2.00 | RSMS $=$ | 1.654 | D J = | 272.40 | UF = | 67.00 | UM $=$ | 5949.90 | A-LEVEL $=$ | 0.951740 | RATIO $=$ | 1.049 |
|  | EN= | 3.00 | RSMS $=$ | 2.349 | D J = | 255.77 | UF = | 61.50 | QM $=$ | 6060.18 | A-LEVEL $=$ | 0.757669 | RATIO= | 1.030 |
|  | EN= | 4.00 | RSMS $=$ | $\underline{3.566}$ | DJ $=$ | 244.56 | UF = | 58.22 | CMM | 6161.48 | A-LEVEL $=$ | U.271201 | RATIO= | 1.013 0.098 |
|  | EN= | 5.00 | RSMS $=$ | 5.149 | DJ $=$ | 233.55 | UF = | 55.95 | QM CM | 6253.60 6334.96 | A-LEVEL A-LEVEL | 0.037519 0.001580 | RATIU RATIO | 1.0198 0.985 |
|  | EN= | 6.00 | RSMS $=$ | 6.975 | DJ= | 230.58 225.94 | UF $=$ UF $=$ | 54.29 53.00 | OM $\mathrm{OM}=$ | 6334.90 6408.00 | A-LtVEL $=$ | 0.000321 | RATIO= | 0.974 |
| N | EN= | 7.00 | RSMS $=$ RSMS $=$ | $8.97 C$ 11.064 | DJ $=$ $0 \mathrm{~J}=$ | 225.99 222.36 | UF $=$ UF $=$ | 51.97 | $Q M=$ | 6472.92 | A-LEVEL $=$ | n.000000 | RAT10= | 0.964 |
|  | EN $=$ EN $=$ | 8.00 9.00 | RSMS $=$ RSMS $=$ | 11.064 13.222 | DJ= | 2219.46 | UF = | 51.10 |  | 6530.42 | A-LEVEL $=$ | 0.000000 | RATIO= | 0.955 |
|  | EN $=$ EN $=$ | 9.00 10.00 | RSMS $=$ RSMS $=$ | 13.422 15.418 | DJ= | 219.44 217.05 | UF = | 50.36 | $Q M=$ | 6581.27 | A-LEVEL $=$ | 0.000000 | RATIO= | 0.948 |

OPTIMUM (CLOSEST FITTING MODEL) IS AS SET OUT BELCW

Figures 2 to 5 are computer plots of speed (u) against density (k) and flow rate (q) against density for both subsystems on the same day. The observed data points are shown, and the optimum model curve is also drawn on each plot.

Further examples of plotted traffic data output are shown in figures 6 to 9. These figures give an indication of the range of model parameters used and indicate that the optimum models did, in fact, fit the data well when the acceptance level was high.

## Results

The condensed results of capacity, acceptance level of the model, and weather condition are shown in Table 4. Those capacities with an acceptance level greater than $10 \%$ are shown with an $A$ for accept, and those with an acceptance level between $1 \%$ and $10 \%$ are shown with a $D$ for doubtful. From an original source of 24 days, only 11 days in subsystem 3 and 10 days in subsystem 5 were acceptable at the $10 \%$ level.


FIGURE 2. SPEED-DENSITY RELATIONSHIP FOR SUB-SYSTEM 3, JUNE 25, 1968.


FIGURE 3. FLOW-DENSITY RELATIONSHIP FOR SUB-SYSTEM 3, JUNE 25, 1968.


FIGURE 4. SPEED-DENSITY RELATIONSHIP FOR SUB-SYSTEM 5, JUNE 25, 1968.


FIGURE 5. FLOW-DENSITY RELATIONSHIP FOR SUB-SYSTEM 5, JUNE 25, 1968.


FIGURE 6. SPEED-DENSITY RELATIONSHIP FOR SUB-SYSTEM 3, JUNE 26, 1968.


FIGURE 7. FLOW-DENSITY RELATIONSHIP FOR
SUB-SYSTEM 3, JUNE $26,1968$.


FIGURE 8. SPEED-DENSITY RELATIONSHIP FOR
SUB-SYSTEM 5, JUNE 26, 1968.


FIGURE 9. FLOW-DENSITY RELATIONSHIP FOR SUB-SYSTEM 5, JUNE 26, 1968.

TABLE 4. CAPACITIES AND MODEL ACCEPTANCE LEVELS

| Date |  | Dry/Wet | SUB-SYSTEM 3 |  |  | SUB-SYSTEM 5 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{gathered} \text { Capacit } \\ \text { VPM } \end{gathered}$ |  | Acceptance Level | Capaci VPM |  | Acceptance Level |
| Feb | 13 | Wet | 4795 D | D | . 0772 | 4817 |  | . 0000 |
| Mar | 21 | Wet | 5000 | U | . 0079 | 4932 | U | . 0001 |
| May | 6 | Dry | 5836 D | D | . 0404 | 5917 | A | . 2903 |
| May | 7 | Dry | 5541 |  | . 2340 | 5883 | A | . 2342 |
| May | 8 | Wet | 5338 U |  | . 0000 | 5792 | D | . 0350 |
| May | 9 | Dry | 5684 D | D | . 0422 | 5688 | D | . 0180 |
| June | 6 | Dry | 5640 A | A | . 5199 | 5933 | A | . 8764 |
| June | 12 | Dry | 5732 A | A | . 3795 | 5883 | A | . 9195 |
| June | 21 | Wet | 4530 | A | . 9494 | 4685 | A | . 8022 |
| June | 25 | Dry | 5495 | A | . 8388 | 5892 | A | . 9653 |
| June | 26 | Wet | 4729 | A | . 9602 | 4733 | D | . 0542 |
| Aug | 14 | Dry | 5554 | U | . 0002 | 5710 | A | . 1134 |
| Sept | 12 | Dry | 5652 | U | . 0000 | 5762 | D | . 0241 |
| Sept | 23 | Wet | 5140 | D | . 0872 | 5359 | D | . 0702 |
| Oct | 17 | Dry | 5380 | U | . 0000 | 5520 | U | . 0000 |
| Oct | 21 | Dry | 5284 | A | . 8282 | 5689 | A | . 9901 |
| Oct | 29 | Dry | 5711 | U | . 0025 | 5853 | A | . 5382 |
| Oct | 30 | Dry | 5340 | U | . 0089 | 5619 | U | . 0003 |
| Oct | 31 | Dry | 5641 | A | . 4463 | 5708 | U | . 0000 |
| Nov | 5 | Dry | 5639 | A | . 1961 | 5829 | U | . 0000 |
| Nov | 6 | Dry | 5592 | A | . 1340 | 12092 | U | . 0000 |
| Nov | 7 | Dry | 5595 | U | . 0001 | 5675 | U | . 0000 |
| Nov | 8 | Wet | 5208 | U | . 0000 | 89554 | U | . 0000 |
| Dec | 12 | Wet | 4770 | A | . 9759 | 4995 | A | . 2576 |

(A denotes acceptable; D, doubtful; $U$, unacceptable)

## DISCUSSION OF RESULTS

The general attrition of data due to its apparent unacceptability in fitting the model might lead the reader to the false conclusion that the theoretical model used is inappropriate. No mathematical model can perfectly describe the reality which it represents, and the sophistication of the model chosen will depend upon what aspects of reality it is desired that it represent.

A model was desired in this study which would adequately permit the determination of capacity from the flow density relationship. Any model chosen to fit traffic data on such a plane is subject to certain limitations. The first limitation already mentioned when discussing rainfall intensity is that the model is required to fit points which represent traffic operation over a period of time, in this case approximately two hours. With records of vehicle flow rates and densities, even the most sophisticated model could not cope with a large change in, for example, truck percentages which alter the capacity. Similarly high intensity rain for a short period during the two hours could have the same effect. Accidents could also cause such a mixture of points for different conditions.

This resulted in the rejection of data where the conditions affecting flow rates were not uniform. This unacceptability of data applied irrespective of the degree of sophistication of the model chosen. A bias in favor of those data where conditions were uniform is exactly what is required by the objectives of this study. This
study is interested only in data taken when the conditions affecting capacity could be related to the capacity itself. The fact that the model did not reflect reality when conditions were variable is part of the data screening process, and does not reflect upon the worth of the model.

The accepted capacity values, classified by subsystem and weather condition are shown in Table 5. It should be emphasized that these values are representative of an entire set of compatible data points, and that they have survived a rigorous screening process. No value may be arbitrarily ignored as a freak, and each constitutes a very positive and definite representation of the capacity of the subsystem in question for the conditions prevailing during the study period of approximately two hours during which the set of data was obtained.

To compare the dry weather and wet weather capacities, all the capacities in each subsystem were "normalized." This means that the capacities were all reduced by the factor necessary to result in a dry weather capacity mean of 100 . The dry weather mean in subsystem 3 was 5570.5, and in subsystem 5 it was 5845.0. The subsystem 3 factor was therefore $100 / 5570.5$ and the subsystem 5 factor was 100/5845.0. In this way all capacities could be compared to a dry weather mean of 100 .

It can be seen that on the basis of a dry weather capacity of 100 , the wet weather capacity is about 84 . The sixteen dry weather capacities sampled fall within a range of 94.8 to 102.9 , or a range of approximately $5 \%$ of the mean. Statistical methods were used on these

TABLE 5. ACCEPTED CAPACITIES

| Sub-System | Date | V.P.H. | CAPACITY |  |
| :---: | :---: | :---: | :---: | :---: |
| Normalized | Dry/Wet |  |  |  |
| 3 | May 7 | 5541 | 99.47 | Dry |
| 3 | June 6 | 5640 | 101.25 | Dry |
| 3 | June 12 | 5732 | 102.90 | Dry |
| 3 | June 25 | 5495 | 98.64 | Dry |
| 3 | Oct 21 | 5284 | 94.86 | Dry |
| 3 | Oct 31 | 5641 | 101.27 | Dry |
| 3 | Nov 5 | 5639 | 101.34 | Dry |
| 3 | Nov 6 | 5592 | 100.39 | Dry |
| 3 | June 21 | 4530 | 81.32 | Wet |
| 3 | June 26 | 4729 | 84.89 | Wet |
| 3 | Dec 12 | 4770 | 85.63 | Wet |
| 5 | May 6 | 5917 | 101.23 | Dry |
| 5 | May 7 | 5883 | 100.65 | Dry |
| 5 | June 6 | 5933 | 101.51 | Dry |
| 5 | June 12 | 5883 | 100.65 | Dry |
| 5 | June 25 | 5892 | 100.80 | Dry |
| 5 | Aug 14 | 5710 | 97.69 | Drv |
| 5 | Oct 21 | 5689 | 97.33 | Dry |
| 5 | Oct 29 | 5853 | 100.14 | Dry |
| 5 | June 21 | 4685 | 80.15 | Wet |
| 5 | Dec 12 | 4995 | 85.42 | Wet |

data to establish the fact that rain has a highly significant effect on capacity, and that the wet weather capacity may be expected, with $95 \%$ confidence, to be between 81.2 and $85.8 \%$ of dry weather capacity. The dry weather capacities were all very closely bunched, so much so, that tolerance limits of 93.1 to 106.9 were calculated, within which $95 \%$ of the normalized dry weather capacities could be expected to lie. This provides some indication of the stability of capacity and its sensitivity to weather conditions.

The question of how much these results would differ if the model acceptance level were changed may now be investigated. Table 6 shows the additional results of capacity and weather conditions which would have to be considered if the acceptance level were changed from $10 \%$ to $1 \%$. The capacity figures are normalized by application of the same multiplying factors for subsystem 3 and 5 which were used in Table 5.

It can immediately be seen that the inclusion of the additional capacity measurements in Table 6 results in a bigger scatter of capacity values for each weather condition. An analysis of variance test on the entire set of results shown in Tables 5 and 6 nevertheless shows a highly significant difference between dry and wet weather capacities.

Having established that rain has a significant and drastic effect on capacity, the question regarding the likelihood of rain during the peak hours may be considered. It is hardly worthwhile providing protective measures against an event which may occur with negligable probability.

TABLE 6. CAPACITIES OF DOUBTFUL ACCEPTABILITY (Acceptance Level Between $1 \%$ and $10 \%$ )

| Sub-System | Date | V.P.H. | CAPACITY <br> Normalized | Dry/Wet |
| :---: | :---: | :---: | :---: | :---: |
| 3 | May 6 | 5836 | 104.77 | Dry |
| 3 | May | 9 | 5684 | 102.04 |
| 3 | Feb 13 | 4795 | 86.08 | Dry |
| 3 | Sept 23 | 5140 | 92.27 | Wet |
| 5 | May 9 | 5688 | Wet |  |
| 5 | Sept 12 | 5762 | 97.31 | Dry |
| 5 | May 8 | 5792 | Dry |  |
| 5 | June 26 | 4733 | 99.09 | Wet |
| 5 | Sept 23 | 5359 | 80.98 | Wet |

From a ten-year rainfall record in Houston, ${ }^{6}$ the number of occasions on which a certain amount of rain fell between certain hours was determined. The average frequency for various intensities of rain recorded during the hours $7-9$ a.m. and $4-6$ p.m. in Houston, is shown as Table 7. For example, the number of times that 0.25 inches or more of rain was observed during these hours was on the average of eight times per year.

Most of the rainfall recorded during the "wet" conditions For this research were greater than 0.02 inches. This amount is likely to occur about 50 times per year in Houston, summing morning and evening peak periods. This would seem to be a high enough frequency to warrant consideration in the design and control of Houston freeways.

TABLE 7. HOUSTON PRECIPITATION. FREQUENCY OF OCCURRENCE

$$
7-9 \text { a.m. } \quad 4-6 \text { p.m. }
$$

BOTH

|  | Frequency/ <br> Year | Frequency/ <br> Year | Frequency/ <br> Year | Cumulative <br> Frequency/ <br> Year |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| TRACE | 42.7 | 34.4 | 77.1 | 150.6 |
| $.00-$ | 12.6 | 20.4 | 73.5 |  |
| $.02-.01^{\prime \prime}$ | 7.8 | 15.8 | 18.2 | 34.0 |
| $.10-.24^{\prime \prime}$ | 5.7 | 1.6 | 11.3 | 53.1 |
| $.25-.49^{\prime \prime}$ | 2.3 | 3.8 | 19.1 |  |
| $.50-.99^{\prime \prime}$ | 1.3 | 0.3 | 0.6 | 7.8 |
| $1.00-1.99^{\prime \prime}$ | 0.3 |  | 0.1 | 0.6 |
| $2.00+$ |  |  | 0.1 | 4.0 |

CONCLUSIONS
Based on the results of this research, the following conclusions can be stated:

1. Rain significantly reduces freeway capacity.
2. The capacity of the freeway during rain can be expected to be $81 \%$ to $86 \%$ of the dry weather capacity with $95 \%$ confidence.
3. Dry weather capacity is very stable. Ninetyfive percent of the dry weather capacity values can be expected to fall within $7 \%$ of the mean observed capacity $99 \%$ of the time.
4. The frequency of rain during the peak periods in Houston is on the order of fifty times per year.
5. Drew, D., Brewer, K., Buhr, J., Whitson, R., 'Multilevel Approach Applied to the Design of a Freeway Control System," Presented at 48 th Annual Meeting of Highway Research Board, Washington, 1969.
6. Highway Research Board Committee on Highway Capacity, "Highway Capacity Manual," Special Report 87, 1965.
7. Moskowitz, Karl and Newman, Leonard, 'Notes on Freeway Capacity," Highway Research Report 27, 1963.
8. Drew, Donald R., "Traffic Flow Theory and Control," McGraw-Hill, New York, 1968.
9. Wilde, Douglas J., "Optimum Seeking Methods;" Prentice-Hall Inc. 1964.
10. U.S. Weather Bureau, "Climatography of the U.S. No. 40-41. Climatic Guide, Houston-Galveston, Texas Area," U.S. Government Printing office.
